| | SCHOOL OF PHYSICAL & M | ATHEMATICAL SCIENCES |
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| | MATHEN | MATICS |
| 'otal (| Duestions : 60 | Question Booklet Series |
| 'ime A | Allowed : 70 Minutes | Roll No. : |
| 1. | Instructions for Write your Entrance Test Roll Number in the spa and fill up the necessary information in the spaces | r Candidates : ace provided at the top of this page of Question Booklet provided on the OMR Answer Sheet. |
| 2. | OMR Answer Sheet has an Original Copy and a Ca entries in the Original Copy, candidate should en entries made in the Original Copy against each ite | andidate's Copy glued beneath it at the top. While making isure that the two copies are aligned properly so that the m are exactly copied in the Candidate's Copy. |
| 3. | All entries in the OMR Answer Sheet, including an only. | swers to questions, are to be recorded in the Original Copy |
| 4. | Choose the correct / most appropriate response darken the circle of the appropriate response con read by the OMR Scanner and no complaint to thi | for each question among the options A, B, C and D and npletely. The incomplete darkened circle is not correctly s effect shall be entertained. |
| 5. | Use only blue/black ball point pen to darken the gel/ink pen or pencil should be used. | circle of correct/most appropriate response. In no case |
| 6. | Do not darken more than one circle of options for response shall be considered wrong. | r any question. A question with more than one darkened |
| 7. | There will be 'Negative Marking' for wrong an 0.25 marks from the total score of the candidate. | swers. Each wrong answer will lead to the deduction of |
| 8. | Only those candidates who would obtain positive admission. | e score in Entrance Test Examination shall be eligible for |
| 9. | Do not make any stray mark on the OMR sheet. | |
| 10 | . Calculators and mobiles shall not be permitted insi | de the examination hall. |
| 11 | . Rough work, if any, should be done on the blank s | heets provided with the question booklet. |
| 12 | . OMR Answer Sheet must be handled carefully and be evaluated. | it should not be folded or mutilated in which case it will not |
| 13 | . Ensure that your OMR Answer Sheet has been sig | ned by the Invigilator and the candidate himself/herself. |
| 14 | . At the end of the examination, hand over the OMF original OMR sheet in presence of the Candidate | Answer Sheet to the invigilator who will first tear off the and hand over the Candidate's Copy to the candidate. |

1.

The solution of the linear partial differential equation 4.

2p+3q=1 is given by :

- (A) f(2x-y, 3y-z) = 0
- (B) f(3x-2y, y-3z) = 0
- (C) f(2x, 3y, z) = 0
- (D) None of these
- 2. The 2nd order partial differential equation

$$x \frac{\partial^2 z}{\partial x^2} + y \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = 3$$
, is elliptic if:

- (A) $y^2 > 12x$
- (B) $y^2 < 12x$
- (C) $y^2 < 4x$
- (D) $y^2 > 4x$
- 3. Choose the correct statement with regard to two bounded sets A and B such that $A \subset B$
 - I. $\sup A \leq \sup B$
 - II. infA≥infB
 - (A) Only I
 - (B) Only II
 - (C) Both I & II
 - (D) Neither I nor II

Any infinite subset of a countable set :

- (A) is countable
- (B) is uncountable
- (C) either countable or uncountable
- (D) does not exist
- 5. Choose the correct statement from the following :
 - (A) The supremum of a bounded set always belongs to the set
 - (B) The infimum of a bounded set always belongs to the set
 - (C) Both supremum and infimum of a bounded set always belong to the set
 - (D) None of these
- 6. For a function $f: A \rightarrow B$, if the range of f is uncountable, then domain of f is:
 - (A) finite
 - (B) countable
 - (C) uncountable
 - (D) either countable or uncountable

7. Which of the following is not a Cauchy sequence?

(A)
$$\left\{\frac{(-1)^{n}}{n}\right\}$$

(B) $\left\{(-1)^{n}\right\}$
(C) $\left\{\frac{1}{n!}\right\}$
(D) $\left\{1-\frac{1}{2}+\frac{1}{3}-\frac{1}{4}+...+\frac{(-1)^{n}}{n}\right\}$

For the given statements, choose the correct statement (s) 11. If the series $\sum (2a_n - 1)$ is convergent, then the 8. $\lim_{n\to\infty} a_n = ?$ from the following : (A) 0 I. A monotonic increasing sequence which is not (B) 1/2 bounded above, diverges to infinity (C) 1 II. A monotonic decreasing sequence which is not (D) none of these bounded below, diverges to minus infinity 12. If $\sum a_n$ is a convergent series of positive terms, then (A) only I $\sum \frac{a_n}{1+a_n}$ is: (B) only II (C) both I & II (A) oscillatory (D) neither I nor II (B) divergent The sequence $\{S_n\}$, with $S_n = 1 + \frac{1}{2} + \frac{1}{3} + ... + \frac{1}{n}$; (C) convergent 9. (D) none of these (A) converges to some finite number 13. The $\lim_{n\to\infty} \frac{1^2 + 2^2 + ... + n^2}{n^3} = ?$ (B) diverges finitely (C) converges to 2 (A) $\frac{1}{3}$ (D) diverges to infinity (B) $\frac{2}{3}$ 10. For what value of a, the value of $\lim_{n\to\infty} 3\frac{n^{1/n}}{2} = a^{-1}$? (A) 0 (C) $\frac{1}{2}$ (B) 1 (D) None of these (C) $\frac{2}{3}$ 14. For the series with nth term $a_n = \frac{1}{n(n+1)}$, the sum (D) $\frac{3}{2}$ $\sum a_n = ?$ (A) 0 (B) 1 (C) 1/2 (D) Infinity

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of a function given by $f(\alpha) = \int_{a}^{b} f(x, \alpha) dx$, where a, b are constants?

(A)
$$f'(\alpha) = \frac{\partial}{\partial \alpha} \int_{a}^{b} f(x, \alpha) dx$$

(B) $f'(\alpha) = \frac{d}{d\alpha} \int_{a}^{b} f(\alpha) dx$
(C) $f'(\alpha) = \int_{a}^{b} \frac{\partial}{\partial \alpha} f(x, \alpha) dx$
(D) $f'(\alpha) = \int_{a}^{b} \frac{d}{d\alpha} f(x, \alpha) dx$

16. Given
$$f(a) = \int_{a}^{b} \frac{\sin ax}{x} dx$$
, then what is the value of $f'(a)$?

(A)
$$\frac{\sin 3a}{a}$$

(B)
$$\frac{3\sin a^3 - 2\sin a^2}{a}$$

(C) $\frac{3\sin a^2 - 2\sin^2 a}{a}$
(D) $\frac{3\sin a^3 - 3\sin^2 a}{6a}$

6a

- 17. The power series $\sum 3^{-n} (z-1)^{2n}$ converges if:
 - (A) |z|≤3
 - (B) $|z| < \sqrt{3}$
 - (C) $|z-1| < \sqrt{3}$
 - (D) $|z-1| \le \sqrt{3}$

- 15. Which of the following correctly defines Leibnitz rule 18. Which of the following is the radius of convergence of the series $\sum z^{n!}$?
 - (A) 0
 - (B) ∞
 - (C) 1
 - (D) a real number > 1
 - 19. If the number of generators in a cyclic group of infinite order is k, then k = ?
 - (A) 1
 - (B) 2
 - (C) finite
 - (D) infinite
 - 20. If α and β are the smallest positive integers which respectively denote the orders of non-cyclic and nonabelian groups, then
 - (A) $\alpha = 4$ and $\beta = 4$
 - (B) $\alpha = 4$ and $\beta = 6$
 - (C) $\alpha = 6$ and $\beta = 4$
 - (D) None of these
 - 21. The number of even permutations in a symmetric group
 - S₆ is:
 - (A) 3
 - (B) 6
 - (C) 360
 - (D) 720

- 22. Which of the following is not a group under 26. Which of the following is not a normal subgroup? multiplication? (Given $\omega^3 = 1, i^2 = -1$):
 - (A) $\left\{1, 5, \frac{1}{5}\right\}$
 - (B) $\{1, -1, i, -i\}$
 - (C) $\{1, \omega, \omega^2\}$
 - (D) Non-zero rational numbers
- 23. Which of the following is true for a group of prime order p?
 - I. It has no non-trivial subgroups
 - II. It is always cyclic as well as abelian
 - (A) Only I
 - (B) Only II
 - (C) Both I & II
 - (D) Neither I nor II
- 24. In the group of integer modulo 6, $\langle Z_6, + \rangle$, the inverse of an element $\overline{2} \in Z_6$ is :
 - (A) 1
 - (B) <u>2</u>
 - (C) <u>3</u>
 - (D) 4
- 25. The alternating group A_n is not simple for :
 - (A) n = 3
 - (B) n=4
 - (C) n = 5
 - (D) n≤5

- (A) Kernel of a homorphism (B) Alternating group in S_n (C) Centralizer of a group (D) Normalizer of an element in a group 27. Choose the correct statement(s): I. Every ideal is a subring II. The ring of complex numbers is a field (A) only I (B) only II (C) neither I nor II (D) both I & II 28. The polynomial $p(x) = a_0 + a_1x + ... + a_n x^n$; over a UFD is said to be primitive if the gcd of $a_0, a_1, a_2, ...,$ a_n is (Given $a_0, a_2, ..., a_n$ are integers) (A) 1 (B) 2 (C) 3 (D) 4 29. Given two ideals I and J of a ring R such that $I \subset J$, then union of I and J: (A) is an ideal (B) need not be an ideal
 - (C) is a maximal ideal of R
 - (D) is a prime ideal of R



30. For what value of k, $\frac{z}{\langle k \rangle}$ is a field?

- (A) k = 1
- (B) k = 2
- (C) k = 4
- (D) Any value of k
- 31. Given a differentiable function f(x) in a closed interval 35. [2, 7] with f(2) = 3 and $f'(x) \le 5$ for all values of x in (2, 7), the maximum possible value of f(x) at x = 7 is:
 - (A) 7
 - (B) 14
 - (C) 15
 - (D) 28
- 32. Let f(x) be continuous and differentiable function for all real's such that f(x+y) = f(x) - 3xy + f(y) and 36.

 $\lim_{h\to 0} \frac{f(h)}{h} = 7$, then the value of f'(x) is:

- (A) -3x + 7
- (B) 3x-7
- (C) 2f(x) + 7
- (D) 7

33. If $u = \log xy$ where $x^2 + y^2 = 1$, then $\frac{du}{dx} = ?$

(A) $\frac{1}{x}$ (B) $\frac{1}{x} + \frac{1}{y}$ (C) $\frac{1}{x} - \frac{x}{y}$

(D)
$$\frac{1}{x} - \frac{x}{y^2}$$

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- 34. The nth derivative of the function f(x) = xⁿ e^x at x = 0 is given by:
 - (A) $n! e^n$
 - (B) n!
 - (C) (n+1)!
 - (D) None of these

In a Cycloid, $x = a(\theta + \sin \theta)$ and $y = a(1 - \cos \theta)$, the angle ψ the tangent makes to the horizontal is :

- (A) 2θ
- (B) θ
- (C) $\frac{\theta}{2}$
- (D) $\frac{\theta}{3}$

For $r = ae^{\theta \cot \alpha}$, the tangent is inclined at—angle to the radius vector.

- (A) 0
- **(B)** π
- (C) $\frac{\pi}{2}$
- (D) a constant
- 37. The curvature of the function $f(x) = x^3 x + 1$ at x = 1 is given by :
 - (A) $\frac{6}{5}$ (B) $\frac{3}{5}$ (C) $\frac{6}{5^{\frac{3}{2}}}$ (D) $\frac{3}{5^{\frac{3}{2}}}$

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- tangents of the curves :
 - (A) Are real and coincident
 - (B) Have no real tangents
 - (C) Are real and distinct
 - (D) None of these
- 39. The value of k in Rolle's theorem for $f(x) = x^3 3x$ in the interval $[0, \sqrt{3}]$ holds :
 - (A) 1
 - (B) $\frac{1}{3}$

 - (C) -1
 - (D) $\frac{2}{3}$

40. If the Rolle's theorem holds for the function

- $f(x) = x^4 + ax^3 + bx$, in $-1 \le x \le 1$ and $f'\left(\frac{1}{2}\right) = 0$, then the value of ab = ?(A) -64 (B) -8 (C) - 4
- (D) -1

41. Using Cauchy's Mean value theorem for the functions $f(x) = e^x$, $g(x) = e^{-x}$ in the interval [2, 3], the value of cis:

- (A) 1.5
- (B) 2.5
- (C) 3
- (D) 3.5
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38. A double point on a curve is said to be node, if two 42. Given $f(x) = x^3 - 3x - 1$ is continuous in the closed interval $\left[\frac{13}{7}, -\frac{11}{7}\right]$ and f'(x) exists in the interval, $\left(\frac{13}{7}, -\frac{11}{7}\right)$ the value of k such that it lies in $\left(\frac{13}{7}, -\frac{11}{7}\right)$ is: (A) 0 (B) -1 (C) 1 (D) ± 1

43. The value of the integral $\int \frac{dx}{x(x+1)}$ is:

(A)
$$\ln \left| \frac{x+1}{x} \right| + c$$

(B) $\ln \left| \frac{x}{x+1} \right| + c$
(C) $\ln \left| \frac{x-1}{x} \right| + c$
(D) $\ln \left| \frac{x}{x+1} \right| + c$

44. The reduction formula for $\int \tan^n x \, dx$ is :

(A)
$$\frac{\tan^{n-1} x}{n-1} - \int \tan^{n-1} x \, dx$$

- (B) $\frac{\tan^{n-1}x}{n} \int \tan^{n-2}x \, dx$
- (C) $\frac{\tan^{n-1}x}{n-1} \int \tan^{n-2}x \, dx$
- (D) $\frac{\tan^{n-1}x}{n-1} + \int \tan^{n-2}x \, dx$

45. For what value of k, $\int \frac{dx}{x(x+2)} = k \ln \left| \frac{x}{x+2} \right| + c$? 49. The value of $\frac{1}{D^2 + a^2} \sin ax = ?$ (A) $-\frac{x}{2}\cos ax$ (A) 1 (B) -1 (B) $-\frac{x}{2a}\cos ax$ (C) 2 (C) $-\frac{x}{2a}\sin ax$ (D) $\frac{1}{2}$ 46. What is the value of $\int_0^{8\pi} |\sin x| dx$? (D) $\frac{x}{2a}\cos ax$ (A) 2 50. The solution y(x) of $(D^2 + 1) y = 0$ is : (B) 4 (A) $A\cos x - B\sin x$ (C) 8 (B) $Ae^{x} + Be^{-x}$ (C) $A\cos x + B\sin x$ (D) 16 (D) $-A\cos x + B\sin x$ 47. The particular integral of $(D^2-3D+2)y = e^{5x}$ is: 51. The solution of $p^2 - 9p + 18 = 0$ is given by : (A) e^{5x} (A) (y-x-a)(y+x-a)(B) $\frac{1}{30}e^{5x}$ (B) (y-3x-a)(y-6x-a)(C) (y+3x-a)(y-x+a)(C) $\frac{1}{12}e^{5x}$ (D) None of these (D) None of these 52. Which of the following is the solution of 48. The complementary function of $y_2 - 3y_1 + 2y =$ $\frac{dy}{dx} = y (\operatorname{cosec} x - \operatorname{cot} x)?$ cos 3x is: (A) $y = c \sec^2 \frac{x}{2}$ (A) $c_1 e^x + c_2 e^{2x}$ (B) $c_1 e^{-x} + c_2 e^{-2x}$ (B) $y = c \log \sin \frac{x}{2}$ (C) $c_1 e^{2x} + c_2 e^{-3x}$ (C) $y = c \log \frac{x}{2}$ (D) None of these (D) None of these

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- 53. The singular solution of $y = px + p p^2$ is:
 - $(A) \quad y = \frac{x+1}{2}$ (B) $y = \frac{x+1}{4}$

(C)
$$y = \left(\frac{x+1}{2}\right)^2$$

- (D) Does not exist
- 54. By means of a substitution $u = y^3$, the equation $y = 3xp + 6y^2p^2$ reduces to :

(A)
$$u = x \frac{du}{dx} + \frac{2}{3} \left(\frac{du}{dx} \right)^2$$

(B) $u = x \frac{du}{dx} + \frac{1}{3} \left(\frac{du}{dx} \right)^2$

(C)
$$u = x \frac{du}{dx} - \frac{2}{3} \left(\frac{du}{dx}\right)^2$$

- (D) None of these
- 55. For any positive integer n and a Bessel's function $J_n(x)$, choose the correct expression from the following:
 - (A) $J_{-n}(x) = (-1)^{n+1} J_n(x)$ (B) $J_{-n}(x) = (-1)^n J_n(x)$
 - (C) $J_{-n}(x) = -J_n(x)$
 - (D) $J_{-n}(x) = (-1)^n J_{n+1}(x)$

56. Which of the following determines a Bessel's differential equation?

(A)
$$x^{2}y_{2} + xy + (x^{2} - n^{2})y = 0$$

(B) $xy_{2} + y + xy = 0$
(C) $x^{2}y_{2} + xy + (x^{2} - 1)y = 0$

- (D) All of them
- 57. If $P_n(x)$ is the Legendre polynomial, then $P_0(x) +$

$$P_{1}(x) = ?$$

- (A) 1
- (B) x
- (C) 1 + x
- (D) None of these

The Wronskian of $y_1 = x^2$ and $y_2 = x^2 \log x$ is : 58.

(A) 0

(B) 1

(C) x

(D) x^{3}

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a(x + y) + b(x - y) + abt + c, the resulting partial

differential equation is :

(A)
$$z = \frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} + \frac{\partial z}{\partial t} + \left(\frac{\partial z}{\partial x}\right) \left(\frac{\partial z}{\partial y}\right) \left(\frac{\partial z}{\partial t}\right)$$

(B)
$$z = \frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} + \frac{\partial z}{\partial t} - \left(\frac{\partial z}{\partial x}\right) \left(\frac{\partial z}{\partial y}\right) \left(\frac{\partial z}{\partial t}\right)$$

(C)
$$\left(\frac{\partial z}{\partial x}\right)^2 - \left(\frac{\partial z}{\partial y}\right)^2 = 4\left(\frac{\partial z}{\partial t}\right)$$

(D) None of these

- 59. Be eliminating arbitrary constants a, b and c from z = 60. By eliminating arbitrary function from $z = f\left(\frac{y}{x}\right)$, the PDE is given by :
 - (A) px + qy = 0
 - (B) z = px + qy
 - (C) px qy = 0
 - (D) None of these

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| | ENTRANCE TEST-2023 | | | | | | | |
| | SCHOOL OF PHYSICAL & MATHEMATICAL SCIENCE | | | | | | | |
| | | | MATI | HEMATICS | | | | _ |
| Total (| Total Questions : 60 Question Booklet Series | | | | | | let Series 🛛 🗛 | |
| Time A | Allowed | : 70 Minu | tes | | Roll No. : | | | |
| | | | Instructio | ns for Candidates : | | | | |
| 1. | Write your E and fill up th | Entrance Test H ne necessary in | Roll Number in th formation in the | e space provided at spaces provided on | the top of th the OMR A | nis page o Answer S | of Question Book Sheet. | let |
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| 13. | Ensure that herself. | your OMR A | nswer Sheet has | been signed by the | e Invigilator | r and the | e candidate himse | elf/ |
| 14. | At the end of the original (| f the examinat DMR sheet in p | ion, hand over th presence of the Ca | e OMR Answer Shee ndidate and hand ove | et to the inv er the Candi | igilator v date's Co | who will first tear of opy to the candida | off te. |
| SM-29 | 575–A | | | $1 \\ \odot$ | | | [Turn ov | /er |

- 1. Let $A = \{x \in R : x < 1\}$ and $B = \{x \in R : -1 < x \le 3\}$. Then :
 - (A) Both A and B are bounded
 - (B) A is bounded above by 1 and its supremum $1 \in A$
 - (C) The supremum of A belongs to A and the infimum of B belongs to B
 - (D) The supremum of A does not belong to A and the supremum of B belongs to B
- 2. Which of the following is true ?
 - (A) The set of the real numbers is the neighbourhood of each of its points.
 - (B) The set Q of rational numbers is the neighbourhood of each of its points.
 - (C) The closed interval [a, b] is a neighbourhood of its end points a and b
 - (D) None of the above
- 3. What is the set of limit points for the set

$$\mathbf{S} = \left\{-1, \ 1, \ -\frac{1}{2}, \ \frac{3}{2}, \ -\frac{2}{3}, \ \frac{4}{3}, \ \dots\right\}$$

- $(A) \quad \left\{-\frac{1}{2}, \frac{3}{2}\right\}$
- (B) $\{-1, 1\}$
- (C) $\{0, -1\}$
- (D) None of the above
- 4. Which of the following is not true ?
 - (A) The set of all integers if countable.
 - (B) The set of all ordered pairs of integers is countable.
 - (C) The set of all real numbers is uncountable.
 - (D) The set of all rational numbers is uncountable.
- SM-29575-A

5. What is the limit point of the sequence $\{a_n\}$,

where
$$a_n = \frac{(-1)^{n-1}}{n!}, n \in N$$

(A)
$$-\frac{1}{2}$$

(B) -1

(C) 0

6.

(D) None of the above

If
$$a_n = n^2$$
 and $b_n = -n^2$, $n \in N$, then

- (A) the sequence $(a_n + b_n)$ diverges
- (B) the sequence $(a_n b_n)$ converges

(C) the sequence
$$\left\{\frac{a_n}{b_n}\right\}$$
 diverges
(D) the sequence $\left\{\frac{a_n}{b_n}\right\}$ converges

7.
$$\lim_{n \to \infty} \left(\frac{2n-3}{n+1} \right)$$
 equals

(A) 0

- (B) 1
- (C) 2
- (D) -3
- 8. Which of the following is not true ?
 - (A) If a sequence is convergent, it converges to a unique limit.
 - (B) Every convergent sequence is bounded.
 - (C) Every bounded sequence is convergent.
 - (D) Every bounded monotonic sequence is convergent.

- If the series $\sum_{n=1}^{\infty} a_n$ is convergent, then $\lim_{n \to 0} a_n$ 9.
 - equals :
 - (A) 0
 - **(B)** 1
 - (C) ∞
 - (D) None of the above
- 10. For any fixed value of n, the series $\sum_{n=1}^{\infty} \frac{\sin nx}{n^2}$ 14. is :
 - (A) absolutely convergent
 - (B) divergent
 - (C) oscillates finitely
 - (D) oscillates infinitely

11. If $\sum a_n$ is a positive term series such that

- (A) l < 1
- (B) 1 < l < 3
- (C) $l \ge 3$
- (D) None of the above

12. The series $A = \sum_{n=1}^{\infty} a_n$, where $a_n = \frac{(-1)^{n+1}}{\sqrt{n}}$. (D) None of the above 16. What is the identity element of the group of all $\frac{1}{\sqrt{n}} = a_1 + b_2 + 1$ Then

- (A) A is convergent
- (B) A is divergent
- (C) $\{a_n\}$ is monotonically increasing sequence
- (D) the series $|a_n|$ is convergent

13. The radius of convergence and the exact interval of convergence of the power series

$$\sum \frac{(n+1)x^{n}}{(n+2)(n+3)}$$
 is :
(A) R = 0, [0, 1]
(B) R = 1, [-1, 1]
(C) R = ∞
(D) None of the above
Let {f_n} be a sequence

of functions such that $\lim_{n\to\infty} f_n = f(x), x \in [a,b]$, and let

 $M_n = \sup_{x \in [a, b]} |f_n(x) - f(x)|. \text{ Then } f_n \rightarrow f$ uniformly on [a, b] if and only if :

- (A) $M_n \rightarrow 0$ as $n \rightarrow \infty$ (B) $M_n \rightarrow \infty$ as $n \rightarrow \infty$
- (C) $M_n \rightarrow 1$ as $n \rightarrow \infty$
- (D) None of the above

 $\lim_{n \to \infty} (a_n)^{\frac{1}{n}} = l$, then the series is convergent if: 15. Let $\{f_n\}$ be a sequence, where $f_n(x) = \frac{nx}{1 + n^2 x^2}$, then

- (A) $M_n \rightarrow 0$ as $n \rightarrow \infty$ (B) $M_n \rightarrow \frac{1}{2}$ as $n \rightarrow \infty$
- (C) $M_n \rightarrow 1$ as $n \rightarrow \infty$
- integers Z with operation aob = a + b + 1, a, $b \in Z$.
 - (A) 0
 - (B) 1
 - (C) -1
 - (D) None of the above

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- 17. The set of all $n \times n$ non-singular matrices 21. Let $G = \{a\}$ be a cyclic group of order six having their elements as rational numbers is :
 - (A) an infinite abelian group wrt matrix multiplication
 - (B) an abelian group wrt matrix addition
 - (C) an infinite non-abelian group wrt matrix multiplication
 - (D) None of the above
- 18. If $\alpha = (1 \ 2 \ 3 \ 4 \ 5)$ and $\beta = (2 \ 3) \ (4 \ 5)$ be two permutations of five symbols 1, 2, 3, 4, 5 then ²². $\alpha\beta$ equals :
 - (A) (1 3 5)
 - (B) (2 4 5)
 - (C) (1 2 3)
 - (D) None of the above
- 19. Which of the following is the set of generators of the cyclic group $G = (\{0, 1, 2, 3, 4, 5\}, +6)$ are :
 - (A) $\{1, 2\}$
 - (B) $\{1, 5\}$
 - (C) $\{2, 5\}$
 - (D) None of the above
- 20. Which of the following is true ?
 - (A) The symmetric group P_3 of permutations of degree three is non-abelian, while its subgroup A_3 is abelian
 - (B) The symmetric group P_4 of permutations of degree four is abelian, while its subgroup A_4 is also abelian
 - (C) The symmetric group P_3 of permutations of degree three is non-abelian, while its subgroup A_3 is also non-abelian
 - (D) None of the above
- SM-29575-A

- and H be the subgroup generated by a^2 . Then the order of the quotient group (G/H) is :
- (A) 1
- (B) 2
- (C) 3
- (D) 4
- Which of the following is true for the group of order 45 ?
 - (A) G has a normal subgroup of order 9
 - (B) G has an element of order 9
 - (C) G is a non-abelian group
 - (D) G has no proper subgroup of order 5
- 23. What is the order of the element $\frac{2}{3} + z$ in the quotient group (G/Z) of the additive group of rationals ?
 - (A) 2
 - (B) 3
 - (C) 5
 - (D) 6
- 24. If the quotient group (G/Z), where Z is the centre of the group G, then
 - (A) G is abelian
 - (B) G is cyclic
 - (C) G is non-abelian
 - (D) None of the above
- 4 0

- 25. The set $F = \{0, 1, 2, 3, 4, 5, 6\}$ under addition 29. What is the locus of the extremity of the polar and multiplication modulo 7 forms :
 - (A) Commutative ring with zero divisors
 - (B) Non-commutative ring with unity
 - (C) Field
 - (D) None of the above
- 26. Let R[x] be the ring of polynomials of a ring R, then which of the following statements is/are true ?
 - (i) R is an integral domain if and only if R[x] is an integral domain.
 - (ii) If R is an integral domain, then deg [f(x) g(x)] = deg f(x) + deg g(x),where f(x), $g(x) \in R[x]$.
 - (A) (i) only
 - (B) (ii) only
 - (C) Neither (i) nor (ii)
 - (D) Both (i) and (ii)
- 27. What is the number of proper ideals in a 31. field F?
 - (A) At least one
 - (B) Zero
 - (C) Exactly one
 - (D) None of the above

28. $\lim_{n\to\infty} \left(a^{\frac{1}{n}}-1\right)n$ equals :

- (A) log a
- (B) 1
- (C) ∞
- (D) None of the above

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subnormal of the curve $r = f(\theta)$?

(A)
$$\frac{\mathrm{dr}}{\mathrm{d}\theta}$$

(A) $\frac{\pi}{2}$

(B) 0

(C) -1

(D) π

(B) $\theta - \frac{\pi}{2}$ (C) $r = f'\left(\theta - \frac{\pi}{2}\right)$

- (D) None of the above
- 30. What is the angle of intersection of the curves $r = a(1 + \cos \theta), r = b(1 - \cos \theta)$?

- What is the radius of curvature at any point of the curve $r = ae^{\theta \cot \alpha}$?
 - (A) r $cosec \alpha$
 - (B) $r \cot \alpha$
 - (C) r sec α
 - (D) None of the above
 - 32. The asymptotes of the curve $r\theta = a$ are :
 - (A) $r \sin\theta = a$
 - (B) $r \cos\theta = a$
 - (C) $\cos\theta = r^2$

5 0

(D) None of the above

| 33 | If $U = \sqrt{x^2 - y^2} \sin^{-1} \frac{y}{2}$ then $x \frac{\partial U}{\partial x} + y \frac{\partial U}{\partial x}$ | <u>U</u> 37. | Let the functions $f(x)$ as | | |
|-----|--|--------------|---|--|--|
| 55. | equals : | У | $f(x) = \begin{cases} 1, & \text{if } x \ge 0\\ 0, & \text{if } x < 0 \end{cases}$ | | |
| | (A) 2U | | $\begin{bmatrix} 0 & \text{if } x > 0 \end{bmatrix}$ | | |
| | (B) 0 | | $g(x) = \begin{cases} 0, & \text{if } x = 0 \\ 1, & \text{if } x < 0 \end{cases}$ | | |
| | (C) U | | Then | | |
| | (D) None of the above | | (A) $f(x)$ is continuous | | |
| | | | (B) $g(x)$ is continuous | | |
| 34. | If Z = x ^y , then $\frac{\partial Z}{\partial x}$ equals : | | (C) $f(x) + g(x)$ is cont | | |
| | OX | | (D) $f(x)g(x)$ is discontinued as $f(x)g(x) = \frac{1}{2} \int_{-\infty}^{\infty} \frac{1}$ | | |
| | (A) $x^y \log x$ | 38. | If $x = a \cos \theta$ and $y = 1$ | | |
| | (B) y x^{y-1} | | of $\frac{d^2y}{dx^2}$ at $\theta = \frac{\pi}{2}$ is : | | |
| | (C) $y e^x$ | | h | | |
| | | | | | |

- (D) None of the above
- 35. What is the nth-derivative of 3^{2x} ?

(A)
$$y_n = 3^{2x} (\log 3)^n$$

- (B) $y_n = 2(3^{2x})^n (\log 3)$
- (C) $y_n = 2^n 3^{2x} (\log 3)^n$
- (D) None of the above

36. $\frac{d}{dx}(\sin\sqrt{x})$ equals :

(A) $\cos \sqrt{x}$

(B) $\frac{1}{2\sqrt{x}}\cos\sqrt{x}$

(C)
$$\frac{\sqrt{x}}{2}\cos\sqrt{x}$$

(D) None of the above

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 ∂U 37. Let the functions f(x) and g(x) be defined by :

- at x = 0
- at x = 0
- inuous at x = 0
- inuous at x = 0

38. If
$$x = a \cos \theta$$
 and $y = b \sin \theta$, then the value

$$(A) -\frac{b}{a^2}$$

(B) ab

(C)
$$-\frac{b}{a}$$

- (D) None of the above
- 39. What is the value of the function $f(x) = x^2 e^x$? (A) $4e^{-2}$
 - (B) 0
 - (C) -4
 - (D) None of the above
- 40. Rolle's theorem cannot be applied to the function f(x) = |x| in [-1, 1] because :
 - (A) the function is discontinuous at x = 0
 - (B) the function is not derivable at x = 0
 - (C) the function is discontinuous at $x = \frac{1}{2}$
 - (D) the function is not derivable at $x = -\frac{1}{2}$

41. The coefficient of x in the Maclaurin's series of f(x) = a^x is :
(A) 1

- (B) log a (P) (C) a (B)
- (D) $(\log a)^2$
- 42. $\int \frac{1}{x x^{3}} dx \text{ equals} :$ (A) $\log \sqrt{1 - x^{2}}$ (B) $\log x - \log \sqrt{1 - x^{2}}$ (C) $\log x - \log(1 - x^{2})$ (D) $\log x + \log \sqrt{1 - x^{2}}$ 43. $\int_{1}^{2} \log x \, dx \text{ equals} :$ (A) $\log 4 - 1$ (B) 2 $\log 2$ (C) 2 $\log 2 + 1$
 - (D) None of the above

44. The reduction formula of $I_n = \int tan^n x \, dx$ is

- (A) $I_n = \frac{\tan^{n-1} x}{n-1} I_{n-2}$ (B) $I_n = \frac{\tan^{n-2} x}{n-2} - I_{n-1}$ (C) $I_n = \frac{2\tan^n x}{n} - I_{n+3}$
- (D) None of the above
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- 45. For odd n, $\int_{0}^{\pi} \frac{\sin nx}{\sin x} dx$ equals : (A) 0 (B) $-\pi$ (C) π
 - (D) None of the above
- 46. What is the general solution of the differential equation

$$\frac{dy}{dx} = e^{x-y} + x^2 e^{-y} ?$$
(A) $y = \frac{x^3}{3} + e^x + c$
(B) $e^y = \frac{x^3}{3} + e^x + c$
(C) $y = e^x + e^{-y} + c$
(D) None of the above

47. What is the particular integral of the differential equation

?

$$(D^{2} - 3D + 2)y = e^{x} + e^{2x}$$
(A) $\frac{e^{x}}{5} + \frac{xe^{2x}}{6}$
(B) $-xe^{x} + \frac{xe^{2x}}{4} + c$
(C) $xe^{2x} - xe^{x}$

(D) None of the above

48. What is the complementary function of the 52. For a first order non-linear differential equation differential equation dv

$$(D^{4} - D^{2})y = 2 ?$$
(A) $c_{1}e^{x} + c_{2}e^{-x}$
(B) $c_{1} + c_{2}x + c_{3}e^{x}$
(C) $c_{1} + c_{2}x + c_{3}e^{x} + c_{4}e^{-x}$

- (D) None of the above
- 49. What is the general solution of the differential equation

$$x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 4y = 0 \quad ?$$

(A)
$$y = (c_1 + c_2 \log x)x^2$$

(B)
$$y = (c_1 e^x + c_2 e^{-x})x$$

(C)
$$y = (c_1 + c_2 \log x)$$

- (D) None of the above
- 50. What is the singular solution of the differential

equation $y = px + \frac{a}{p}$, where $p = \frac{dy}{dx}$? (A) $y^2 = 4ax$ (B) $y = 4ax^2$ (C) y = 4ax(D) None of the above 51. What is the general solution of the differential 54.

equation
$$(px - y)^2 = p^2 + m^2$$
, where $p = \frac{dy}{dx}$.

- (A) $y = cx \pm \sqrt{m^2 + c^2}$ (B) $y = \sqrt{cx - m}$ (C) $y = \sqrt{m^2 - 4ac}$
- (D) None of the above

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 $f\left(x, y, \frac{dy}{dx}\right) = 0$, which of the following

statements is/are true ?

- (i) Its general solution must contain only one arbitrary constant.
- (ii) Its singular solution can be obtained by substituting particular values of the arbitrary constant in its general solution.
- (iii) Its singular solution is an envelope of its general solution which also satisfies the equation.
- (A) (i), (ii) and (iii)
- (B) (i) and (ii)
- (C) (i) and (iii)
- (D) (ii) and (iii)
- 53. Which of the following is a non-linear differential equation ?

(A)
$$\frac{d^2y}{dx^2} + 3\frac{dy}{dx} = e^x$$

(B)
$$\frac{dy}{dx} + 3y = e^x$$

(C)
$$\left(\frac{dy}{dx}\right)^2 + 5y = 0$$

(D) None of the above

Let
$$I = \int_{-1}^{1} P_m(x) P_n(x) dx$$
, where $P_m(x)$ and $P_n(x)$

are Legendre polynomials, then

(A) I = 0, if $m \neq n$

(B)
$$I = 0$$
, if $m = n$

(C) I = $\frac{2}{2n+1}$, if m \neq n

(D) I =
$$\frac{2}{2n+1}$$
, if m > n

55. For nth Legendre polynomial $C_n \left[\frac{d^n (x^2 - 1)^n}{dx^n} \right]$,

the value of C_n is :

(A)
$$\frac{1}{n! 2^{n}}$$

(B) $\frac{n!}{2^{n}}$

- (C) n! 2ⁿ
- (D) None of the above
- 56. Which of the following is the Bessel's equation ?

(A)
$$z^{2}\left(\frac{d^{2}w}{dz^{2}}\right) + z\left(\frac{dw}{dz}\right) + (z^{2} + n^{2})w = 0$$

(B) $z^{2}\left(\frac{d^{2}w}{dz^{2}}\right) - z\left(\frac{dw}{dz}\right) + (z^{2} - n^{2})w = 0$
(C) $z^{2}\left(\frac{d^{2}w}{dz^{2}}\right) + z\left(\frac{dw}{dz}\right) + (z^{2} - n^{2})w = 0$

- (D) None of the above
- 57. What is the Wronskian of x and xe^2 ?
 - (A) 0
 - (B) $x x^2 e^x$
 - (C) x^2e^x
 - (D) None of the above

- 58. The partial differential equation obtained from $z = f(x) + e^{y}g(x)$ by eliminating the arbitrary functions is :
 - (A) p = q
 - (B) t = q
 - (C) r = s
 - (D) None of the above
- 59. What is the general solution of the partial differential equation $p 2q = 3x^2 \sin(y + 2x)$?
 - (A) $x^{3}sin(y + 2x) z = \phi(y + 2x)$
 - (B) $\sin(y + 2x) = z$
 - (C) $\phi(y 2x) = \cos(y + 2x)$
 - (D) None of the above
- 60. The partial differential equation

$$xy\frac{\partial^2 u}{\partial x^2} - (x^2 - y^2)\left(\frac{\partial^2 u}{\partial x \partial y}\right) - xy\left(\frac{\partial^2 u}{\partial y^2}\right) + y\frac{\partial u}{\partial x}$$
$$-x\frac{\partial u}{\partial y} = 2(x^2 - y^2)$$

- (A) is parabolic at all points
- (B) is hyperbolic at all points
- (C) is elliptic at all points
- (D) None of the above

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ROUGH WORK

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ROUGH WORK

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| | | ENTR | ANCE TEST-2022 |
| | | SCHOOL OF PHYS | ICAL & MATHEMATICAL SCIENCES |
| | | | MATHEMATICS |
| To | tal (| Duestions · 60 | Question Booklet Series A |
| Tir | me A | Allowed : 70 Minutes | Roll No. : |
| | | | |
| | 1 | Write your Entropee Test Dell Nu | nstructions for Candidates : |
| | 1. | and fill up the necessary informat | tion in the space provided at the top of this page of Question Bookle |
| 1.1.2.4 | 2. | OMR Answer Sheet has an Orig making entries in the Original Co so that the entries made in the O Copy. | inal Copy and a Candidate's Copy glued beneath it at the top. While opy, candidate should ensure that the two copies are aligned properly riginal Copy against each item are exactly copied in the Candidate' |
| | 3. | All entries in the OMR Answer SI Copy only. | heet, including answers to questions, are to be recorded in the Origina |
| | 4. | Choose the correct / most appropriat darken the circle of the appropriat read by the OMR Scanner and no | riate response for each question among the options A, B, C and D and e response completely. The incomplete darkened circle is not correctly complaint to this effect shall be entertained. |
| | 5. | Use only blue/black ball point per gel/ink pen or pencil should be us | n to darken the circle of correct/most appropriate response. In no case sed. |
| | 6. | Do not darken more than one circl response shall be considered wro | le of options for any question. A question with more than one darkened ong. |
| | 7. | There will be 'Negative Markin of 0.25 marks from the total score | g' for wrong answers. Each wrong answer will lead to the deduction of the candidate. |
| | 8. | Only those candidates who would for admission. | d obtain positive score in Entrance Test Examination shall be eligible |
| | 9. | Do not make any stray mark on th | e OMR sheet. |
| | 10. | Calculators and mobiles shall not | be permitted inside the examination hall. |
| | 11. | Rough work, if any, should be don | ne on the blank sheets provided with the question booklet. |
| | 12. | OMR Answer Sheet must be hand will not be evaluated. | lled carefully and it should not be folded or mutilated in which case i |
| | 13. | Ensure that your OMR Answer Sherself. | Sheet has been signed by the Invigilator and the candidate himself |
| | 14. | At the end of the examination, har the original OMR sheet in presence | nd over the OMR Answer Sheet to the invigilator who will first tear of e of the Candidate and hand over the Candidate's Copy to the candidate |
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SEAL

1.
$$\lim_{x\to 0} \frac{e^{\sin x} - 1}{x} \text{ equals :}$$
(A) 0
(B) -1
(C) e
(D) 1
2. Let $f(x) = \begin{cases} 1, & x \ge 0 \\ -1, & x < 0, \\ g(x) = \begin{cases} -1, & x \ge 0 \\ 1, & x < 0. \end{cases}$
(A) f and g are continuous
(B) fg is discontinuous
(C) f + g is continuous
(D) None of the above
3. If $z = x^4y^2 \sin^{-1}\left(\frac{y}{x}\right)$, then $x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y}$ equals : 7.
(A) 6z
(B) 3z

- (C) 9z
- (D) 6
- 4. Let $z = x^2 3y^2 + 20$, where x = 2 cost and

y = 2 sint. At
$$t = \frac{\pi}{4}$$
, $\frac{dz}{dt}$ equals :

- (A) 16
- (B) -16
- (C) -8 (D) 8

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- 5. What is the radius of curvature of the curve s = a secψ tanψ + a log (secψ + tanψ) at the point (s, ψ) ?
 - (A) 2a $\sec^3\psi$
 - (B) a $\sec^3\psi$
 - (C) 2 $\sec^3\psi$
 - (D) None of the above
- 6. What is the angle between the radius vector and the tangent to the curve $r = a(1 + \sin\theta)$ at
 - $\theta = \frac{\pi}{6} ?$ (A) $\frac{\pi}{6}$ (B) $\frac{\pi}{2}$ (C) $\frac{\pi}{4}$

(D) None of the above

What is the pedal equation of the curve $a^2 = r^2 \cos 2\theta$?

- (A) $a^2 = rp$
- (B) a = rp
- (C) a = r + p
- (D) None of the above

What is the number of asymptotes of the curve

- $r = \frac{a}{1 \cos \theta}$? (A) 2 (B) 1 (C) 0
- (D) None of the above
- 2.

8.

9.

On which of the following functions Rolle's theorem cannot be applied ? 13.

- (A) $f(x) = \sin x$ in $[0, \pi]$
- (B) $f(x) = \sqrt{4-x^2}$ in [-2, 2]
- (C) f(x) = |x| in [-1, 1]
- (D) $f(x) = x^2$ in [-1, 1]
- 10. In which of the following intervals, all the ¹⁴ conditions of the Lagrange's mean value theorem is satisfied ?
 - (A) [2, 4]
 - (B) [1, 3]
 - (C) [-2, 2]
 - (D) None of the above
- 11. $\lim_{x \to 0} \left(\frac{\ln(1+x)}{\sin x} \right)$ equals :

(A) -1

- (B) 1
- (C) 0
- (D) None of the above
- 12. What is the maximum value of the function $f(x) = 2x^3 9x^2 24x 20$?
 - (A) 1
 - (B) 7
 - (C) -7
 - (D) None of the above
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13. $\int \frac{dx}{\sqrt{2x - x^2}} \text{ equals :}$ (A) $\cos^{-1}(x - 1)$ (B) $\sin^{-1}(x - 1)$ (C) $\sin(x - 1)$ (D) $\cos(x - 1)$

14. $\int \frac{e^x}{(e^x - 1)(e^x + 2)} dx$ equals :

(A) $\ln \left| \frac{e^{x} + 1}{e^{x} + 2} \right|^{\frac{1}{3}}$

- (B) $\ln \left| \frac{e^{x} 1}{e^{x} + 2} \right|^{\frac{1}{3}}$
- (C) $\ln \left| \frac{e^{x} 1}{e^{x} 2} \right|^{\frac{1}{3}}$
- (D) None of the above
- 15. $\frac{d}{dx} \int_{0}^{\cos x} (t^4 + 6) dt \text{ equals }:$ (A) $-x(\cos^4 x + 6) \sin x$ (B) $-x(\cos^4 x + 6) \cos x$ (C) $-(\cos^4 x + 6) \cos x$ (D) None of the above
 16. The differential equation $(ay^2 + x + x^8)dx$
 - $+ (y^8 y + bxy)dy = 0$ is exact if :
 - (A) b = a
 - (B) a = 1 and b = 3
 - (C) a = 3 and b = 1
 - (D) b = 2a
- 3

17. What is the integrating factor for the differential 20. What is the general solution of the different equation equation

$$(x+1)\frac{dy}{dx} - y = e^{3x}(x+1)^2$$
 ?

- (A) $\frac{1}{1+x^2}$ (B) $\frac{1}{1+x}$ (C) $\frac{1}{1-x}$
- (D) 1 + x
- 18. What is the particular integral for the differential equation

 $(D + 2)(D - 1)^{3}y = (e^{x} + 1)$?

- (A) $\frac{1}{18}x^3e^x \frac{1}{2}$
- (B) $18x^3e^x 2$
- (C) $\frac{1}{18}x^2e^x \frac{1}{2}$
- (D) None of the above
- 19. What is the general solution of the differential equation

 $(D^2 + 1)y = \cos 2x + e^{-x}$?

- (A) $c_1 \cos x + c_2 \sin x \frac{1}{3} \cos 3x + \frac{1}{2} e^{-x}$
- (B) $(c_1 + c_2 x)e^x + \frac{1}{3}\cos x + \frac{1}{2}e^{-x}$
- (C) $c_1 \cos x + c_2 \sin x \frac{1}{3} \cos 2x + \frac{1}{2} e^{-x}$
- (D) None of the above

$$\left(\frac{dy}{dx}\right)^2 - 7\left(\frac{dy}{dx}\right) + 12 = 0$$
?
(A) $(y - 3x - c) (y - 4x - c) = 0$
(B) $(y + 3x - c) (y - 4x - c) = 0$
(C) $(y - 3x - c) (y + 4x - c) = 0$
(D) None of the above
. What is the general solution of the difference equation $p = \log(px - y)$, where $p = \frac{dy}{dx}$

$$(A) y = cx - e^x$$

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(B)
$$y = cx - e^{c}$$

(C)
$$y = c - e^x$$

- (D) None of the above
- 22. If α is the degree and β is the order of differential equation

$$\left(\frac{d^2y}{dx^2}\right)^{\frac{1}{3}} = \left(y + \frac{dy}{dx}\right)^{\frac{1}{2}}$$

Then $3\alpha + 5\beta$ equals :

(B) 18

- (C) 28
- (D) None of the above

23. The differential equation $(y - px)^2 = a^2(1 + b^2)^2$

- where $p = \frac{dy}{dx}$, is :
- (A) Linear equation
- (B) Lagrange's equation
- (C) Clairaut's equation
- (D) None of the above

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24. What is the expansion of x^2 in terms of the 27. What is the partial differential equation obtained Legendre polynomial ?

(A)
$$\frac{1}{2}[2p_2(x) + p_0(x)]$$

(B) $\frac{1}{3}[2p_2(x) + 3p_0(x)]$
(C) $\frac{1}{3}[2p_2(x) + p_0(x)]$

(D) None of the above

25. If $J_n(x)$ is the Bessel function, then $J_{-\frac{1}{2}}(x)$ equals : 28. What is the general solution of the partial

(A)
$$\frac{2}{\pi x}$$

(B) $\frac{\pi x}{2}$

(C)
$$\sqrt{\frac{2}{\pi x}} \sin x$$

- (D) None of the above
- 26. What is the general solution of the Bessel's differential equation

$$x^{2}\left(\frac{d^{2}y}{dx^{2}}\right) + x\left(\frac{dy}{dx}\right) + \left(x^{2} - \frac{9}{16}\right)y = 0.$$

(A)
$$y = AJ_{\frac{9}{16}}(x) + BJ_{-\frac{9}{16}}(x)$$

(B)
$$y = AJ_{\frac{3}{4}}(x) + BJ_{-\frac{3}{4}}(x)$$

(C)
$$y = AJ_{\frac{4}{3}}(x) + BJ_{-\frac{4}{3}}(x)$$

(D) None of the above

from $z = f(x^2 - y^2)$ by eliminating the arbitrary function ?

(A)
$$y \frac{\partial z}{\partial x} = x \frac{\partial z}{\partial y}$$

(B) $x \frac{\partial z}{\partial x} = y \frac{\partial z}{\partial y}$
(C) $y \frac{\partial z}{\partial x} = z \frac{\partial z}{\partial y}$

(D) None of the above

differential equation
$$\frac{\partial z}{\partial x} + \frac{\partial z}{\partial y} = \sin x$$

- (A) $\phi(x y, z + \cos x) = 0$
- (B) $\phi(xy, z + \cos x) = 0$
- (C) $\phi(x y, z + \sin x) = 0$
- (D) $\phi(x y, z \cos x) = 0$
- 29. What is the complete integral of the partial differential equation $z = px + qy - 2\sqrt{pq}$.

(A)
$$z = (ax + by)^2 - 2\sqrt{ab}$$

- (B) $z = axy 2\sqrt{ab}$
- (C) $z = ax + by 2\sqrt{ab}$
- (D) None of the above
- 30. At all points, the partial differential equation

$$\frac{\partial^2 u}{\partial x^2} + 4 \left(\frac{\partial^2 u}{\partial x \partial y} \right) + 4 \left(\frac{\partial^2 u}{\partial y^2} \right) = 0$$

- (A) is hyperbolic
- (B) is elliptic

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- (C) is parabolic
- (D) None of the above

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(A) Both (1) and (2) are true (B) Only (1) is true (C) Only (2) is true (D) Neither (1) is true nor (2) is true (A) set of rational numbers (B) set of irrational numbers (C) set of integers (D) set of real numbers (A) 1 (B) 2 (C) infinite (D) None of the above (A) set of all integers coefficients (C) set $\{1, 4, 9, 16, \dots\}$

32. Which of the following is order complete ?

(1) The set $\left\{-1, -\frac{1}{2}, -\frac{1}{3}, -\frac{1}{4}, \dots\right\}$ is bounded.

(2) The set $\left\{\frac{1}{3}, \frac{4}{5}, \frac{9}{7}, \frac{16}{9}, \dots\right\}$ is bounded.

33. What is number of limit points in a finite set ?

- 34. Which of the following is uncountable ?
 - (B) set P_n of all polynomial functions with integer
 - (D) set of all real numbers

- 31. Which of the following statements is/are true? 35. What is the number of limit points of the sequen $\{1, 2, 1, 4, 1, 6, 1, \dots\}$?
 - (A) one
 - (B) more than one but finite
 - (C) infinite
 - (D) 0

36. The sequence $\left\{1+\frac{1}{n}\right\}$

- (A) converges to zero
- (B) converges to 1
- (C) converges to 2
- (D) diverges to infinity

37. If $\lim_{n \to \infty} a_n = 9$, then $\lim_{n \to \infty} \left(\frac{(a_1 + a_2 + \dots + a_n)}{n} \right)$ equals :

- (A) 0
- (B) 3
- (C) 9
- (D) None of the above
- 38. Which of the following is NOT true ?
 - (A) A necessary and sufficient condition the convergence of a monotonic seque is that it is bounded.
 - (B) Every monotonic decreasing sequence where the sequence where th is bounded below diverges.
 - (C) Every monotonic increasing sequence wh is not bounded above diverges.
 - (D) A monotonic increasing bounded ab sequence converges.

- 39. The series $\frac{1.2}{3^2.4^2} + \frac{3.4}{5^2.6^2} + \frac{5.6}{7^2.8^2} + \dots$
 - (A) oscillates finitely
 - (B) oscillates infinitely
 - (C) is divergent
 - (D) is convergent
- 40. Which of the following statements is true ?
 - (1) the infinite series $\sum_{n=1}^{\infty} \frac{1}{n^{1+\frac{1}{n}}}$ is divergent
 - (2) the infinite series $\sum \frac{1}{n^{2+\frac{1}{n}}}$ is convergent
 - (A) Both (1) and (2) are true
 - (B) Only (1) is true
 - (C) Only (2) is true

(D) Neither (1) is true nor (2) is true

- 41. Which of the following statements is true ?
 - (1) The infinite series $1 \frac{1}{2} + \frac{1}{3} \frac{1}{4} + \dots$ is conditionally convergent
 - (2) The infinite series $1 \frac{1}{2^3} + \frac{1}{3^3} \frac{1}{4^3} + \dots$ is absolutely convergent
 - (A) Both (1) and (2) are true
 - (B) Only (1) is true
 - (C) Only (2) is true
 - (D) Neither (1) is true nor (2) is true

42. If $\sum U_n$ is a positive term series such that $\lim_{n \to \infty} (U_n)^{\frac{1}{n}} = t$, then the series converges if (A) t = 1(B) t > 1(C) t < 1(D) t = 2

43. Which of the following statements is/are true for the sequence $F_n(x) = x^n$ on [0, 1] ?

- (1) Uniformly convergent
- (2) Pointwise convergent
- (A) Both (1) and (2)
- (B) Only (1)
- (C) Only (2)
- (D) Neither (1) nor (2)
- 44. If a sequence $\{f_n\}$ converges uniformly in [a, b]and x_0 is a point of [a, b] such that $\lim_{x \to x_0} f_n(x) = a_n$,
 - $n = 1, 2, 3, \dots, then$:
 - (A) $\{a_n\}$ diverges
 - (B) $\{a_n\}$ converges

(C)
$$\lim_{x \to x_0} f(x) \neq \lim_{n \to \infty} a_n$$

(D) $\lim_{x \to x_0} f(x) \neq a_n$

 If R is the radius of convergence and β is the exact interval of convergence of the power series

3)

5)

3)

$$\sum \frac{(x-1)^n}{2^n}$$
, then :
(A) R = 2 and $\beta = (-1, \beta)$
(B) R = 4 and $\beta = (-1, \beta)$
(C) R = ∞ and $\beta = (-1, \beta)$

(D) None of the above

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46. Which of the following forms a group? (A) $\{1, 2, 3\}$ under multiplication modulo 4 (B) $\{1, -1, i, -i\}$ under addition (C) $\{0, 1, 2, 3\}$ under multiplication modulo 4 (D) $\{1, 2, 3, 4\}$ multiplication modulo 5 47. In the group GL(2, Z_{11}), the inverse of $\begin{pmatrix} 2 & 6 \\ 5 & 5 \end{pmatrix}$ (D) G has a unique proper subgroup 51. What is the number of proper subgroups of a is $\begin{pmatrix} k & k \\ k+1 & k-1 \end{pmatrix}$, then 5k + 3 equals : (A) One (B) Two (A) 45 (C) Four (B) 46 (D) Six (C) 47 (D) None of the above 48. In the multiplicative group $\{1, -1, i, -i\}$, if x is the inverse of -1 and y is the inverse of i, then (A) 4 xy equals : (B) 5 (A) i (C) 6 (B) -i (C) 1 (D) -1 49. For an abelian group G with a, $b \in G$ and n a subgroups is itself a normal subgroup. non-negative integer, which of the following statements is/are true ? (1) $(ab)^n = a^n b^n$ (2) $(ab)^{-1} = a^{-1}b^{-1}$ (A) Both (1) and (2) (B) Only (1) (C) Only (2) (C) Only (2) (D) Neither (1) nor (2)

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50. Which of the following is NOT true for a group G of order 7 ? (A) G is cyclic (B) G is abelian (C) G has no proper subgroups (D) G has a unique proper subgroup finite cyclic group of order 12? 52. What is the order of element 3 in the group $(\{0, 1, 2, 3, 4\}, +5)$? (D) None of the above 53. Which of the following statements is/are true?

- (1) The intersection of any collection of normal
 - (2) If H and K are subgroups of an abelian group G, then HK is a subgroup of G.
 - (A) Both (1) and (2)
 - (B) Only (1)

8

(D) Neither (1) nor (2)

9

- 6. The set M of all nxn matrices with their elements as real numbers is a :
 - (A) Commutative ring with unity
 - (B) Non-commutative ring with unity
 - (C) Non-commutative ring without unity
 - (D) Ring without zero divisors
- abelian.
- order 3.
- (D) The symmetric group P_3 of degree 3 is 60.
- 3 and A_3 is the alternating group of
- where P_3 is the symmetric group of degree
- abelian. (B) A quotient group of a cyclic group is cyclic. (C) The quotient group P_3/A_3 is an abelian group,
- (C) Both (1) and (2) 55. Which one of the following is NOT true ?
- (B) Only (2)

(1) A subgroup H of index 2 in a group G is

(2) If H and N are subgroups of a group G,

with N normal in G, then $H \cap N$ is normal in G.

a normal subgroup of G.

- (A) Only (1)

- (D) Neither (1) nor (2)
- - - Which of the following is NOT order of a finite field ?
 - (A) 81
 - (B) 125
 - (C) 32
 - (D) 36

Which of the following statements is/are true ?

- (1) A ring has more than one unity.
- (2) A unit of a ring divides every element of the ring.
- (A) Both (1) and (2)
- (B) Only (1)
- (C) Only (2)
- (D) Neither (1) nor (2)

- (A) A field
- (B) An integral domain
- (C) A division ring
- (D) None of the above
- 58. The ring of all 2×2 matrices over rationals is :
 - (A) An integral domain
 - (B) A commutative ring
 - (C) A field
 - (D) None of the above
- (A) A quotient group of an abelian group is 59.

54. Which of the following statements is/are true ? 57. The ring of integers is :

| $ \begin{tabular}{ c c c c c } \hline \end{tabular} \end{tabular}$ | | | | | | Sr. No | | |
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| | SCHOOL OF PHYSICAL & MATHEMATICAL SCIENCES | | | | | | | |
| | MATHEMATICS | | | | | | | |
| Total | Questions | : 60 | | | Questio | n Booklet | t Series | |
| Time | Allowed | 70 Minutes | | | Roll No. : | | | |
| | | | Instructions fo | or Candidates | : | | | |
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| 10 | . Calculators | and mobiles shall | not be permitted | inside the exan | nination hall | | | |
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1. The infimum and supremum of the set 5.

| $\left\{1 + \frac{(-1)^n}{n} : n \in \mathbb{N}\right\} \text{ is }:$ |
|---|
| (A) -1, 1 |
| (B) 0, 1 |
| (C) $-1, \frac{2}{3}$ |
| (D) 0, $\frac{2}{3}$ |

- 2. For any positive real number *a* there exists a positive integer *n* such that :
 - (A) n > a
 - (B) n < a
 - (C) n = a
 - (D) None of the above
- 3. If A = {1, 2, 3 ... n} then the set of limit points of A is :
 - (A) Countable
 - (B) Uncountable
 - (C) Empty
 - (D) Singleton
- 4. A subset S of real numbers has a limit point if :
 - (A) S is finite
 - (B) S is countably infinite
 - (C) S is infinite and bounded
 - (D) S is uncountable
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- The sequence (ρ^n) converges for :
 - (A) $\rho > 1$
 - (B) $-1 \le \rho < 1$
 - (C) $\rho < -1$
 - (D) $-1 < \rho \leq 1$
- 6. The sequence $(n + (-1)^n)$ is :
 - (A) Convergent
 - (B) Divergent
 - (C) Oscillates finitely
 - (D) Oscillates infinitely
- 7. The sequence (a_n) defined by the recursion formula $a_{n+1} = \sqrt{3a_n}$, $a_1 = 1$ is :
 - (A) Monotonically decreasing
 - (B) Monotonically increasing
 - (C) Monotonically increasing and unbounded
 - (D) Monotonically increasing and bounded.
- 8. The sequence (a_n) where $a_n = 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$ converges to :
 - (A) 1
 - (B) 0
 - (C) $\frac{1}{2}$
 - (D) None of the above

9. If $\sum_{n=1}^{\infty} a_n$ is convergent, then for some finite number $\alpha \ge 1$ the series :

(i)
$$\sum_{n=1}^{\infty} a_n$$

(ii)
$$\sum_{n=1}^{\infty} \alpha a_n$$

- (A) (i) is convergent (ii) is divergent
- (B) (i) is divergent (ii) is convergent
- (C) Both are convergent
- (D) Both are divergent

10. The series
$$\sum_{n=1}^{\infty} \left\{ (n^3 + 1)^{\frac{1}{3}} - n \right\}^p$$
 is :

- (A) Convergent for p = 1
- (B) Divergent for p = 1
- (C) Divergent for all values of p
- (D) None of the above

11. The series
$$x + \frac{x^2}{2} + \frac{x^3}{3} + \dots$$
 :

- (A) Converges for x > 1
- (B) Converges for x < 1
- (C) Converges for x = 1
- (D) Converges for all values of x

12. The series
$$1 - \frac{1}{2^p} + \frac{1}{3^p} - \frac{1}{4^p}$$
... converges for :

- (A) p > 1
- (B) p < 1
- (C) p > 0
- (D) p < 0

(A) e (B) -e (C) 1 (D) -1 14. $\lim_{x \to \frac{\pi}{2}} \frac{\log\left(x - \frac{\pi}{2}\right)}{\tan x} =$ (A) $\frac{\pi}{2}$ (B) $-\frac{\pi}{2}$ (C) 0 (D) 1

- 15. For which of the following functions Rolle's theorem fails ?
 - (A) $\sin x$; $x \in [-\pi, \pi]$
 - (B) $\frac{\sin x}{e^x}$; $x \in [0, \pi]$
 - (C) $|x|; x \in [-1, 1]$
 - (D) $x^3 4x$; $x \in [-2, 2]$
- 16. Which of the following functions doesn't have the Maclaurin's expansion :
 - (A) $\log x$
 - (B) $\log(1 + x)$
 - (C) log sec x
 - (D) $\log \cos x$

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13. The maximum value of $(x - l)^2 e^x$ is attained at :

17. The angle between tangent and radius vector 20. Which of the following statements is true for for the curve $r = a(1 + \cos \theta)$ at $\theta = \frac{\pi}{2}$ is :

(A)
$$\frac{\pi}{2}$$

(B)
$$\frac{3\pi}{2}$$

(C)
$$\frac{\pi}{4}$$

(D)
$$\frac{3\pi}{4}$$

- 18. The curve $\frac{x^2}{a^2} \frac{y^2}{b^2} = 1$ has the asymptotes :
 - (A) $y = \pm bx$
 - (B) y = 0
 - (C) $x = \pm by$
 - (D) x = 0
- 19. Which of the following is true for the functions
 - (i) $y = e^x$
 - (ii) $y = \log x$
 - (A) (i) is convex upwards (ii) is concave upwards
 - (B) (i) is concave upwards (ii) is convex upwards
 - (C) (i) is convex downwards (ii) is concave downwards
 - (D) (i) is concave downwards (ii) is convex downwards

- the curve $x^4 + y^4 = 4a^2xy$?
 - (A) The curve is symmetrical w.r.t. x + y = 0
 - (B) The curve is symmetrical w.r.t. x = 0
 - (C) The curve is symmetrical w.r.t. y = 0
 - (D) The curve is symmetrical w.r.t. x = y
- 21. The functional sequence $f_n(x) = \frac{nx}{1+n^2x^2}$ is :
 - (A) Uniformly convergent in [0, 1]
 - (B) Uniformly convergent in [-1, 1]
 - (C) Uniformly convergent in [-1, 0]
 - (D) Uniformly convergent in [1, 2]
- 22. The series $\sum_{n=1}^{\infty} f_n(x)$ is uniformly convergent on [a, b] if there exists a convergent series of positive numbers Σ M_n such that for all $x \in [a, b]$:
 - (A) $| f_n(x) | \leq M_n \forall n$ (B) $| f_n(x) | \ge M_n \forall n$ (C) $|f_n(x)| \leq \sqrt{M_n} \forall n$ (D) $| f_n(x) | \ge \sqrt{M_n} \forall n$
- 23. The limit of a sequence of functions is continuous if :
 - (A) Every function of the sequence is continuous
 - (B) The convergence is uniform
 - (C) Either (A) or (B)
 - (D) Both (A) and (B)

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24. The function
$$f(x) = \begin{cases} 3x-2 & , x \le 0 \\ x+1 & , x > 0 \end{cases}$$
 is :

(A) Continuous

- (B) Discontinuous at x = -1
- (C) Discontinuous at x = 2
- (D) Discontinuous at the origin

25. For
$$u = log(tan x + tan y)$$
, $sin 2x \frac{\partial u}{\partial x} + sin 2y \frac{\partial u}{\partial y} =$

- (A) 0
- (B) 1
- (C) 2
- (D) 4
- 26. Leibnitz theorem is used to find :
 - (A) nth derivative of sum of two functions
 - (B) n^{th} derivative of subtraction of two functions
 - (C) n^{th} derivative of product of two functions
 - (D) None of the above

27.
$$\lim_{x \to 0} (1+x)^{\frac{1}{x}} =$$

(A) 0
(B) 1

- .
- (C) $\frac{1}{e}$
- (D) e

28.
$$\int \frac{dx}{1-4\cos^2 x} =$$
(A) $\frac{1}{2\sqrt{3}} \log \frac{\tan x + \sqrt{3}}{\tan x - \sqrt{3}}$
(B) $\frac{1}{2\sqrt{3}} \log \frac{\tan x - \sqrt{3}}{\tan x + \sqrt{3}}$
(C) $\frac{1}{2\sqrt{3}} \log \frac{\tan x - 2\sqrt{3}}{\tan x - 2\sqrt{3}}$
(D) $\frac{1}{2\sqrt{3}} \log \frac{\tan x - 2\sqrt{3}}{\tan x - 2\sqrt{3}}$
(D) $\frac{1}{2\sqrt{3}} \log \frac{\tan x - 2\sqrt{3}}{\tan x + 2\sqrt{3}}$
29. $\int \frac{dx}{(x+1)\sqrt{x+2}} =$
(A) $\log \frac{\sqrt{x+2}}{\sqrt{x+2}} - 1$
(B) $\log \frac{\sqrt{x+2}}{\sqrt{x+2}} + 1$
(C) $\log \frac{\sqrt{x+2} + 1}{\sqrt{x+2} - 1}$
(D) $\log \frac{\sqrt{x+2} - 1}{\sqrt{x+2} + 1}$
30. If $f(m, n) = \int_{0}^{\pi/2} \cos^m x \cos nx \, dx$ then :
(A) $f(m, n) = \frac{n}{m+n} f(m+1, n+1)$
(B) $f(m, n) = \frac{m}{m+n} f(m+1, n+1)$
(C) $f(m, n) = \frac{m}{m+n} f(m-1, n-1)$
(D) $f(m, n) = \frac{m}{m+n} f(m-1, n-1)$

- $J_{n}(x)$ are connected with the relation :
 - (A) $J_{-n}(x) = -J_{n}(x)$
 - (B) $J_{n}(x) = (-1)^{n} J_{n}(x)$
 - (C) $J_{-n}(x) = -J_{-n}(x)$
 - (D) $J_{-n}(x) = (-1)^n J_{-n}(x)$
- 32. $\int J_n(x) \, dx =$
 - (A) $-J_2(x) \frac{2}{x}J_2(x)$ (B) $J_2(x) - \frac{2}{x}J_2(x)$ (C) $-J_2(x) + \frac{2}{x}J_2(x)$
 - (D) None of the above
- 33. The Legendre polynomial for $m \neq n$,
 - $\int_{-\infty}^{\infty} P_{m}(x) P_{n}(x) dx =$
 - (A) -1
 - (B) 1
 - (C) 0
 - (D) None of the above
- 34. Which of the following sets is a group under multiplication modulo 8?
 - (A) $\{1, 3, 5, 7\}$
 - (B) {1, 2, 3, 4}
 - (C) $\{2, 4, 6, 8\}$
 - (D) $\{1, 2, 3, 4, 5, 6, 7\}$
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- 31. For integer n, the Bessel functions $J_n(x)$ and 35. What is the order of the dihedral group of square ?
 - (A) 2
 - (B) 4
 - (C) 6
 - (D) 8
 - 36. Which of the following is not a group under multiplication?
 - (A) $\mathbb{R} \{0\}$
 - (B) ℝ
 - (C) $\{1, -1, i, -i\}$
 - (D) {1, ω , ω^2 }
 - 37. The identity of the set of positive rationals w.r.t. the binary operation $a * b = \frac{ab}{3}$ is :
 - (A) 0
 - (B) 1
 - (C) 3
 - (D) $\frac{1}{3}$
 - 38. If G is a finite group of even order
 - (i) order of subgroup of G divides order of G
 - (ii) G has an element of order two.
 - (A) Only (i) is true
 - (B) Only (ii) is true
 - (C) Both are true
 - (D) Both are false
- 39. If H and K are subgroups of a group G of finite 43. If R is a ring (i) $C = \{x \in R : xy = yx, z \in R\}$ order and $O(H) > \sqrt{O(G)}$, $O(K) > \sqrt{O(G)}$, then :
 - (A) $O(H \cap K) = \sqrt{O(G)}$
 - (B) $O(H \cap K) = 1$
 - (C) $O(H \cap K) < 1$
 - (D) $O(H \cap K) > 1$
- 40. If $H \subseteq G$ be a subgroup of a group G then which of the following is not true ?
 - (A) Ha = H if $a \in H$
 - (B) Ha = H if $a \in G$
 - (C) Ha = Hb if $ab^{-1} \in H$
 - (D) $ab^{-1} \in H$ if Ha = Hb
- 41. Which of the following statements is true ?
 - (A) Any finite group of order n is cyclic if it has an element of order n.
 - (B) Every cyclic group need not be abelian.
 - (C) The group of integers is not cyclic.
 - (D) None of the above
- 42. If M is a set of all matrices of the type $\begin{pmatrix} a & b \\ -\overline{b} & \overline{a} \end{pmatrix}$

where bars denote the complex conjugates, then M is a :

- (A) Division ring
- (B) Ring but not a division ring
- (C) Field
- (D) Not a ring

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- $\forall y \in R$, (ii) N(a) = {r \in R : ar = ra} then :
 - (A) C is a subring, N(a) is not
 - (B) N(a) is a subring, C is not
 - (C) Both are subrings
 - (D) None is a subring
- 44. In a ring M of matrices of order 2 over integers

the set
$$S = \left\{ \begin{pmatrix} a & 0 \\ b & 0 \end{pmatrix} : a, b \in \mathbb{Z} \right\}$$
 is a :

- (A) Right ideal
- (B) Left ideal
- (C) Two sided ideal
- (D) None of the above
- 45. If R[x] denotes a polynomial ring over R then which of the following statements is true ?
 - (A) R is commutative if R[x] is commutative
 - (B) R[x] is commutative if R is commutative
 - (C) R has no proper zero divisors if R[x] has no proper zero divisors
 - (D) All the above
- 46. The union of two subgroups N_1 and N_2 of a group G is normal if :
 - (A) $N_1 \cap N_2 = \varphi$
 - (B) $N_1 \cap N_2 \neq \varphi$
 - (C) $N_1 \cup N_2 \neq \varphi$
 - (D) None of the above

- 47. Which of the following is true for the groups 51. If M and N are homogenous in Mdx + Ndy = 0 $G_1 = \{1, -1, i, -i\}$ and $G_2 = (\mathbb{Z}, +)$?
 - (A) All subgroups of G_1 are normal
 - (B) All the subgroups of G_2 are normal
 - (C) Both (A) and (B)
 - (D) None of the above
- 48. If N is a normal subgroup of a group G then :

(A)
$$O\left(\frac{G}{N}\right) = O(G) - O(N)$$

(B) $O\left(\frac{G}{N}\right) = O(G) + O(N)$
(C) $O\left(\frac{G}{N}\right) = O(G) \cdot O(N)$
(D) $O\left(\frac{G}{N}\right) = \frac{O(G)}{O(N)}$

49. $\frac{dx}{dy} + Qx = Px^n$ is a Bernoulli's differential

equation where P and Q are :

- (A) Functions of x only
- (B) Functions of x or constants
- (C) Constants only
- (D) Functions of y or constants

50.
$$\frac{1}{D^2 + 4}\cos 2x =$$
(A)
$$\frac{x}{4}\sin 2x$$
(B)
$$\frac{x}{-4}\sin 2x$$
(C)
$$\frac{x}{4}\cos 2x$$
(D)
$$\frac{x}{-4}\cos 2x$$

then the integrating factor is :

(A)
$$Mx + Ny$$

(B) $Mx - Ny$
(C) $\frac{1}{Mx + Ny}$
(D) $\frac{1}{Mx - Ny}$
52. $\frac{1}{f(D)}e^{-x}V =$
(A) $e^{-x}\frac{1}{f(D)}V$
(B) $e^{-x+1}\frac{1}{f(D)}V$
(C) $e^{-x}\frac{1}{f(D+1)}V$
(D) $e^{-x}\frac{1}{f(D-1)}V$

- 53. The solution of the ordinary differential equation $y^2 \log y = xyp + p^2$ is :
 - (A) $\log x = cy + c^2$ (B) $\log y = cx + c^2$ (C) $\log y^2 = cx + c^2$

 - (D) $\log x^2 = cy + c^2$
- 54. The solution of the ordinary differential equation $p^2 = y^2 + 1$ is :
 - (A) $y = sin(c \pm x)$
 - (B) $y = \cos(c \pm x)$
 - (C) $y = \sinh(c \pm x)$
 - (D) $y = \cosh(c \pm x)$

- 55. What is the singular solution of the differential 58. What is the general solution of the partial equation $2px + y^2p^3$?
 - (A) $y = cx + \frac{c^3}{8}$ (B) $y = cx - \frac{c^3}{8}$ (C) $y^2 = cx - \frac{c^3}{8}$ (D) $y^2 = cx + \frac{c^3}{8}$
- 56. The singular solution of the ordinary differential
 - equation $y = xp + \frac{a}{p}$ is :
 - (A) $y^2 = 4ax$
 - (B) $y^2 = -4ax$
 - (C) $x^2 = 4ay$
 - (D) $x^2 = -4ay$
- 57. The partial differential equation by eliminating the arbitrary constants of the equation
 - $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$ is : (A) z = px + qy
 - (B) 2z = px + qy
 - (C) 2z = px qy
 - (D) z = px qy

- differential equation $\frac{y^2z}{x}p + xzq = y^2$. (A) $\phi(x^3 - y^3, x^3 - z^3) = 0$ (B) $\phi(x^3 + y^3, x^3 + z^3) = 0$ (C) $\phi(x^3 - y^3, x^2 - z^2) = 0$ (D) $\phi(x^3 + y^3, x^2 + z^2) = 0$
- 59. The complete solution of the partial differential equation $\sqrt{p} + \sqrt{q} = 1$ is :
 - (A) $z = -ax + (1 \sqrt{a})^2 y + c$ (B) $z = ax - (1 - \sqrt{a})^2 y + c$ (C) $z = -ax - (1 - \sqrt{a})^2 y + c$ (D) $z = ax + (1 - \sqrt{a})^2 y + c$
- 60. What is the solution of the partial differential equation x + qy = pq ?

(A)
$$az = \frac{1}{2}(y + ax)^2 + b$$

(B) $az = \frac{1}{2}(y - ax)^2 + b$
(C) $az = (y + ax)^2 + b$
(D) $az = (y - ax)^2 + b$

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ROUGH WORK

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| er finnen andere and | | MATHEN | MATICS |
| Total | Questions : | 60 | Question Booklet Series |
| Time | Allowed : | 70 Minutes | Roll No. : |
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| 2. | OMR Answer making entries so that the entri Copy. | Sheet has an Original Copy and a s in the Original Copy, candidate s ries made in the Original Copy ag | a Candidate's Copy glued beneath it at the top. Whil should ensure that the two copies are aligned properl gainst each item are exactly copied in the Candidate' |
| 3. | All entries in th Copy only. | ne OMR Answer Sheet, including | answers to questions, are to be recorded in the Origina |
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| 5. | Use only blue/l gel/ink pen or | black ball point pen to darken the pencil should be used. | circle of correct/most appropriate response. In no cas |
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| 10 | . Calculators and | l mobiles shall not be permitted i | inside the examination hall. |
| 11 | . Rough work, if | any, should be done on the blank | k sheets provided with the question booklet. |
| 12 | . OMR Answer S it will not be ev | Sheet must be handled carefully a valuated. | and it should not be folded or mutilated in which case |
| 13 | . Ensure that you herself. | ur OMR Answer Sheet has been | signed by the Invigilator and the candidate himself |
| 14 | At the end of the off the original candidate. | e examination, hand over the OM OMR sheet in presence of the C | AR Answer Sheet to the invigilator who will first tear Candidate and hand over the Candidate's Copy to the |
| J-307 | - C | |) [Turn over |

In S_n the number of distinct cycles of length $r \le n$ is :

(A)
$$\frac{1}{r} \frac{n!}{(n-r)!}$$

1.

(B)
$$r \frac{n!}{(n-r)!}$$

(C)
$$n \frac{n!}{(n-r)!}$$

- (D) None
- 2. The identity of the group $\frac{G}{N}$ is :
 - (A) G
 - (B) $\frac{1}{G}$
 - (C) N
 - (D) $\frac{1}{N}$
- 3. Which of the following is not a ring (w.r.t. usual 8. operations) ?
 - (A) $\mathbb{Z}[i] = \{a + ib : a, b \in \mathbb{Z}\}$
 - (B) $R = \{a + b\sqrt{2} + c\sqrt{3} + d\sqrt{2} : a, b, c, d \in \mathbf{Q}\}$
 - (C) $\mathbb{Q}[\sqrt{p}] = \{a + b\sqrt{p} : a, b \in \mathbb{Q}\}$ for prime p
 - (D) $R = \{a : a \in \mathbf{Q}^*\}$
- 4. If $R = \{f : [a, b] \rightarrow \mathbb{R}, f \text{ is continuous}\}, then : 9$.
 - (A) R is not a ring
 - (B) R is a ring without unity
 - (C) R is a ring but not commutative
 - (D) R is a commutative ring with unity

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5. $G_n = \left\{ e^{\frac{2i\pi r}{n}} : r = 0, 1, 2, 3, ..., n-1 \right\}$ is a cyclic group with generator : (A) 1 (B) e (C) $e^{\frac{2i\pi}{n}}$ (D) $e^{2in\pi}$ The symmetric group S_3 is : 6. (A) Abelian (B) Infinite (C) Non-Abelian (D) Cyclic Which of the following is a homomorphism from $(\mathbb{Z}, +)$ to $(\mathbb{R}, +)$? (A) $f(a) = a^2$ (B) f(a) = 2a(C) $f(a) = \frac{2}{a}$ (D) $f(a) = a^3$ Let M be the ring of all 2×2 matrices, then $S = \left\{ \begin{pmatrix} a & 0 \\ b & 0 \end{pmatrix} : a, b \in \mathbb{Z} \right\} \text{ is :}$ (A) Left ideal but not right ideal (B) Right ideal but not left ideal (C) Two sided ideal (D) None of the above Which of the following is true? (A) Ring of order 7 is non-commutative (B) Ring with unity of order 25 is non-commutative (C) Ring with unity of order 9 is commutative (D) Ring of order 49 is always commutative 2

- 10. Which of the following is not true?
 - (A) Every integral domain is a field
 - (B) Every field is not an integral domain
 - (C) Every finite integral domain is a field
 - (D) Every finite integral domain is not a field
- 11. If R is a ring and R[x] the polynomial ring. Then:
 - (A) If R is commutative then R[x] is commutative
 - (B) If R has no proper zero divisors then R[x] has no proper zero divisors
 - (C) If R is an integral domain the R[x] is an integral domain
 - (D) If R is a field then R[x] is a field
- 12. For the Bessel function J, $[x^n J_n(x)]' =$
 - (A) $x^n J_{n-1}(x)$
 - (B) $x^{n-1} J_{n-1}(x)$
 - (C) $x^n J_n(x)$
 - (D) $nx^{n-1} J_{n-1}(x)$
- 13. The smallest positive root of J₀(x) = 0 lies in the interval :
 - (A) $(\sqrt{2}, 2)$
 - (B) (0, 1)
 - (C) $(3,\sqrt{10})$
 - (D) $(2,\sqrt{8})$
- 14. For the Legendre function, $P_n(-x) =$
 - (A) $-P_n(x)$
 - (B) $(-1)^{n}P_{n}(x)$
 - (C) $P_n(x)$
 - (D) $(-1)^{n+1}P_n(x)$
- 15. The order of the Legendre differential equation

is : (A) 1

- (B) 2
- (C) 3
- (D) 4

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- 16. Which of the following statements is not true ?
 - (A) Every infinite set has a bijection with its proper subset
 - (B) Every finite set can be put in one-one, onto correspondence with the set {1, 2, 3,n}
 - (C) Every infinite is equivalent to the set of integers
 - (D) Every infinite set contains a countable set Which of the following functions is not
- 17. Which of the following functions is not uniformly continuous?
 - (A) $f(x) = x^2$ in [1, 2]

(B)
$$f(x) = \sqrt{x}$$
 in [0, 2]

(C)
$$f(x) = x in [0, 1]$$

(D)
$$f(x) = \frac{1}{x} in(0, 1)$$

18. The number of limit points of the set

$$\begin{cases} \frac{1}{n}; n = 1, 2, 3, \dots \end{cases} is:$$
(A) 1
(B) 2

- (B) 2
- (C) 0 (D) ∞
- $(D) \sim$
- 19. Which of the following sequences is not convergent?

(A) $\left(\frac{1}{n}\right)$ (B) $\left(\frac{1}{n^2}\right)$ (C) $\left(\frac{n}{n+1}\right)$ (D) $\left(\frac{n^2}{n+1}\right)$

- 20. The series $\frac{1}{(\log 2)^p} + \frac{1}{(\log 3)^p} + \dots + \frac{1}{(\log n)^p} + \dots$
 - (A) Converges for p > 0
 - (B) Converges for p < 0
 - (C) Diverges for p > 0
 - (D) Oscillates

[Turn over

21. Which among the following series is not 25. Which of the following sets is not countable? convergent?

(A)
$$\frac{p^n}{n!}, p > 0$$

(B)
$$\frac{p^n}{n^n}, p > 0$$

(C)
$$\frac{\sqrt{nx^n}}{\sqrt{n^2+1}}, x \ge 1$$

(D)
$$\frac{1.2.3...n}{7.10....(3n+4)}$$

22. Which of the following statements is not true ?

- (A) Every bounded sequence is convergent
- (B) Every convergent sequence is bounded
- (C) Every bounded monotonic sequence is convergent
- (D) Every bounded sequence with unique limit point is convergent

23. For the series (i)
$$\sum \frac{(-1)^{n+1}}{\sqrt{n}}$$
 (ii) $\sum \frac{(-1)^{n+1}}{3n-2}$: 2

- (A) Both are absolutely convergent
- (B) Only (i) is absolutely convergent
- (C) Only (ii) is absolutely convergent
- (D) Both are conditionally convergent

24. The function $f(x) = \begin{cases} \frac{\sin 2x}{x} & \text{when } x \neq 0 \\ 1 & \text{when } x = 0 \end{cases}$ when x = 0

(A) Removable discontinuity at origin

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- (B) Essential discontinuity
- (C) No discontinuity
- (D) None of the above

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(A) $\mathbb{Z} \times \mathbb{Z}$ (B) \mathbb{Q} (C) $\{x : 0 < x < 1\}$ (D) $\{\frac{1}{n} : n = 1, 2, 3,\}$

26. The set $S = \{x : x \in \mathbb{Q} \text{ and } x^2 < 2\}$:

- (A) Is a bounded above subset and supremum exists in \mathbb{Q}
- (B) Is not bounded above subset of \mathbf{Q}
- (C) Is a bounded above and has not a supremum in \mathbf{Q}
- (D) None
- 27. If (a_n) is a Cauchy sequence in \mathbb{R} , then :
 - (A) (a_n) is bounded but not convergent
 - (B) (a_n) is convergent but not bounded
 - (C) (a_n) is convergent as well as bounded
 - (D) Nothing can be said

8. The sequence of functions $f_n(x) = e^{-nx}$, $x \in [1, 3]$ is :

- (A) Point-wise convergent but not uniformly convergent
- (B) Uniformly convergent
- (C) Not convergent
- (D) None

29. The series $\sum_{n=1}^{\infty} \frac{(-1)^n n^{500}}{(1.0001)^n}$

- (A) Converges absolutely
- (B) Converges conditionally not absolutely
- (C) Diverges to $-\infty$
- (D) Diverges to ∞
- **4** 000

| 30 | . According to root test the positive term series 36 | 5. The degree of the homogeneous function |
|------------|---|---|
| - | $\sum a_n$ converges if $l < 1$ where : | $x^2 + y^2$ v |
| | (A) $l = \lim_{n \to \infty} (a_n)^n$ | $\frac{y^2}{x^2 - y^2} \frac{\cos y}{x}$ is : |
| i. | (B) $l = \lim_{n \to \infty} (2^n)^{\frac{1}{n}}$ | (A) 0 |
| | (C) $l = \lim_{n \to \infty} (a_n)^n$ | (B) 1 |
| | $(C) i = \min_{n \to \infty} (na_n)^n$ | (C) 2 |
| | (D) $l = \lim_{n \to \infty} (na_n)^{\frac{1}{n}}$ | (D) -1 |
| 31. | $r = ae^{m\theta}$ represents a : | For the functions (i) $y = e^x$ (ii) $y = \log x$: |
| К | (A) Circle | (A) Both are convex |
| | (B) Parabola | (C) (i) is concave (ii) is convex |
| | (C) Cardioid | (D) (i) is convex (ii) is convex |
| | (D) Spiral 38 | . Which of the following statement is true ? |
| 32. | Which of the following functions does not have | (A) Angle between two curves is the angle |
| | a Taylor's expansion in the interval $[-1,1]$? | between their tangents |
| | $(\mathbf{A}) \mathbf{X} $ $(\mathbf{B}) \sin \mathbf{x}$ | (B) Angle between two curves is the angle |
| | $(C) \cos x$ | (C) Angle between their normals |
| | (D) e^x | (c) Angle between two curves is the angle between tangent of one aways and |
| 33. | If $f(x) = x^2 - 6x + 8$ in the interval [2.4] Then | of other |
| | f'(x) = 0, where $x =$ | (D) None of the above statements is true |
| | (A) 2 | |
| | (B) 4 39. | The maximum value of the function $f(x) = \frac{\log x}{x}$ |
| | (C) 3 | is: |
| n agika | (D) 1 | (A) e |
| 34. | Leibnitz's theorem is used to find : | (B) e^2 |
| | (A) n th derivative of trigonometric function | (C) log e |
| | (B) n th derivative of exponential functions | (D) $\frac{1}{2}$ |
| | (C) n th derivative of quotient of two functions | e e |
| 25 | (D) n^{m} derivative of product of two functions | $\lim \frac{\sin \theta - \theta \cos \theta}{2}$ |
| 55. | If $y = 100^{\circ}$. Then the n th derivative $y_n = 40$. | $\lim_{\theta \to 0} \sin \theta - \theta =$ |
| | (A) 100° (B) $100^{\circ} \times 100^{\circ}$ | (A) 1 |
| | (C) $100^{\times} \times 2^{n}$ | (B) -1 |
| | (D) $100^{\times} \times 2$ | (C) -2 |
| | | (D) 2 |
| | | |

JJ-307-C

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41. The curvature of an ellipse is maximum at : (ii) $\frac{dy}{dx}$ 46. (i) ∫ (A) Ends of major axis (A) (i) is linear (ii) is not (B) Ends of minor axis (B) (ii) is linear (i) is not (C) Ends of the line through focus (C) Both are linear (D) Both are not linear (D) None 42. The number of asymptotes to the curve $_{47.}$ $\int_{0}^{\frac{\pi}{2}} \sin^{6} x dx =$ $\left(\frac{y}{x}\right)^2 = \frac{4a}{x}$ is : $\frac{6\pi}{32}$ (A) $\frac{3\pi}{32}$ (A) 1 (B) (B) 2 $\frac{\pi}{32}$ (C) 3 (C) (D) 0 (D) $\frac{5\pi}{32}$ 43. The length of polar sub-tangent to the curve $f(r, \theta) = 0$ is : 48. The order and degree of the differential equation (A) $r^2 \frac{d\theta}{dr}$ $\left\{1 + \left(\frac{d^2 y}{dx^2}\right)^3\right\}^2 = 3\left(\frac{d^3 y}{dx^3}\right)^2 \text{ is :}$ (B) $r^2 \frac{dr}{d\theta}$ (A) 3 and 2(B) 2 and 3 (C) $\frac{1}{r^2} \frac{d\theta}{dr}$ (C) 3 and 6 (D) 6 and 6 (D) $\frac{1}{r^2} \frac{dr}{d\theta}$ 49. The integrating factor of the differential equation xdy = y(1 + xy)dy is : (A) e^x 44. $\int_0^{\pi} \frac{\sin nx}{\sin x} dx =$ (B) e^{-x} (C) x (D) -x (A) 0 if n is even 50. The differential equation Mdy + Ndx = 0 is exact (B) π if n is odd if: (C) Both (A) and (B) true (A) $\frac{\partial M}{\partial y} = \frac{\partial N}{\partial x}$ (D) None 45. $\int \frac{\sqrt{x}}{x+1} =$ (B) $\frac{\partial N}{\partial y} = \frac{\partial M}{\partial x}$ (A) $2\sqrt{x} - 2\tan^{-1}\sqrt{x}$ (C) $\frac{\partial M}{\partial y} = -\frac{\partial N}{\partial x}$ (B) $2\sqrt{x} - 2\sin^{-1}\sqrt{x}$ (D) $\frac{\partial N}{\partial v} = -\frac{\partial M}{\partial x}$ (C) $2\sqrt{x} - 2\cos^{-1}\sqrt{x}$ (D) $2\sqrt{x} - 2\cot^{-1}\sqrt{x}$

| 51. The solution of the differential equation | |
|---|--|
| (dv 2 a) | on 56. Which of the following is not a group? |
| $(1+x^2)\left(\frac{4y}{dx}-4x^2\cos^2 y\right) + x \sin 2y = 0$ wi | th (A) $(\mathbb{Z}, +)$ |
| integrating factor $(1 + x^2)$ is : | (B) $(\mathbb{R}, +)$ |
| $4x^3$ | (C) (\mathbb{R}, \times) |
| (A) $(1 + x^2) \tan y = \frac{1}{3} + 3$ | (D) $(0, +)$ |
| $4x^3$ | |
| (B) $(1 + x^2) \sec y = \frac{11}{3} + 3$ | 57. If $a * b = \frac{ab}{a} a, b \in 0^+$ 0^+ is set of positive |
| $4x^3$ | 2 st - Q, Q is set of positive |
| (C) $(1 + x^2) \sin y = \frac{1x}{3} + 3$ | |
| $4 x^3$ | (A) 1 |
| (D) $(1 + x^2) \cot y = \frac{4x}{3} + 3$ | (B) 2 |
| 52. The solution of the differential equation | \sim (C) 3 |
| $p^2y + 2py = y$ is : | $n (C) \frac{1}{2}$ |
| (A) $x^2 = 2 cxy + c^2$ | 1 |
| (B) $y^2 = 2 cxy + c^2$ | (D) $\frac{1}{2}$ |
| (C) $x^2 = 2 cy + c^2$ | 59 T1 1 5 |
| (D) $y^2 = 2 cx + c^2$ | 58. The order of i in the multiplicative group $\begin{cases} 1 & 1 \\ 1 & 1 \\ 1 & 1 \end{cases}$ |
| 53. The solution of the differential equation | $\{-1, 1, -1, 1\}$ IS: (A) 1 |
| $(x^2D^2 + 3xD)x = \frac{1}{2}$ | (B) 2 |
| $(x D + 3xD)y = \frac{1}{x}$ is: | (C) 3 |
| (A) $A + Bx^{-2} + x^{-1}$ | (D) 4 |
| (B) $A + Bx + x^{-1}$ | 59. If $(\mathbb{Z}, *)$ is a group with $* h = a + b + 1 \forall a, b \in \mathbb{Z}$ |
| (C) $A + Bx^{-2} + x$ | Then inverse of an element a is : |
| (D) $A + Bx^2 + x^{-1}$ | (A) 0 |
| 54. The number of constants in the solution of a | (B) -2 |
| partial differential equation depends on : | (C) - a - 2 |
| (A) Order of differential equation | (D) $a + 2$ |
| (B) Degree of differential equation | $(1 \ 2 \ 3 \ 4 \ 5)$ |
| (C) Number of independent variables | 00. Let $S = \{1, 2, 3, 4, 5\}$ and $f = \begin{bmatrix} 2 & 1 & 4 & 3 & 5 \end{bmatrix}$, |
| (D) Number of dependent variables | then the number of orbits of S under the |
| 55. The differential equation $5 \partial^2 z = \partial^2 z$ | permutation f is : |
| The differential equation $3\frac{\partial^2}{\partial x^2} + 6\frac{\partial^2}{\partial y^2} = xy$ is | (A) 1 |
| classified as : | (B) 2 |
| (A) Elliptical | $(\mathbf{C}) 3$ |
| (B) Parabolic | (<i>D</i>) 4 |
| (C) Hyperbolic | |
| (D) None | |
| JI-307 C | |
| 7 7 7 | |

1. The locus of the middle points of a system of parallel 6. chords of a parabola $y^2 = 4ax$ is :

- (A) A straight line
- (B) A circle
- (C) An ellipse
- (D) A parabola
- The eccentricity of an ellipse whose latus rectum is equal to one half of its minor axis is :
 - (A) $\frac{1}{2}$
 - **(B)** 1
 - (C) $\frac{\sqrt{3}}{2}$
 - (D) $\frac{1}{\sqrt{2}}$
- If e and e* are the eccentricities of a hyperbola and a conjugate hyperbola, then :
 - (A) $e^2 + e^{*2} = 1$
 - (B) $e^2 + e^{*2} = e^2 e^{*2}$
 - (C) $e^2 e^{*2} = 1$
 - (D) $e + e^* = ee^*$
- 4. If $ab h^2 = 0$, then the equation
 - $ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$ represents :
 - (A) A parabola
 - (B) An ellipse
 - (C) A circle
 - (D) A hyperbola
- 5. Which of the following is the condition for the spheres $a(x^2+y^2+z^2)+2lx+2my+n=0$ and $b(x^2+y^2+z^2)=k^2$ to cut orthogonally?
 - (A) $ap^2 = bk$
 - (B) bp² = ak
 - (C) $pk^2 = ab$
 - (D) $ak^2 = bp$

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The equation $ax^2 + by^2 + cz^2 + 2ux + 2vy + 2wz + d = 0$ will represent a cone if:

- (A) $\frac{a^2}{u} + \frac{b^2}{v} + \frac{c^2}{w} = d$
- (B) $au^2 + bv^2 + cw^2 = d$
- (C) $\frac{u^2}{a} + \frac{v^2}{b} + \frac{w^2}{c} = d$

(D)
$$\frac{u^2}{a} + \frac{v^2}{b} + \frac{w^2}{c} = 0$$

- The equation of the right circular cylinder whose axis is the z-axis and radius is 'a' is :
 - (A) $x^2 + y^2 = a^2$
 - (B) $x^2 + z^2 = a^2$
 - (C) $y^2 + z^2 = a^2$
 - (D) $x^2 + y^2 + z^2 = a^2$
- 8. The equation of the tangent planes to the
 - ellipsoid $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$ which are parallel to lx + my + nz = 0 are :

(A)
$$lx + my + nz = \pm \sqrt{a\ell^2 + bm^2 + cn^2}$$

(B)
$$lx + my + nz = \pm \sqrt{a^2 \ell^2 + b^2 m^2 + c^2 n^2}$$

(C)
$$lx + my + nz = \pm \sqrt{\frac{\ell^2}{a} + \frac{m^2}{b} + \frac{n^2}{c}}$$

(D)
$$lx + my + nz = \pm \sqrt{\frac{\ell^2}{a^2} + \frac{m^2}{b^2} + \frac{n^2}{c^2}}$$

| 1 | WIS! | [2 | 1 | 1 | an l | | | | 13. | 3. Which of the following is true for a square matrix A of order n whose rank is less than n? |
|-----|----------------------------------|----------------------------------|---|------------------------------|--------------------------|---------------------------|-------------------|------------------------|----------|--|
| 9. | If A = | = 0 1 | 1 1 | 0 2 | , then A | 4 ⁴ −5. | A ³ +7 | 'A ² -2A | +I | (A) A =0 (B) The columns of A are linearly dependent (C) The rows of A are linearly dependent |
| | (I is th | e uni | t mat | rix of | order 3 |) is ea | qual to | o: | 14. | (D) All of these The value of 'a' for which the system of equations |
| | | 3 | 1 | 1] | | 1.1 | | | | x + 2y + 3z = ax, $3x + y + 2z = ay$, $2x + 3y + z = azhave non-zero solutions is :$ |
| | (A) | 0 | 2 | 0 | | | | | | (A) $a = 2$ (B) $a = 4$ |
| | | [2 | 1 | 1] | | | | | | (C) $a = 6$ (D) $a = 1$ |
| | (B) | 0 | 1 | 0 | | | | 1.2 | 15. | 5. The number of linearly indpendent solutions of the equation $x + y + z + t = 1$ is: (A) 2 |
| | Sacar | [1 | 1 | 2 | - | | | and a | | (A) 2 (B) 3 (C) 4 |
| | | 8 | 5 | 5 | | | | | 16 | (D) 5 6 Which of the following is not a normal vector? |
| | (C) | 5 | 5 | 8 | - 8 | | | | 10. | |
| | | 5 | 4 | 4] | | | | | | (A) i |
| | (D) | 0 | 1 | 0 | | | | | | [1-1] |
| | | L | - | - | Γ 2 | 1 | 1 | 17 | | $\left[\frac{2}{3}\right]$ |
| 10. | The ra | nk of | the n | natrix | 5 | 2 | 0 | -1 -1 | s: | (B) $\frac{2}{3}$ |
| | • | | | | -4 0 | 5 0 | 12 0 | -1 0 | 4.4 | $\left\lfloor \frac{1}{3} \right\rfloor$ |
| | (A) 4 | 4 | | | | | | | | [sin A] |
| | (C) 2 (D) 1 | 2 | | | | | | | | (C) $-\cos\theta$ |
| 11. | The ne to be s | ecess calar | ary an is tha | nd suf at its m | ficient | condi equat | tion fo | or a matr of degree | ix e: | |
| | (B) 3 (C) 2 | 3 | | | | | | | | $\left[\begin{array}{c} \frac{1}{\sqrt{3}} \end{array}\right]$ |
| 12. | Which | n of these P. | ne fol Q, R | lowin each | ig is tru of orde | e for a | any th | ree squa | re | (D) $\left -\frac{1}{\sqrt{3}} \right $ |
| | (A) 1 (B) 1 (C) 1 (D) 1 | fr(PC fr(PR fr(RC fr(RI | (R) = (Q) | Tr(Q Tr(R Tr(R Tr(Q | RP) QP) PQ) RP) | | | | 1. I.I. | $\left[\begin{array}{c} \frac{1}{\sqrt{3}} \end{array}\right]$ |
| HF | 0-2063 | 3-B | | | | | | | 3 | [Turn over |

equation $\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$? (A) $\tan x = \frac{1}{2}(y^2 - 1) + ce^{-y^2}$ (B) $\tan y = \frac{1}{2}(x^2 - 1) + ce^{-x^2}$ (C) $\tan y = \frac{1}{2}(x^2 - 1)e^{-x^2} + c$ (D) $\tan x = \frac{1}{2}(y^2 - 1)e^{-y^2} + c$ (A) $x + y \tan^{-1} \frac{y}{y} = c$ (B) $y + x \tan^{-1} \frac{x}{y} = c$ (C)

The particular integral of the differential equation 19. $(D^2 + 5D + 4)y = x^2 + 7x + 9$ is :

(A)
$$\frac{1}{4}\left(x^{2} + \frac{9}{2}x\right)$$

(B) $\frac{1}{4}\left(x^{2} + \frac{23}{8}\right)$
(C) $\frac{1}{4}\left(x^{2} + \frac{9}{2}x + \frac{8}{23}\right)$
(D) $\frac{1}{4}\left(x^{2} + \frac{9}{2}x + \frac{23}{8}\right)$

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differential equation
$$\frac{d^2y}{dx^2} + y = \csc x$$
?

- (A) $y = c_1 \cos x + c_2 \sin x + \sin x \log \sin x$
- (B) $y = c_1 \cos x + c_2 \sin x + \cos x \log \cos x x \sin x$
- (C) $y = c_1 \cos x + c_2 \sin x + \sin x \log \sin x x \cos x$
- (D) $y=c_1\cos x + c_2\sin x + \cos x \log \cos x x \cos x$
- Which of the following is not true? 21.
 - (A) Any subset of a countable set is countable
 - (B) Any subset of an uncountable set is uncountable
 - (C) If A and B are countable sets, then A U B and A ∩ B are also countable
 - (D) Every infinite set contains a countable set
- 22. Which of the following is true for any sequence {a,} of real numbers?
 - (A) If $\{a_n\}$ is monotonically increasing, then it is convergent.
 - (B) If {a_n} is monotonically decreasing, then it is convergent.
 - (C) If {a,} is bounded, then it is convergent.
 - (D) If {a_n} is a Cauchy sequence, then it is convergent.

For what value of x does the series 23.

- $1 + x + x^2 + x^3 + \dots$ oscillate infinitely?
- (A) x = -1
- (B) |x| < 1
- (C) $x \ge 1$
- (D) x < -1
- Which of the following series is not convergent ? 24.

(A)
$$\sum_{n=1}^{\infty} \cot^{-1} n^2$$

(B) $\sum_{n=1}^{\infty} \frac{n^p}{n!}$
(C) $\sum_{n=1}^{\infty} \frac{1^2 \cdot 3^2 \cdot 5^2 \dots (2n-1)^2}{2^2 \cdot 4^2 \cdot 6^2 \dots (2n)^2}$
(D) $\sum_{n=1}^{\infty} \frac{(-1)^n}{\log n}$

Which of the following is the solution of the differential 20. Which of the following is the general solution of the 17.

$$xdy + ydx + \frac{xdy - ydx}{x^2 + y^2} = 0$$
 is:

D)
$$xy + \tan^{-1} \frac{x}{y} = 0$$

D)
$$xy + \tan^{-1}\frac{x}{y} = c$$

$$xy + \tan^{-1}\frac{y}{x} = c$$

$$xy + \tan^{-1} \frac{x}{-1} = c$$

30. The value of $\iint e^{\frac{y}{x}} dy dx$, where $R = \{(x, y), \}$ 25.

- $0 < x < 1, 0 < y < x^{2}$ is
- (A) 1
- (B) 2
- (C) e
- $\frac{1}{2}$
- (D)

26. If $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ and $r = |\vec{r}|$, then div $(r^n \vec{r}) =$

- (A) $(n+1)r^n$
- (B) $(n+2)r^{n+1}$
- (C) $(n+3)r^{n+2}$
- (D) $(n+3)r^n$
- Which of the following is true for the function 27.

 $f(x, y) = \sqrt{|xy|}$?

- (A) f(x, y) is differentiable at the origin
- (B) f(x, y) is not differentiable at the origin
- (C) The partial derivatives f, f, are continuous at the origin
- (D) None of the above
- Which of the following is true for the function 28.
 - $f(x, y) = x^2 3xy^2 + 2y^4?$ (A) f(x, y) has a maximum value at the origin
 - (B) f(x, y) has a minimum value at the origin
 - (C) f(x, y) has neither a maximum value nor a minimum value at the origin
 - (D) None of the above
- 29. If f(x) is bounded and integrable on [a, b] and $f(x) \ge 0, \forall x \in [a, b], \text{ then}:$

(A)
$$\int_{a}^{b} f(x) dx \ge 0$$
 for $a \le b$

(B)
$$\int_{a}^{b} f(x) dx \le 0 \text{ for } a \le b$$

(C)
$$\int_{a}^{b} f(x) dx \ge 0 \text{ for } b \le a$$

(D) None of the above holds HFO-20633-B

- Which of the following is/are necessary and sufficient condition(s) for a bounded function f to be integrable on [a, b]?
- (A) For any $\varepsilon > 0$, there exists a partition P of [a, b] such that $U(P, f) - L(P, f) < \varepsilon$.
- (B) For any ε > 0, there exists a partition P of [a, b] and a number I lying between L(P, f) and U(P, f) such that :

 $|U(P, f) - I| < \varepsilon$ and $|L(P, f) - I| < \varepsilon$.

(C) For any $\varepsilon > 0$, there exists a $\delta > 0$ such that if P, P* are any two partitions of [a, b] with mesh less than \delta, then :

 $|S(P, f) - S(P^*, f)| \leq \varepsilon.$

- All the above (D)
- Which of the following is the value of $\int (x + |x|) dx$?
- (A) 0

31.

- (B) -1
- (C) 1
- (D) 2
- Which of the following is true for the function f defined 32. on [0, 1] by :

f(x) = 0, when x is irrational or zero = 1/n, when x is any non-zero rational number m/n in its lowest form.

- (A) f(x) is integrable on [0, 1] and the value of the integral is 0.
- (B) f(x) is integrable on [0, 1] and the value of the integral is 1.
- (C) f(x) is not integrable on [0, 1].
- (D) None of the above
- 33. Which of the following is/are true for any group G of prime order ?
 - (A) Giscyclic
 - (B) G is Abelian
 - (C) G has exactly two subgroups
 - (D) All the above

[Turn over

- 34. Which of the following is not true?
 - (A) Every group is a normal subgroup of itself.
 - (B) The center of every group is a normal subgroup of that group.
 - (C) Every subgroup of an Abelian group is normal.
 - (D) There is no non-Abelian group for which every subgroup is normal.
- 35. The exponential map from the group C of complex numbers with addition to the group C* of non-zero complex numbers with multiplication is a homomorphism with kernel:
 - (A) {0}
 - (B) {1}
 - (C) $\{2k\pi i, k \in Z\}$
 - (D) $\{k\pi i, k \in Z\}$
- 36. If P(S) is the power set of a non-empty set S with addition to be the symmetric difference of sets and multiplication to be intersection, then P(S) is :
 - (A) A division ring
 - (B) A Boolean ring
 - (C) A field
 - (D) None of these
- 37. If S and S* are subspaces of a vector space X over the field F, which of the following is/are subspaces of X over F ?
 - (A) S + S*
 - (B) S ∩ S*
 - (C) $L(S \cup S^*)$
 - (D) All the above
- 38. Which of the following is a basis for the vector space C of complex numbers over itself?
 - (A) {0}
 - **(B)** {1}
 - (C) $\{1, i\}$
 - (D) {i}

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- 39. If T is a homomorphism from X to Y, where X and Y are vector spaces over the same field F, with kernel K, then T is an isomorphism if and only if K =
 - (A) {0}
 - (B) Φ
 - (C) X
 - (D) Y
- 40. If X and Y are finite-dimensional vector spaces over the same field F and f is a homomorphism from X onto Y with kernel K, then :
 - (A) $\dim(X) = \dim(Y)$
 - (B) $\dim(X) = \dim(Y) + \dim(K)$
 - (C) $\dim(Y) = \dim(X) + \dim(K)$
 - (D) $\dim(Y) = \dim(X)/\dim(K)$



- (A) 0
- (B) 1
- (C) 2
- (D) -1

42. Which of the following is true for the function :

$$f(x) = e^{\frac{1}{(x-2)^2}}, x \neq 2$$

= 0, x = 2 ?

- (A) f(x) is continuous at x = 2
- (B) f(x) has a discontinuity of first kind at x = 2
- (C) f(x) has a discontinuity of second kind at x = 2
- (D) None of the above

43. If
$$f(x) = x^{n-1} + e^{2x}$$
, then $f^{(n)}(0) =$

- (A) $(n-1)! + 2^n$
- (B) 2ⁿ
- (C) $(n-1)! + 2^{n-1}$
- (D) $2^n + 1$



44. The coefficient of $(x-a)^2$, when log sin x is expanded 48. as a series in (x-a), is :

- (A) log sin a
- (B) cot a
- (C) $\frac{1}{2}$ cosec²a

(D) $-\frac{1}{2}\csc^2 a$

45. Which of the following is the pedal equation of the

parabola
$$\frac{2a}{r} = 1 - \cos \theta$$
?
(A) $p^2 = ar$
(B) $r^2 = ap$
(C) $a^2 = pr$
(D) $p = ar$
46. If $u = \cos^{-1}\left(\frac{x+y}{\sqrt{x}+\sqrt{y}}\right)$, then $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} =$

(A)
$$\frac{1}{2}\cos u$$

(B) $\frac{1}{2}\cot u$
(C) $-\frac{1}{2}\cot u$
(D) $-\frac{1}{2}\cos u$

- 47. What is the radius of curvature of the circle $r = a \cos \theta$?
 - (A) a
 - (B) $\frac{a}{2}$
 - -
 - (C) 2a
 - (D) a²

The equation of the hyperbola having x + y - 1 = 0and x - y + 2 = 0 as its asymptotes and passing through the origin is :

- (A) x+y-1=2(x-y+2)
- (B) (x+y-1)(x-y+2)+2=0
- (C) (x+y-1)(x-y+2)=0
- (D) (x+y-1)(x-y+2)-2=0

49. The equation $z\overline{z} + (1+i)z + (1-i)\overline{z} = 0$ represents:

- (A) A straight line
- (B) A circle
- (C) An ellipse
- (D) None of these
- 50. If $\sin \phi = i \tan \theta$, then $\cos \theta + i \sin \theta =$

(A)
$$\tan \frac{\phi}{2}$$

(B) $\tan \left(\frac{\pi}{4} - \frac{\phi}{2}\right)$
(C) $\tan \left(\frac{\pi}{4} + \frac{\phi}{2}\right)$
(D) $\tan \phi$

51. The principal value of i' is :

- (A) $e^{\frac{\pi}{2}}$
- (B) $e^{-\frac{\pi}{2}}$
- (C) e^π
- (D) e^{-π}

52. Which of the following is the imaginary part of

 $\sin^{-1}(\cos\theta + i\sin\theta), \ 0 < \theta < \frac{\pi}{2}$?

- (A) $\cos^{-1}\sqrt{\sin\theta}$
- (B) $\sin^{-1}\sqrt{\cos\theta}$

(C) $\log(\sqrt{\sin\theta} + \sqrt{1 + \sin\theta})$

(D) $\log(\sqrt{1+\sin\theta} - \sqrt{\sin\theta})$

[Turn over

53. When $x^4 - 3x^3 + 4x^2 - 6x + 7$ is divided by x - 1, 58. If α , β , γ are the roots of the equation then the remainder is :

- (A) 7
- (B) 6
- (C) 5
- (D) 3
- 54. The equation which increases the roots of the equation $x^3 + 6x^2 + 7x + 2 = 0$ by 2 is :
 - (A) $x^3 5x + 4 = 0$
 - (B) $x^3 4x + 5 = 0$
 - (C) $x^3 6x + 7 = 0$
 - (D) $x^3 7x + 6 = 0$
- 55. The equation whose roots are 2 times the roots of the equation $x^7 - 5x^4 + 13x^2 - 11 = 0$ is :
 - (A) $x^7 10x^4 + 52x^2 88 = 0$
 - (B) $x^7 20x^4 + 52x^2 88 = 0$
 - (C) $x^7 40x^4 + 208x^2 352 = 0$
 - (D) $x^7 40x^4 + 416x^2 1408 = 0$
- 56. For what value of k the roots of the equation $x^{3}-6x+11x+k=0$ are in A.P.?
 - (A) k = 4
 - (B) k = 5
 - (C) k = -6
 - (D) k = 6

57. If x + y + z = 1, $x^2 + y^2 + z^2 = 2$, $x^3 + y^3 + z^3 = 3$, then $x^{5} + y^{5} + z^{5} =$

- (A) 4
- (B) 5
- (C) 6
- (D) 7

 $x^3 + 2x^2 - 3x - 1 = 0$, then the value of

$$\frac{1}{\alpha^3} + \frac{1}{\beta^3} + \frac{1}{\gamma^3}$$
 is:

- (A) 42
- (B) -42
- (C) 24
- (D) -36

59. If $G^2 + 4H^3 < 0$, then the cubic equation $x^{3} + 3Hx + G = 0$ has :

- (A) One real and two conjugate complex roots
- (B) All the three roots real and two of them are equal
- (C) All the three roots real and distinct
- (D) No real roots
- 60. Which of the following is true for any zero 'a' of the polynomial?

 $z^5 + z^4 + z^3 + z^2 + z + 1$?

- (A) |a| < 1
- (B) |a| = 1
- (C) |a| > 1
- (D) None of these

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1. The value of
$$\int_{0}^{\frac{\pi}{6}} \sin^{8} 3\theta d\theta$$
 is :

(A)
$$\frac{3\pi}{16}$$

(B) $\frac{5\pi}{32}$
(C) $\frac{64}{35}$
(D) $\frac{35\pi}{768}$

The order and the degree of the differential 2. equation

$$\left[1 + \left(\frac{dy}{dx}\right)^2\right]^{\frac{3}{2}} = k\frac{d^2y}{dx^2}$$

are respectively :

- (A) 2 and 1
- (B) 1 and 2
- (C) 2 and 2
- (D) 1 and 1
- The solution of the differential equation 3. $ydx - xdy + 3x^2y^2e^{x^3} dx = 0$ is : (A) $x + ye^{x^3} = cy$
 - (B) $y + xe^{x^3} = cx$
 - (C) $x ye^{x^3} = cv$

(D)
$$v - xe^{x^3} = cx$$

The particular integral of the differential equation 4. $(D^3 - 6D^2 + 11D - 6)y = e^{-2x} + e^{-3x}$

is :

(A) $-\frac{1}{120}(e^{-2x}+e^{-3x})$

(B)
$$-\frac{1}{120}(e^{-2x}+3e^{-3x})$$

(C)
$$-\frac{1}{120}(2e^{-2x}+e^{-3x})$$

(D) $\frac{1}{120}(2e^{-2x}+e^{-3x})$

If P and Q are non-singular square matrices of the same order, then adj(PQ) =

- (A) adj(P).adj(Q)
- (B) adj(Q).adj(P)
- (C) |PQ|.I

5.

6.

(D) |PQ|PQ

Which of the following is not true for any non-singular matrix M with transpose M' and inverse M⁻¹?

- (A) |M'| = |M|(B) $M^{-1} = M'$
- (C) $(M^{-1})' = (M')^{-1}$
- (D) Tr(M') = Tr(M)
- 7. If $P = \begin{bmatrix} 2 & -1 \\ -2 & 1 \end{bmatrix}$, then $P^5 =$
 - (A) 3P
 - (B) 9P
 - (C) 27P
 - (D) 81P

 - The rank of the matrix $\begin{bmatrix} 2 & 3 & -1 & -1 \\ 1 & -1 & -2 & -4 \\ 3 & 1 & 3 & -2 \\ 6 & 3 & 0 & -7 \end{bmatrix}$ is :
 - (A) 4 (B) 3

8.

9.

- (C) 5
- (D) 2

The number of linearly independent solutions of the equation x + y + z = 1 is :

- (A) 4
- (B) 3
- (C) 1
- (D) 2

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- 10. Which of the following is not true?
 - (A) The columns of a non-singular matrix are linearly independent
 - (B) The rows of a matrix A of order m×n are linearly dependent iff rank of A is less than m
 - iff its rank is less than n
 - (D) For any matrices of suitable order, $rank(ABC) \le rank(AB)$
- 11. For what values of m and n, the system of equations x + y + z = 6, x + 2y + 3z = 10 and x + 2y + mz = nhave no solution?
 - (A) m = 3, n = 10
 - (B) $m \neq 3, n = 10$
 - (C) $m = 3, n \neq 10$
 - (D) $m \neq 3, n \neq 10$
 - 12. For any orthogonal matrix P:
 - (A) $P^{-1} = P$
 - (B) PP' = P
 - (C) PP' = P'
 - (D) $P^{-1} = P'$

13. For what values of m does the equation 18. $2x^3 - 9x^2 + 12x + m = 0$ have two equal roots ?

- (A) m = -1, -4
- (B) m = -4, -3
- (C) m = -4, -5
- (D) m = -1, -3

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- 14. If α , β , γ are the roots of the equation $x^3 - 6x^2 + 12x - 8 = 0$, then the equation whose roots are $\alpha - 2$, $\beta - 2$, $\gamma - 2$ is :
 - (A) $x^3 + 6x^2 12x + 8 = 0$ (B) $x^3 - 8x^2 + 12x - 6 = 0$ (C) $x^3 = 0$ (D) $x^3 + 6 = 0$
- (C) A square matrix A of order n is non-singular 15. If α , β , γ are the roots of the equation $x^3 - x^2 + 8x - 6 = 0$, then the equation whose roots are α^2 , β^2 , γ^2 is :
 - (A) $x^3 + 15x^2 + 52x 36 = 0$
 - (B) $x^3 15x^2 52x + 36 = 0$
 - (C) $x^3 15x^2 + 52x 36 = 0$
 - (D) $x^3 + 15x^2 52x + 36 = 0$
 - 16. The condition that the roots of the equation $x^3 - px^2 + qx - r = 0$ may be in G.P. is :
 - (A) pq = r
 - (B) pr = q
 - (C) $2p^3 9pq + 27r = 0$
 - (D) $p^3r = q^3$

17. If α , β , γ are the roots of the equation

 $x^{3} + 2x^{2} - 3x - 1 = 0$, then $\frac{1}{\alpha^{2}} + \frac{1}{\beta^{2}} + \frac{1}{\gamma^{2}} =$

- (A) 41
- (B) 42
- (C) -52
- (D) 23

The number of imaginary roots of the equation $x^{7} - 3x^{4} + 2x^{3} - 1 = 0$ is at least :

- (A) 2 (B) 3
- (C) 4
- (D) 5

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Turn over

- 19. Which of the following is true for any root 'a' of 23. Which of the following series is not convergent? the equation $z^4 + z^2 + 1 = 0$?
 - (A) |a| = 1
 - (B) |a| < 1
 - (C) |a| > 1
 - (D) None of these
- 20. The sum of the cubes of the roots of the equation $x^3 6x^2 + 11x 6 = 0$ is :
 - (A) 6
 - (B) 11
 - (C) 36
 - (D) 121
- 21. Which of the following is not true?
 - (A) If A and B are countable sets, then A ∪ B is also a countable set
 - (B) If A is a countable set, then every subset of A is also countable
 - (C) If A is an uncountable set, then every subset of A is also uncountable
 - (D) If A and B are countable sets, then so is their Cartesian product
- 22. Which of the following is not true for any two bounded sequences {a_n} and {b_n} of non-negative real numbers ?
 - (A) $\underline{\lim}(a_n b_n) \leq \underline{\lim}(a_n).\underline{\lim}(b_n)$
 - (B) $\underline{\lim}a_n.\overline{\lim}b_n \leq \overline{\lim}(a_nb_n)$
 - (C) $\overline{\lim}(a_n b_n) \le \overline{\lim} a_n ... \overline{\lim} b_n$
 - (D) $\underline{\lim}(a_n b_n) \leq \underline{\lim} a_n . \underline{\lim} b_n$

(A) $\sum_{n=1}^{\infty} \frac{1}{n^{1+\frac{1}{n}}}$ (B) $\sum_{n=0}^{\infty} \{(n^3+1)^{\frac{1}{3}}-n\}$ (C) $\sum_{n=0}^{\infty} \frac{\sqrt{n+1}-\sqrt{n-1}}{n}$ (D) $\sum_{n=1}^{\infty} \frac{\sin \frac{1}{n^2}}{n^2}$

24. The series $\sum_{n=1}^{\infty}$

$$\frac{1^2 \cdot \cdot \cdot \cdot \cdot (2n-1)^2}{2^2 \cdot \cdot \cdot \cdot (2n)^2} x^{n-1}, x > 0$$

converges for :

- (A) x > 1
- (B) x = 1
- (C) x < 1
- (D) None of these

25. The value of
$$\int_0^4 [x] dx$$
 is :

- (A) 4
- (B) 8
- (C) 6
- (D) 17

26. Which of the following is true for the function

f(x) = x, when x is rational

= -x, when x is irrational

on [0, 1]?

00

- (A) f is integrable, but |f| is not integrable
- (B) |f| is integrable, but f is not integrable
- (C) f and |f| are both integrable
- (D) Neither f nor |f| is integrable

FDM-2553-B

- 27. Which of the following is true for any two bounded and integrable functions f and g on [a, b]?
 - (A) f+g is integrable
 - (B) f-g is integrable
 - (C) f.g is integrable

(D) $\frac{f}{g}$ is integrable

- 28. Which of the following is not true for any refinement P* of a partition P of [a, b] and any bounded function f defined on [a, b]?
 - (A) $L(P, f) \leq L(P^*, f)$
 - (B) $U(P, f) \le U(P^*, f)$
 - (C) $L(P^*, f) \le U(P^*, f)$
 - (D) $U(P^*, f) \le U(P, f)$
- 29. What is the value of $\Gamma\left(\frac{5}{2}\right)$?
 - (A) $3\sqrt{\pi}$
 - (B) $3\frac{\sqrt{\pi}}{4}$
 - (C) $3\frac{\sqrt{\pi}}{2}$

(D)
$$\frac{\sqrt{\pi}}{2}$$

30. The value of $\iint_{A} e^{x+y+z} dx dy dz$, where 34. $A = \{(x, y, z), 0 \le x \le 1, 0 \le y \le 1, 0 \le z \le 1\}$ is :

- $(A) e^2$
- (B) e^{3}
- (C) $(e-1)^2$
- (D) $(e-1)^3$

FDM-2553-B

31. The value of $\iint_{A} \frac{dxdy}{\sqrt{(1-x^2)(1-y^2)}}, \text{ where}$ $A = \{(x, y), 0 \le x \le 1, 0 \le y \le 1\}, \text{ is :}$

(A) $\frac{\pi^2}{4}$ (B) $\frac{\pi^2}{2}$ (C) $\frac{\pi^2}{3}$

(D) $\frac{\pi^2}{8}$

- 32. If $r = \sqrt{x^2 + y^2 + z^2}$, then $\nabla^2(r^n) =$
 - (A) nr^{n-2}
 - (B) $(n+1)r^{n-2}$
 - (C) $n(n+1)r^{n-1}$
 - (D) $n(n+1)r^{n-2}$
- 33. Which of the following is not true?
 - (A) Every group is a subgroup of itself
 - (B) Every group has exactly two improper subgroups
 - (C) Every cyclic group is abelian
 - (D) Every group of prime order is simple

Which of the following functions from R to R is a permutation of R?

- (A) f(x) = x + 1
- (B) $g(x) = x^2$
- (C) $h(x) = e^x$

5

(D) None of these

[Turn over

0 - 9 8 (8)

- 35. Which of the following is not a homomorphism? 38.
 - (A) $\phi: F \rightarrow R$ defined by $\phi(f) = 3f, f \in F$, where F is the additive group of all functions mapping R into R and R is the additive group of all real numbers
 - (B) $\phi: M_n \to R$ defined by $\phi(A) = Tr(A), A \in M_n$, where M_n is the additive group of all $n \times n$ matrices with real entries and R is the additive group of all real numbers

(C)
$$\phi: F \to R^*$$
 defined by $\phi(f) = \int_0^1 f(x) dx, f \in F$,

where F is the multiplicative group of all continuous functions from R into R that are non-zero at every $x \in R$ and R^{*} is the multiplicative group of all non-zero real numbers

- (D) \$\phi: R* → R*\$ defined by \$\phi(x) = |x|, x ∈ R*\$, where R* is the multiplicative group of all non-zero real numbers
- 36. Which of the following is a sufficient condition for a ring R to be commutative ?
 - (A) $a^2 = a, \forall a \in \mathbb{R}$
 - (B) $a^3 = a, \forall a \in \mathbb{R}$
 - (C) Both (A) and (B)
 - (D) Neither (A) nor (B)
- 37. Which of the following is/are true in a vector space V over the field F?
 - (A) $ax = 0_v \Rightarrow a = 0_r \text{ or } x = 0_v$
 - (B) $a.0_v = 0_v$
 - (C) $0_{\rm F} = 0_{\rm V}$
 - (D) All of these

FDM-2553-B

If P and Q are subspaces of a vector space V_F , which of the following is not a subspace of V_F ?

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- (A) $P \cap Q$
- (B) $P \cup Q$
- (C) P+Q
- (D) aP + bQ, $a, b \in F$
- 39. The dimension of the vector space C of complex numbers over the field R of real numbers is :
 - (A) 1
 - (B) 2
 - (C) 3
 - (D) None of these
- 40. If V_F is a finite-dimensional vector space of dimension n and k is the kernel of a homomorphism from V_F onto F_F , then the

dimension of the quotient space $\frac{V}{K}$ is equal to :

- (A) 0
- **(B)** 1
- (C) n
- (D) None of these

41. If
$$f(x) \rightarrow 0$$
 as $x \rightarrow 0$, then $\lim_{x \rightarrow 0} \frac{e^{f(x)} - 1}{f(x)}$

(D) -1

42. Which of the following is a point of discontinuity 45. of the second kind of the function

The angle of intersection of the curves $r = a \cos \theta$ and $r = a(1 - \cos \theta)$ is :

f(x) = 1, x = 0(A) $\frac{\pi}{3}$ $= x + \frac{1}{2}, 0 < x < \frac{1}{2}$ (B) $\frac{2\pi}{3}$ $=\frac{1}{2}, x = \frac{1}{2}$ (C) $\frac{3\pi}{2}$ $=x+\frac{1}{2}, \frac{1}{2} \le x < 1$ (D) $\frac{5\pi}{6}$ = 0, x = 1?(A) x = 0(B) $x = \frac{1}{2}$ (C) x = 1(D) None of these 43. The coefficient of $\left(x-\frac{\pi}{2}\right)^4$, when sin x is expanded as a Taylor series in $\left(x - \frac{\pi}{2}\right)$, is : (A) 1 (B) $-\frac{1}{2}$ (C) $\frac{1}{24}$ is : (D) $\frac{1}{720}$ (A) ab 44. If $2y = x(1 + y_1)$, then $y_3 =$ (B) $\frac{b^2}{a}$ (A) $x^2 + y^2$ (C) $\frac{a^2}{b}$ (B) $x^2 - y^2$ (C) 0(D) $\frac{a}{b}$ (D) x + y7 FDM-2553-B

46. Which of the following is true for the function $u = \sin^{-1} \left(\frac{\sqrt{x} - \sqrt{y}}{\sqrt{x} + \sqrt{y}} \right) ?$ (A) $\frac{\partial u}{\partial x} = -\frac{\partial u}{\partial y}$ (B) $\frac{\partial u}{\partial x} = -\frac{x}{y} \frac{\partial u}{\partial y}$ (C) $\frac{\partial u}{\partial x} = -\frac{y}{x} \frac{\partial u}{\partial y}$ (D) $\frac{\partial u}{\partial x} = -xy \frac{\partial u}{\partial y}$ 47. The maximum value of the radius of curvature of

47. The maximum value of the radius of curvature of the ellipse

 $p^2 = a^2 \cos^2 \psi + b^2 \sin^2 \psi$

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48. Which of the following is not an asymptote of the 52. $sin(log i^i) =$ curve $x^{3}+2x^{2}y-xy^{2}-2y^{3}+4y^{2}+2xy+y-1=0$? (A) 1 (A) y = x + 1(B) 0 (B) y = -x + 1(C) -1 (C) $y = -\frac{1}{2}x$ (D) i 53. If the point (α, β) lies outside the parabola (D) x + y = 0 $y^2 = 4ax$, then $\beta^2 - 4a\alpha$ is : 49. The equation |z + 1| + |z - 1| = 4 represents in the z-plane : (A) Zero (A) A circle (B) Positive (B) An ellipse (C) Negative (C) A square (D) None of these (D) A rectangle 54. The eccentricity of the ellipse 50. If $x_r = \cos \frac{\pi}{2^r} + i \sin \frac{\pi}{2^r}$, r = 1, 2, 3,...., then $4x^2 + y^2 - 8x + 2y + 1 = 0$ $\prod_{r=1}^{\infty} X_r =$ is : (A) $\sqrt{3}$ (A) 1 (B) $\frac{\sqrt{3}}{2}$ (B) $\frac{\pi}{2}$ (C) π (C) $2\sqrt{3}$ (D) -1 51. If $x + iy = \cosh(u + iv)$, then : (D) $\frac{2}{\sqrt{3}}$ (A) $\frac{x^2}{\cosh^2 u} + \frac{y^2}{\sinh^2 u} = 1$ 55. The line lx + my + n = 0 will touch the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ if: (B) $\frac{x^2}{\cosh^2 u} - \frac{y^2}{\sinh^2 u} = 1$ (A) $a^2l^2+b^2m^2=n^2$ (C) $\frac{x^2}{\sinh^2 u} + \frac{y^2}{\cosh^2 u} = 1$ (B) $al^2 + bm^2 = n^2$ (C) $l^2 + m^2 = n^2$ (D) $\frac{x^2}{\sinh^2 y} - \frac{y^2}{\cosh^2 y} = 1$ (D) $a^2l^2 - b^2m^2 = n^2$

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56. The center of the conic

 $21x^2 - 6xy + 29y^2 + 6x - 58y - 151 = 0$

is :

- (A) (1, 0)
- (B) (0, 0)
- (C) (0, 1)
- (D) (1, 1)
- 57. The radius of the circle in which the plane x+2y-z = 4 cuts the sphere $x^2+y^2+z^2-x+z-2 = 0$ is :

(A)
$$\frac{3}{\sqrt{6}}$$

(B)
$$\sqrt{\frac{5}{2}}$$

- (C) 3
- (D) 1
- 58. The semi-vertical angle of the right circular cone having its vertex at the origin and passing through the circle $x^2 + z^2 = 25$, y = 4 is :
 - (A) $\tan^{-1}\left(\frac{5}{4}\right)$
 - (B) $\tan^{-1}\left(\frac{4}{5}\right)$
 - (C) $\tan^{-1}(5)$
 - (D) $\tan^{-1}(4)$

- 59. The locus of the tangent lines to a sphere which are parallel to a given line is :
 - (A) A sphere
 - (B) A cone
 - (C) A cylinder
 - (D) None of these
- 60. The surface represented by $\frac{x^2}{2} \frac{y^2}{3} = z$ is :
 - (A) An elliptic paraboloid
 - (B) A hyperbolic paraboloid
 - (C) A hyperboloid of one sheet
 - (D) A hyperboloid of two sheets

FDM-2553-B

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| | ENTRANCE ' | TEST-2017 |
| | SCHOOL OF DIIVSICAL AND M | ATHEMATICAL SCIENCES |
| | SCHOOL OF PHYSICAL AND M | ATICS |
| | | Question Booklet Series A |
| 'ime A | Juestions : 60 Jowed : 70 Minutes | Roll No. : |
| | | |
| 1. | Instructions for C Write your Roll Number in the space provided at th necessary information in the spaces provided on the C | andidates : e top of this page of Question Booklet and fill up the OMR Answer Sheet. |
| 2. | OMR Answer Sheet has an Original Copy and a Cand entries in the Original Copy, candidate should ensur- entries made in the Original Copy against each item a | lidate's Copy glued beneath it at the top. While making re that the two copies are aligned properly so that the are exactly copied in the Candidate's Copy. |
| 3. | All entries in the OMR Answer Sheet, including answer only. | ers to questions, are to be recorded in the Original Cop |
| 4. | Choose the correct / most appropriate response for darken the circle of the appropriate response comple- read by the OMR Scanner and no complaint to this e | each question among the options A, B, C and D an etely. The incomplete darkened circle is not correctl ffect shall be entertained. |
| 5. | Use only blue/black ball point pen to darken the cir gel/ink pen or pencil should be used. | rcle of correct/most appropriate response. In no cas |
| 6. | Do not darken more than one circle of options for an response shall be considered wrong. | ny question. A question with more than one darkene |
| 7. | There will be 'Negative Marking' for wrong answe 0.25 marks from the total score of the candidate. | ers. Each wrong answer will lead to the deduction of |
| 8. | Only those candidates who would obtain positive sc admission. | core in Entrance Test Examination shall be eligible for |
| 9. | Do not make any stray mark on the OMR sheet. | |
| 10. | . Calculators and mobiles shall not be permitted inside | the examination hall. |
| 11. | Rough work, if any, should be done on the blank she | ets provided with the question booklet. |
| . 12. | OMR Answer sheet must be handled carefully and it so be evaluated. | hould not be folded or mutilated in which case it will no |
| 13. | . Ensure that your OMR Answer Sheet has been signed | d by the Invigilator and the candidate himself/herself. |
| 14. | At the end of the examination, hand over the OMRA original OMR sheet in presence of the Candidate an | nswer Sheet to the invigilator who will first tear off th d hand over the Candidate's Copy to the candidate. |
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Which of the following are the points of discontinuity of the function f(x) in the interval [0, 1] where

- f(x) = 2, when x = 0 = $4x^2 + 1$, $0 < x < \frac{1}{2}$
 - $= 2x + 1, \frac{1}{2} \le x \le 1$?
- (A) x = 0 and $x = \frac{1}{2}$ only
- (B) $x = \frac{1}{2}$ only
- (C) x = 0 only
- (D) None of the above
- 2. What is the coefficient of x^2 in the power series expansion of $log(1 + e^x)$?
 - (A) $\frac{1}{8}$

1.

- (B) $\frac{1}{4}$
- (C) 2
- (D) None of the above
- 3. Which of the following is the kth derivative of the function y = SinxCosx ?
 - (A) $y_k = 2^k \operatorname{Sin}(x + k\pi)$
 - (B) $y_k = 2^k \cos(x + k\pi)$
 - (C) $y_k = 2^{k-1} \cos\left(2x + \frac{k\pi}{2}\right)$
 - (D) $y_k = 2^{k-1} \operatorname{Sin}\left(2x + \frac{k\pi}{2}\right)$
- 4. What is value of $\lim_{x \to 0} \frac{\sin x x + 2x^3}{x^3}$? (A) 2
 - (B) $\frac{13}{6}$
 - (C) $\frac{5}{3}$
 - (D) $\frac{11}{6}$

DAJ-11119-A

If S is the length of an arc of the curve f(r, Q) = 0, then which of the following is true ?

(A)
$$\left(\frac{dS}{dQ}\right)^2 = 1 + \left(\frac{dQ}{dr}\right)^2$$

(B) $\int \left(\frac{dS}{dQ}\right)^2 = 1 + r^2 \left(\frac{dr}{dQ}\right)^2$
 $\left(\frac{dS}{dQ}\right)^2 = \left(\frac{dr}{dQ}\right)^2$

C)
$$\left(\frac{\mathrm{dS}}{\mathrm{dQ}}\right)^2 = \mathrm{r}^2 \left(\frac{\mathrm{dr}}{\mathrm{dQ}}\right)^2$$

(D) None of the above

If
$$u = \sin^{-1}\left(\frac{x^2 + y^2}{x + y}\right)$$
,

then for which of the following value of f(u),

$$x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} = f(u) ?$$

(A) sin u

5.

6.

- (B) tan u
- (C) $\frac{1}{2} \sin 2u$
- (D) ¹/₂ tan 2u
- 7. How many asymptotes does the curve $y^2 = \theta x$ have ?
 - (A) None
 - (B) One
 - (C) Two
 - (D) More than two

8. How many double points are on the curve ?

$$x^4 + y^3 + 2x^3 + 3y^2 = 0$$
?

- (A) Four
- (B) Three
- (C) Two
- (D) One

2

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Let
$$Z_1$$
 and Z_2 be two complex numbers, then

$$|Z_1 + Z_2|^2 = |Z_1|^2 + |Z_2|^2$$

if and only if

9.

(A) $Z_1 - Z_2$ is purely imaginary

(B)
$$\frac{Z_1}{Z_2}$$
 is purely imaginary

(C)
$$\frac{Z_1}{Z_2}$$
 is purely real

(D) None of the above

10. Which of the following is the value of $(1 + \omega)^3$ where :

$$\omega = \left(\cos\frac{2\pi}{3} + i\sin\frac{2\pi}{3}\right)?$$

- (A) -i
- (B) i
- (C) -1
- (D) 1

11. Which of the following is the real part of $\cos^{-1}(i)$?

- (A) $\frac{\pi}{2}$
- (B) $\frac{1}{4}$
- (C) π
- (D) None of the above
- 12. What is the sum to n terms of the series $\cos \theta + \cos 3\theta + \cos 5\theta + \dots$?

(A)
$$\frac{\cos 2n\theta}{2\sin \theta}$$

(B)
$$\frac{\sin 2n\theta}{2\sin \theta}$$

(C)
$$\frac{\cos n\theta}{\sin \theta}$$

(D)
$$\frac{\sin n\theta}{\cos \theta}$$

13. For what value of k, the line y = 3x + k touches the parabola $y^2 = 2x$? (A) $\frac{2}{3}$ (B) $\frac{3}{2}$ (C) $\frac{5}{6}$

- (D) None of the above
- 14. If CP is an equi-conjugate semi-diameter of an ellipse

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1,$$

then which of the following is the length of CP?

- (A) $\frac{a+b}{2}$ (B) $\frac{ab}{2}$ (C) $\sqrt{\frac{a^2+b^2}{2}}$ (D) $\sqrt{a^2+b^2}$
- 15. If a circle and the rectangular hyperbola $xy = c^2$ mee in the four points k_1, k_2, k_3, k_4 , then what is the valu of the product $k_1k_2k_3k_4$?
 - (A) c^4
 - **(B)** 1
 - (C) 2
 - (D) None of the above

16. Which of the following is the centre of the conic

$$x^2 - 5xy + y^2 + 8x - 12y + 15 = 0?$$

$$(A) (-4, 0)$$

(B) (0,4)

3

- (C) $\left(-4, -\frac{16}{3}\right)$
- (D) None of the above

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17. For what value of the constant k, the two spheres $x^2 + y^2 + z^2 + 6y + 2z + 1$

$$x^{2} + y^{2} + z^{2} + 6y + 2z + k = 0$$
 and
 $x^{2} + y^{2} + z^{2} + 6x + 8y + 4z + 20 = 0$?

- (A) -6
- (B) 4
- (C) · 8
- (D) None of the above
- 18. What is the general equation of the cone of second degree which possess through the axes ?
 - (A) $ax^2 + by^2 + cz^2 = 0$
 - (B) fyz + gzx + hxy = 0
 - (C) $ax^2 + by^2 + cz^2 = xy + yz + zx$
 - (D) None of the above
- 19. Which of the following is the equation of cylinder which intersects the curve

 $x^2 + y^2 + z^2 = 1$, ux + vy + wz = d

- and whose generator are parallel to the axis of x?
- (A) $ux^2 + vy^2 + wz^2 = 1$
- (B) $(u + v)x^2 + (v + w)y^2 + (w + u)z^2 = d$
- $(C) \quad u^2xy + v^2yz + w^2zx = d$
- (D) None of the above
- 20. Tangent planes are drawn to the conicoid $ax^2 + by^2 + cz^2 = 1$ through the point (α , β , γ), then the perpendiculars to them from origin generate the conc. :

(A)
$$(\alpha x + \beta y + \gamma z)^2 = \left(\frac{x^2}{a} + \frac{y^2}{b} + \frac{z^2}{c}\right)$$

- (B) $(axy + byz + czx)^2 = 1$
- (C) $(ax + by + cz)^2 = (\alpha xy + \beta yz + \gamma zx)^2$
- (D) None of the above
- 21. For which of the following values of $\psi(x)$,

$$\int \tan^5 x \, dx - \frac{\tan^4 x}{4} = \psi(x) ?$$

(A) $\log \sec x + \tan^2 x$

(B) $\log \sec x - \frac{1}{2} \tan^2 x$

(C) $x - \tan x$

(D) $\tan^2 x - \log \sec x$

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22. Which of the following is the value of

$$\frac{1}{(D-2)^2} (x^3) ?$$
(A) $x^3 - 3x^2 + 9x - 3$
(B) $\frac{1}{8} (2x^3 + 3x^2 - 9x + 8)$
(C) $\frac{1}{8} (2x^3 + 6x + 9x + 6)$
D) None of the above

23. Which of the following is the solution of differential equation

$$y = 2px + y^2p^3$$

$$(A) \quad y^2 = cx + \frac{c^3}{8}$$

$$(B) \quad y = 2cx + c^3y^2$$

(C)
$$y = 2cx^2 + c^3$$

- (D) None of the above
- 24. Let $P_n(x)$ denote the Legendre polynomials for n = 0, 1, 2, ..., then for which of following values of the pair (k, ℓ)

$$(2n+1) x P_n(x) = k P_{n+1}(x) + \ell P_{n-1}(x) ?$$

- (A) (2n-1, 2n+1)
- (B) (n-1, n+1)

(C)
$$(n, n-1)$$

(D) (n+1, n)

25. For what value of the pair (m, n), the matrix

$$2m\begin{bmatrix} -1 & 1 & -1 \\ 8 & -6 & 2 \\ -5 & n & -1 \end{bmatrix}$$

is the inverse of the matrix

| | | 0 | 1 | 2] | |
|-----|----|------|-----|----|---|
| | | 1 | 2 | 3 | ? |
| | | 3 | 1 | 1 | |
| (A) | (| 3,1 | ; | | |
| (B) | (| 1,3 |) | | |
| (C) | (| - 1, | 3) | | |
| (D) | (- | - 1. | -3) | | |

26. Let
$$A = \begin{bmatrix} 2 & -1 \\ -2 & 1 \end{bmatrix}$$
,

then for what value of the integer k, $A^{10} = 3^k A$?

- 9 (A)
- 6 (B)
- 3 (C)
- None of the above (D)

What is the rank of the matrix 27.

| - | 1 | 3 | 2 | 1] |
|--------------|---|---|----|----|
| | 3 | 1 | 4 | 2 |
| State No. 10 | 5 | 7 | 8 | 4 |
| | 7 | 5 | 10 | 5 |

- (A) One
- (B) Two
- Three (C)
- (D) Four
- For which value of P, the vectors 28.

| [7] | | 2 | | 8 | |
|-----|---|---|---|---|--|
| 4 | , | 1 | , | P | |
| 6 | | 3 | | 3 | |

are linearly dependent?

- (A) 8
- 7 (B)
- 6 (C)
- (D) 5

29. Let $A = [a_{ij}]_{5 \times 4}$ be a matrix of order 5 × 4, then the columns of A are linearly independent if and only if :

- R(A) = 4(A)
- R(A) = 5(B)
- R(A) < 4(C)
- None of the above (D)

How many linearly independent solutions does the 30. of equations

x + y - 4z - 2u = 0, 2x - 3y + 2z + 2u = 0have ? (A) 4 (B) 3 2 (C) (D) None Let A be a matrix of order 3×5 with rank of A 31.

- Then how many linearly independent solutions the system of non-linear homogeneous equ $AX = H, H \neq 0$, have ?
 - (A) 4
 - 3 **(B)**
 - 2 (C)

32.

- None of the above (D)
- For which value of the pair (α , β), the matrix $\begin{bmatrix} \frac{1}{\sqrt{3}} & 0 & \alpha \\ -\frac{1}{\sqrt{3}} & \beta & \frac{1}{\sqrt{6}} \\ \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{6}} \end{bmatrix}$

is an orthogonal matrix ?

- (A) $\left(\frac{2}{\sqrt{6}}, \frac{1}{\sqrt{2}}\right)$ (B) $\left(\frac{1}{\sqrt{6}}, -\frac{1}{\sqrt{3}}\right)$ (C) $\left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{6}}\right)$
- None of the above (D)

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| 33. | If α, β | , γ are the roots of the equation | 1.1 |
|-----|---------|--|-----|
| | | $x^3 + 9x^2 + 23x + 15 = 0,$ | |
| | then w | hich of the following is the value of | |
| | | $1 + \frac{1}{1} + \frac{1}{2}$ | |
| | | $\frac{1}{\alpha\beta} + \frac{1}{\beta\gamma} + \frac{1}{\gamma\alpha}$ | |
| | (A) | 5 | |
| | | 23 | |
| | (B) | 15 | |
| | A.C. | | |
| | (C) | 4 | |
| | | 1 me manifestive transfer ward and I | |
| | (D) | 5 | |
| 34. | The | roots of the equation | |
| | | $28x^3 + 39x^2 + 12x - 1 = 0$ | |
| | are in | Harmonic progression. Which of the following | |
| • | is its | mean root ? | |
| | (A) | 4 | |
| | | 1 | |
| | (D) | 4 | |
| | | | |
| | (C) | 7 | |
| | (D) | None of the above | |
| 35 | . Whi | ch of the following is the equation whose roots | • |
| | are | less than 2 than that of the equation | |
| | | $x^3 + 4x^2 + 7x + 8 = 0$? | |
| | (A) | $y^3 + 10y^2 - 35y + 36 = 0$ | |
| | (B) | $y^3 - 10y^2 + 35y - 30 = 0$ | |
| | (C) | $y^3 + 6y^2 + 3y + 30 = 0$ | |
| | (D) | $y^3 + 10y^2 + 35y + 40 = 0$ | s |
| 36 | 5. Wh | the squares of the roots of the equation | |
| | are | $x^{3} - 2x^{2} - x + 2 = 0$? | |
| | (1) | $y^{3} + 6y^{2} + 9y + 4 = 0$ | |
| | (A) | $y^3 + 9y^2 - 6y + 4 = 0$ | |
| | | $y^3 - 6y^2 + 9y - 4 = 0$ | |
| | (C) |) None of the above | |
| | | | |

- What is the value of $S_3 = \alpha^3 + \beta^3 + \gamma^3$ where α , β , γ 37. are the roots of the equation
 - $x^3 x^2 + 1 = 0$?
 - (A) 4
 - 3 (B)
 - -2 (C)
 - None of the above (D)

The cubic equation 38.

$$x^3 + 3x + 14 = 0$$

has:

- All the three roots real and distinct (A)
- One real and two conjugate imaginary roots (B)
- All the three roots not only real but two of them (C) are also equal
- None of the above (D)

The equation 39.

$$x^4 - 5x^3 + 7x^2 - 5x + 6 = 0$$

has:

- no negative root (A)
- at least one negative root (B)
- at least two negative roots (C)
- None of the above (D)

How many roots does the polynomial equation : 40.

$$4z^6 - 3z^5 + 3z^4 - 2z^3 + 2z^2 - 2z + 1 = 0$$

have within and on the circle $|z| \le 1$?

- (A) None
- Two **(B)**
- (C) Four
- Six (D)
- Which of the following statements are true ? 41.
 - The set of all integers is countable and set of (A) all polynomial functions P_n with integer coefficients is countable
 - The set of all integers is countable but set of all **(B)** polynomial functions P_n with integer coefficients is not countable
 - The set of all integers is not countable but se (C) of all polynomial functions P_n with intege coefficients is countable
 - None of the above (D)

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42. How many limit points does the sequence $\{s_n\}$ where

$$\mathbf{S}_{n} = (-1)^{n} \left\{ \left(1 + \frac{1}{n} \right) \right\}, n \in \mathbb{N}$$

have ?

- (A) None
- (B) One
- (C) Two
- (D) More than two

43. Consider the series $\sum \frac{1}{n^{3k}}$, then which of the following is true?

- (A) The series converges for $k < \frac{1}{3}$
- (B) The series converges for $0 < k < \frac{1}{3}$
- (C) The series diverges for $k > \frac{1}{3}$
- (D) The series diverges for $k \le \frac{1}{3}$
- 44. Let $f(x) = x^2$, $g(x) = \frac{1}{x}$ and I = [-1, 1], then
 - (A) f(x) and g(x) are both uniformly continuous on I
 - (B) f(x) is uniformly continuous on I but g(x) is not uniformly continuous on I
 - (C) f(x) and g(x) are not both uniformly continuous on I
 - (D) f(x) is not uniformly continuous on I but g(x) is uniformly continuous on I

45. Consider the function

$$f(x) = \begin{cases} 0 & \text{when } x \text{ is rational} \\ 1 & \text{when } x \text{ is irrational} \end{cases}$$

over the interval [-1, 2]. If U(P, f) is the upper Riemann sum of f relative to a partition P, then U(P, f) =

- (A) 2
- (B) 3
- (C) 0

(D) None of these



46. Consider the two functions
$$f(x)$$
 and $g(x)$ defined by

$$f(x) = \begin{cases} 3 & \text{when } x \neq 0 \\ 0 & \text{when } x = 0 \end{cases}$$

$$g(x) = \begin{cases} 0 & \text{when } x \text{ irrational or zero} \\ \frac{1}{q} & \text{when } x = p/q \text{ is a non-zero rational} \\ & \text{number and} \frac{p}{q} \text{ in lowest form} \end{cases}$$

over the interval I = [0, 1]. Then which of the following is true ?

- (A) f(x) and g(x) are both integrable on I
- (B) f(x) is integrable on I but g(x) is not integrable on I
- (C) f(x) and g(x) both are not integrable on I
- (D) None of the above

$$\int_0^4 [x] dx ?$$

- (A) 8
- (B) 4
- (C) 6
- (D) None of the above

48. If a function f(x) is continuous on [2, 5], then there exists a point 'c' in [2, 5] such that

$$\int_{2}^{5} f(x) dx =$$
3c

(B) cf(2)

(A)

- (C) cf(5)
- (D) 3f(c)



49.

For what value of k, the function f(x, y) defined by

$$f(x, y) = \begin{cases} \frac{xy^{k}}{x^{2} + y^{2k}} & , (x, y) \neq (0, 0) \\ 0 & , (x, y) = (0, 0) \end{cases}$$

is continuous at (0, 0)?

- (A) k = 1
- (B) k = 2
- (C) k = 3
- (D) None of these
- 50. If $xyz = t_1t_2t_3$, what is the minimum value of $t_2t_3x + t_3t_1y + t_1t_2z$? (A) $t_1 + t_2 + t_3$
 - (B) $3t_1t_2t_3$
 - (C) $t_1 t_2 t_3$
 - (D) None of the above
- 51. If $\beta(m, n)$ denotes the beta function, which of the

following is the value of $\beta\left(\frac{3}{2},\frac{1}{2}\right)$?

(A) $\frac{\pi}{2}$

- (B) $\frac{\pi}{3}$
- (C) $\frac{\pi}{4}$

(D) None of the above

52. What is the value of the double integral

 $\iint_{R} (x^{2} + y^{2}) dx dy$

where R is the region defined by $R = \{(x, y) : 0 \le x \le y \le 1\}$? (A) 1

above

(B) $\frac{2}{3}$

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53. Let G be a group of all 2 × 2 non-singular matrices over the real numbers, then which of the following represent a member Z(G), the centre of G ?

(A)
$$\begin{bmatrix} a & a \\ a & 0 \end{bmatrix}$$

(B)
$$\begin{bmatrix} a & 0 \\ 0 & a \end{bmatrix}$$

(C)
$$\begin{bmatrix} 0 & a \\ a & 0 \end{bmatrix}$$

- (D) None of the above
- 54. Let G be a finite group with order O(G). If N is a normal sub-group of G, then which of the following is true ?

(A)
$$O\left(\frac{G}{N}\right) = O(G) - O(N)$$

(B) $O\left(\frac{G}{N}\right) = O(G).O(N)$
(C) $O\left(\frac{G}{N}\right) = \frac{O(G)}{O(N)}$
(D) $O\left(\frac{G}{N}\right) = O(G) + O(N)$

- 55. If $a = (1 \ 2 \ 3 \ 5)$ and $b = (1 \ 5 \ 7 \ 9)$, then which of the following is equal to $a^{-1}ba$? Where $(f_{\circ}g)(x) = f(g(x))$
 - (A) (3795)
 - (B) (5793)
 - (C) (12789)

8

(D) None of the above

56. For which of the following value of k,

$$Z_k = \{0, 1, 2, \dots, k-1\},\$$

the ring of integers mod k, is a field?

- (A) 256
- (B) 961
- (C) 1147
- (D) None of the above
- 57. Let operation of addition and scalar multiplication in $V = \{(a, b) : a, b \in R\}$

be defined as follows :

- (I) (a, b) + (c, d) = (0, b + d) and k(a, b) = (0, kb)
- (II) (a, b) + (c, d) = (a + c, b + d) and k(a, b) = (0, kb).

Then which of the following is true?

- (A) V is a vector space over R with respect to operation defined by (I)
- (B) V is the vector space over R with respect to operation defined by (II)
- (C) V is not a vector space with respect to operations defined by (I) and (II)
- (D) None of the above

- 58. If W_1 and W_2 are two sub spaces of a finite dimensional vector space V, then $\dim(W_1 \cap W_2) =$
 - (A) $\dim(W_1) + \dim(W_2)$
 - (B) $\dim(W_1) + \dim(W_2) \dim(W_1 + W_2)$
 - (C) $\dim(W_1) \dim(W_2)$
 - (D) $\dim(W_1)/\dim(W_2)$
- 59. If S and T are non-empty subsets of a vector space V and L(S) is the linear span of S, then which of the following is true ?
 - (A) L(S) is a sub space of V and $L(S) \subset L(T)$ if $S \subset T$
 - (B) L(S) is a sub space of V and $L(S) \supset L(T)$ if $S \subset T$
 - (C) L(S) is a not a sub space of V
 - (D) None of the above
- 60. Given two vector spaces V and W over field F, let Hom(V, W) be the set of all vector space homomorphisms of V into W. If dim(V) = 19 and dim(W) = 21, then what is the dim Hom(V, W) ?
 - (A) 40
 - (B) 19
 - (C) 21
 - (D) None of the above

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| ENTRANC | E TEST-2016 |
| FACULTY OF PHYSICAL | & MATERIAL SCIENCES |
| M.A./M.Sc. M | ATHEMATICS |
| otal Questions : 60 | Question Booklet Series |
| ime Allowed : 70 Minutes | Roll No. : |
| 1. Write your Roll Number in the space provided necessary information in the spaces provided on | or Candidates : at the top of this page of Question Booklet and fill up th the OMR Answer Sheet. |
| 2. OMR Answer Sheet has an Original Copy and a C entries in the Original Copy, candidate should e entries made in the Original Copy against each ite | Candidate's Copy glued beneath it at the top. While making nsure that the two copies are aligned properly so that the em are exactly copied in the Candidate's Conv. |
| 3. All entries in the OMR Answer Sheet, including an only. | iswers to questions, are to be recorded in the Original Copy |
| 4. Choose the correct / most appropriate response darken the circle of the appropriate response con read by the OMR Scanner and no complaint to this | for each question among the options A, B, C and D and ppletely. The incomplete darkened circle is not correctly s effect shall be entertained |
| 5. Use only blue/black ball point pen to darken the gel/ink pen or pencil should be used. | circle of correct/most appropriate response. In no case |
| 6. Do not darken more than one circle of options fo response shall be considered wrong. | r any question. A question with more than one darkened |
| 7. There will be 'Negative Marking' for wrong ans 0.25 marks from the total score of the candidate. | wers. Each wrong answer will lead to the deduction of |
| Only those candidates who would obtain positive admission. | score in Entrance Test Examination shall be eligible for |
| 9. Do not make any stray mark on the OMR sheet. | (C) Continues has an atministration (C) |
| 10. Calculators and mobiles shall not be permitted insid | e the examination hall |
| 11. Rough work, if any, should be done on the blank sh | eets provided with the question 1 |
| 2. Ensure that your OMR Answer Sheet has been sign | ed by the Invigilator and the set is a set of the set o |
| 3. OMR Answer sheet must be handled carefully and it | should not be failt and the candidate himself/herself. |
| be evaluated. | should not be folded or mutilated in which case it will not |
| At the end of the examination, hand over the OMR original OMR sheet in presence of the Candidate and the Ca | Answer Sheet to the invigilator who will first tear off the ad hand over the Candidate's Copy to the candidate |
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M.A./M.Sc. Mathematics/A

- 1. Which of the following is true for the function f(x) = |x|?
 - (A) It is continuous for all x
 - (B) It is differentiable for all x
 - (C) It is continuous as well as differentiable for all x
 - (D) It is neither continuous nor differentiable at x = 0

2. If
$$f(x) = e^{\frac{1}{x}}, x \neq 0$$

= 0, x = 0

then $\lim_{x\to 0} f(x)$:

- (A) = 0(B) = 1 $(C) = \infty$ (D) Does not exist
- 3. At x = 0, the function :

$$f(x) = \frac{\sin 2x}{x}, x \neq 0$$
$$= 1, x = 0$$

is:

- (A) Continuous
- (B) Differentiable
 - (C) Continuous but not differentiable
 - (D) Neither continuous nor differentiable
 - 4. If f'(x) is positive in [a, b], then :
 - (A) f(a) < f(b) (B) f(a) > f(b)

 (C) f(a) = f(b) (D) None of the above holds

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5. The coefficient of $\left(x - \frac{\pi}{4}\right)^3$ when sin x is expanded in ascending powers of $\left(x - \frac{\pi}{4}\right)$ is:

(A)
$$-\frac{1}{\sqrt{2}}$$
 (B) $-\frac{1}{2\sqrt{2}}$
(C) $-\frac{1}{6\sqrt{2}}$ (D) $-\frac{1}{4\sqrt{2}}$

6. $\lim_{x\to 0} (1-x)^{\frac{1}{x}} =$

- (A) 1 (B) $\frac{1}{e}$ (C) e (D) ∞
- 7. The points of minimum curvature on the curve $y = \log \sin x$ are, for any integer n, given by x =
 - (A) $\pm \frac{n\pi}{2}$ (B) $\pm \frac{n\pi}{3}$ (C) $\pm n\pi$ (D) $\pm \frac{n\pi}{4}$
- 8. Which of the following curves has no asymptotes?

| (A) | $y^2 = 4ax$ | (B) | $\mathbf{x}^2\mathbf{y}^2 + \mathbf{y}^2 = 1$ |
|-----|---|-----|--|
| (C) | $\mathbf{x}\mathbf{y}^3 + \mathbf{x}^3\mathbf{y} = 1$ | (D) | $\mathbf{x}\mathbf{y}^2 + \mathbf{y}^2 = \mathbf{x}$ |

9. The general value of x which satisfies the equation :

 $\operatorname{cis} x. \operatorname{cis} 2x. \operatorname{cis} 3x \dots \operatorname{cis} nx = 1$

is:

(A)
$$\frac{2m\pi}{n+1}$$
 (B) $\frac{2m\pi}{n(n+1)}$
(C) $\frac{4m\pi}{n(n+1)}$ (D) $\frac{4m\pi}{n}$

where m is an integer.

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10. If $\cos\theta = \frac{1}{2}\left(x + \frac{1}{x}\right)$, $\cos\phi = \frac{1}{2}\left(y + \frac{1}{y}\right)$, then one of the values of $x^{m}y^{n} + \frac{1}{x^{m}y^{n}}$ is: (A) $2\cos(\theta + \phi)$ (B) $2\cos(m\theta + n\phi)$ (C) $2\cos(n\theta + m\phi)$ (D) $2\cos(m\theta - n\phi)$ 11. $\tan^{-1}\frac{1}{2} + \tan^{-1}\frac{1}{2} =$

(A)
$$\frac{\pi}{2}$$
 (B) $\frac{\pi}{3}$
(C) $\frac{\pi}{4}$ (D) π

12. The sum to n terms of the series

 $\tan^{-1}\frac{1}{3} + \tan^{-1}\frac{1}{7} + \tan^{-1}\frac{1}{13} + \dots$

is equal to :

(A)
$$\tan^{-1} \frac{n}{n+2}$$
 (B) $\tan^{-1} \frac{n+2}{n}$
(C) $\tan^{-1} \frac{1}{n+2}$ (D) $\tan^{-1} \frac{1}{n+1}$

13. The line $y = mx + \frac{a}{m}$ touches the parabola $y^2 = 4ax$ at the point :

(A) $(am^2, 2am)$ (B) $\left(am^2, \frac{2a}{m}\right)$ (C) $\left(\frac{a}{m^2}, 2am\right)$ (D) $\left(\frac{a}{m^2}, \frac{2a}{m}\right)$

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× 4 ×

14. The distance between the foci of the ellipse $3x^2 + 4y^2 = 12$ is equal to :

 (A) 4
 (B) 3

 (C) 2
 (D) 1

15. If a circle cuts the rectangular hyperbola $xy = a^2$ in points t_1, t_2, t_3, t_4 , then $t_1t_2t_3t_4 =$

- (A) 1 (B) 2
- (C) a^2 (D) a^4

16. The conditions for the line $\frac{x-\alpha}{l} = \frac{y-\beta}{m} = \frac{z-\gamma}{n}$ to lie in the plane

- ax + by + cz + d = 0 are :
 - (A) $a\alpha + b\beta + c\gamma = 0$, al + bm + cn + d = 0
 - (B) $a\alpha + b\beta + c\gamma = 0$, al + bm + cn = 0
 - (C) $a\alpha + b\beta + c\gamma + d = 0$, al + bm + cn = 0
 - (D) $a\alpha + b\beta + c\gamma + d = 0$, al + bm + cn + d = 0

17. The equation of the radical plane of two spheres

 $x^{2} + y^{2} + z^{2} + 2u_{1}x + 2v_{1}y + 2w_{1}z + d_{1} = 0$

and

 $x^{2} + y^{2} + z^{2} + 2u_{y}x + 2v_{y}y + 2w_{y}z + d_{y} = 0$

is:

(A)
$$(u_1 - u_2)x + (v_1 - v_2)y + (w_1 - w_2)z + (d_1 - d_2) = 0$$

(B)
$$(u_1 + u_2)x + (v_1 + v_2)y + (w_1 + w_2)z + (d_1 + d_2) = 0$$

(C)
$$2(u_1 - u_2)x + 2(v_1 - v_2)y + 2(w_1 - w_2)z + (d_1 - d_2) = 0$$

(D) $2(u_1 + u_2)x + 2(v_1 + v_2)y + 2(w_1 + w_2)z + (d_1 + d_2) = 0$

18. The general equation to the cone of the second degree passing through the axes is :

(A)
$$ax^2 + by^2 + cz^2 + 2ux + 2vy + 2wz + d = 0$$

- (B) $ax^2 + by^2 + cz^2 + 2fyz + 2gzx + 2hxy = 0$
- (C) $ax^2 + by^2 + cz^2 + 2fyz + 2gzx + 2hxy + 2ux + 2vy + 2wz + d = 0$
- (D) fyz + gzx + hxy = 0

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× 5 ×

19. The surface represented by $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 0$ is:

(A) An ellipsoid(B) A hyperboloid of one sheet(C) A sphere(D) A cone

20. The condition for the plane $\lambda x + my + nz = p$ to touch the central conicoid $ax^2 + by^2 + cz^2 = 1$ is :

- (A) $a^{2}l^{2} + b^{2}m^{2} + c^{2}n^{2} = p^{2}$ (B) $al^{2} + bm^{2} + cn^{2} = p^{2}$ (C) $\frac{l^{2}}{a} + \frac{m^{2}}{b} + \frac{n^{2}}{c} = p^{2}$ (D) $\frac{l^{2}}{a^{2}} + \frac{m^{2}}{b^{2}} + \frac{n^{2}}{c^{2}} = p^{2}$
- $21. \quad \int \frac{\mathrm{dx}}{\mathrm{x}^2 \sqrt{1+\mathrm{x}^2}} =$

(A)
$$\frac{x}{\sqrt{1+x^2}}$$

(B) $-\frac{x}{\sqrt{1+x^2}}$
(C) $\frac{\sqrt{1+x^2}}{x}$
(D) $-\frac{\sqrt{1+x^2}}{x}$

22. The value of $\int_0^{\pi} \frac{\sin nx}{\sin x} dx$, where n is an odd integer, is :

(A) 0
(B) π
(C) n
(D) nπ

23. The area bounded by the curve $y = \cos x (0 \le x \le 2\pi)$, the x-axis and the ordinate $x = 2\pi$ is equal to :

(A) 2 (B) 2π (C) 4π (D) 4

× 6 ×

24. For what value of n is div $\overline{F} = 0$, where $\overline{F} = r^n r$, $\overline{r} = xi + yj + zk$ and $r = |\vec{r}|$?

- (A) -2 (B) -1(C) -3 (D) -4
- 25. The degree and order of the differential equation

$$x\frac{dy}{dx} + y = a\frac{dx}{dy}$$

are respectively :

- (A) 2,1
 (B) 1,2
 (C) 1,1
 (D) 2,2
- 26. The solution of the differential equation

$$x(1 + y^2)dx + y(1 + x^2)dy = 0$$

is:

(A)
$$1 + x^2 + y^2 = k$$

(B) $(1 + x^2)(1 + y^2) = k$
(C) $\frac{1 + x^2}{1 + y^2} = k$
(D) $\frac{1 + y^2}{1 + x^2} = k$

27. Which of the following differential equations is not exact?

| (A) | xdy + (y - x)dx = 0 | (B) | $(e^{y}+1)\cos x dx + e^{y}\sin x dy = 0$ |
|-----|-------------------------------------|------------|---|
| (C) | $(x^2 + y^2)dx + (x^2 - y^2)dy = 0$ | (D) | $(1-2xy-y^2)dx - (x+y)^2dy = 0$ |

28. The particular integral of the differential equation

 $(D^3 - 3D + 2)y = x^2 e^x$

is:

(A)
$$e^{x}\left(\frac{x^{4}}{36} - \frac{x^{3}}{27} + \frac{x^{2}}{27}\right)$$
 (B) $e^{x}\left(\frac{x^{4}}{27} - \frac{x^{3}}{27} + \frac{x^{2}}{36}\right)$
(C) $e^{x}\left(\frac{x^{4}}{27} - \frac{x^{3}}{36} + \frac{x^{2}}{27}\right)$ (D) $e^{x}\left(\frac{x^{4}}{36} + \frac{x^{3}}{27} + \frac{x^{2}}{27}\right)$

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[Turn over

P+(0+9)*(9+0)+9

29. If A is a square matrix and $P = A + \overline{A}'$, $Q = A - \overline{A}'$ then :

- (A) P is symmetric, Q is skew-symmetric
- (B) P is skew-symmetric, Q is symmetric
- (C) P is Hermitian, Q is skew-Hermitian
- (D) P is skew-Hermitian, Q is Hermitian
- 30. Which of the following is not true for any three square matrices P, Q, R of the same order ?
 - (A) P + (Q + R) = (P + Q) + R(B) P(QR) = (PQ)R(C) P(Q + R) = PQ + PR(D) $PQ = PR \Rightarrow Q = R$
- 31. For what values of α , β , γ , the matrix

| [| 0 | 2β | γ] | |
|-----|---|----------|----|--|
| A = | α | β | -γ | |
| 1 | α | $-\beta$ | γ | |

satisfies AA' =1?

- (A) $\alpha = \pm \frac{1}{\sqrt{6}}, \beta = \pm \frac{1}{\sqrt{2}}, \gamma = \pm \frac{1}{\sqrt{3}}$
- (B) $\alpha = \pm \frac{1}{\sqrt{3}}, \beta = \pm \frac{1}{\sqrt{2}}, \gamma = \pm \frac{1}{\sqrt{6}}$
- (C) $\alpha = \pm \frac{1}{\sqrt{2}}, \beta = \pm \frac{1}{\sqrt{3}}, \gamma = \pm \frac{1}{\sqrt{6}}$
- (D) $\alpha = \pm \frac{1}{\sqrt{2}}, \beta = \pm \frac{1}{\sqrt{6}}, \gamma = \pm \frac{1}{\sqrt{3}}$
- 32. If A is an idempotent matrix of order 3 whose trace is equal to 5, then the trace of $5A^4 4A^3 + 3A^2 4A + I$ is equal to :
 - (A) 5
 (B) 4

 (C) 3
 (D) 2 9

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× 8 ×

33. The sum and the product of the roots of the characteristic equation of the matrix

 $\mathbf{A} = \begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$

are respectively :

- (A) 7 and 7 (B) 7 and 5
- (C) 7 and 6 (D) 7 and 8

34. For what value of b does the system of equations 2x + y + 2z = 0, x + y + 3z = 0, 4x + 3y + bz = 0 have a non-trivial solution?

| (A) | b = 2 | (B) | b = 3 | |
|-----|-------|-------------|-------|--|
| (C) | b = 6 | (D) | b = 8 | |

F1 1 27

35. The rank of the matrix
$$\begin{bmatrix} 1 & 1 & 2 \\ 1 & 2 & 2 \\ 2 & 2 & 3 \end{bmatrix}$$
 is equal to :

(A) 2 (B) 3

(C) 1

36. The number of linearly independent solutions of the equation x + y = 1 is:

- (A) 1 (B) 2
- (C) 3 (D) 4

37. The condition that the roots of the equation $x^3 - px^2 + qx - r = 0$ are in G.P. is that :

(D) 4

| (A) | $q^3 = p^3 r$ | $(B) p^3 = q^3 r$ |
|-----|---------------|--------------------|
| | | |
| 1 | | |

(C) $r^3 = p^3 q$ (D) pqr = 1

38. If P(x) = 0 is an equation of odd degree such that $x^n P\left(\frac{1}{x}\right) = P(x)$, which of the

following is a root of P(x) = 0?

- (A) x = 1 (B) x = -1
- (C) x = 0 (D) None of these

39. If α , β , γ are the roots of the cubic $x^3 + px^2 + qx + r = 0$, then $\alpha^3\beta^3 + \beta^3\gamma^3 + \gamma^3\alpha^3 =$

> (A) 3r - pq(B) $\frac{q^2 - 2pr}{r^2}$ (C) $2(p^2 - 3q)$ (D) $3r^2 + q^3 - 3pqr$

40. How many roots of the equation $z^4 + z^2 + 1 = 0$ lie in |z| < 1?

- (A) 1 (B) 2
- (C) 3 (D) None

41. If the sequences $\{a_n\}$ and $\{b_n\}$ are defined by $a_n = 2^n$, when n is odd

n 2, when it is eau

 $= 3^{n}$, when n is even

and

 $b_n = 3^n$, when n is odd

 $= 2^{n}$, when n is even,

then the limit superior of the sequence $\left\{ (a_n b_n)^{\frac{1}{n}} \right\}$ is equal to :

- (A) 2 (B) 3
- (C) 6 (D) 9

× 10 ×

| 42. | The serie | $es \frac{x}{1} + \frac{1}{2} \cdot \frac{x^3}{3} + \frac{1 \cdot 3}{2 \cdot 4} \cdot \frac{x}{3}$ | $\frac{x^5}{5} + \frac{1.3.5}{2.4.6} \cdot \frac{x^7}{7} + \dots$ | is convergent if : | |
|-----|-----------|--|---|----------------------------|-------------|
| | (A) | $x^2 > 1$ | (B) | $x^2 \le 1$ | |
| | (C) | x > 1 | (D) | x < 1 | |
| | | | | | |
| 43. | Under w | hat condition does th | e equation $ax = e^{x}$ | have a root between 0 and | d1? |
| | (A) | a = e | (B) | a < e | |
| | (C) | a > e | (D) | None | |
| | | | | | |
| 44. | Under w | what condition is $ x +$ | y < x + y ; x, | y ∈ R ? | |
| | (A) | xy>0 | (B) | xy = 0 | |
| | (C) | xy < 0 | (D) | xy ≤ 0 | |
| | | | | | |
| 45. | Which o | of the following is true | for the function f d | efined over [a, b] by | |
| | f(x) | = x, when x is rational | | | |
| | | =-x, when x is irratio | nal? | | (x) = (x,x) |
| | (A) | f is integrable but f | is not integrable of | over [a, b] | |
| | (B) | f is integrable but | f is not integrable of | over [a, b] | |
| | (C) | f and $ f $ are both in | tegrable over [a, b |] | |
| | (D) | Neither f nor $ f $ is in | ntegrable over [a,] | b] | |
| | | | | | |
| 46. | Which o | of the following is not t | rue? | | |
| | (A) | Every continuous fu | unction on [a, b] is i | integrable over [a, b] | |
| | (B) | Every monotonic fu | nction on [a, b] is i | integrable over [a, b] | |
| | (C) | Every integrable fur | nction over [a, b] is | continuous on [a, b] | |
| | (D) | A bounded function integrable over [a, b | having a finite nu b] | mber of discontinuities or | n [a, b] is |
| | | | | | |

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× 11 ×

47. If f is a bounded function defined on [a, b] and P_1, P_2 are any two partitions of [a, b], then:

(A)
$$L(P_{1} \cup P_{2}, f) \le L(P_{p}, f)$$
 (B) $U(P_{1} \cup P_{2}, f) \ge U(P_{p}, f)$
(C) $L(P_{1} \cup P_{2}, f) \le U(P_{1} \cup P_{2}, f)$ (D) $U(P_{p}, f) \le U(P_{2}, f)$

48. The value of the R-integral $\int_{1}^{1} f(x) dx$, where f(x) = |x| is:

| (A) | 0 | (B) 1 |
|-----|---|-----------|
| (C) | 2 | (D) 3 |

49. $\lim_{(x,y)\to(0,0)} \frac{xy^3}{x^2+y^6}$

(A) = 0 $(B) = \infty$ (C) = 1(D) Does not exist

50. At (0, 0) the function

f(x,y) =
$$\frac{x^2y}{x^3 + y^3}$$
, (x, y) ≠ (0,0)
= 0, (x, y) = (0, 0)

is:

(A) Continuous

(C) Discontinuous

- (B) Differentiable
- (D) Continuous but not differentiable

(C) Every antemobile function over (a, bilis de

51. The value of $\iint xyf(x, y)dxdy$, where $A = \{(x, y), 0 < x < 1, 0 < y < 1\}$ and

f(x, y) = x + y is:

(A)
$$\frac{7}{12}$$
 (B) $\frac{11}{144}$
(C) $-\frac{1}{11}$ (D) $\frac{1}{3}$

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× 12 ×

52. The function $f(x, y) = x^3 + y^3 - 3x - 12y + 20$ has a maximum value at :

(A) (1,2)(B) (-1,2)(C) (1,-2)(D) (-1,-2)

53. Let the binary operation * be defined on the set Z of integers by a*b=a+b-7. Then the inverse of 2 in Z is :

| (A) | -2 | (B) 0 |) |
|-----|----|-------|---|
| (C) | 10 | (D) 1 | 2 |

54. A non-commutative group has :

- (A) At least 4 elements (B) At least 5 elements
- (C) At least 6 elements (D) None of these

55. The number of generators of an infinite cyclic group is :

- (A) 0 (B) 1
- (C) 2 (D) Infinite

56. If $f: G \rightarrow G'$ is an isomorphism, then the kernel of f is equal to :

- (A) (e) (B) G
- (C) G' (D) None of these

57. Which of the following is incorrect in the theory of rings?

- (A) Every ideal is a subring
- (B) The product of any two ideals is again an ideal
- (C) Every field is an integral domain
- (D) None of the above

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58. The ideal (2) in the ring of integers is :

| (A) | A prime ideal | (B) | A principal ideal |
|-----|---------------|------------|-------------------|
| | | | |

(C) A maximal ideal (D) All of the above

- 59. Which of the following is true for the vectors (1, 0, 0), (0, 1, 0) and (0, 0, 1) in the real vector space R³?
 - (A) They are linearly dependent in \mathbb{R}^3 (B) They form a basis of \mathbb{R}^3

(C) Both (A) and (B) (D) Neither (A) nor (B)

- 60. If V and W are vector spaces over the same field F of dimensions m and n respectively, then Hom(V, W) is a vector space over F of dimension :

 - (C) n^2 (D) $\frac{m}{n}$



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× 15 ×

M.A./M.Sc. Mathematics/B

| 1. | For what values of m, n, the system of equations x + y + z = 6, $x + 2y + 3z = 10$, $x + 2y + mz = n$ |
|----|---|
| | have no solution ? |
| | (A) $m = 3, n = 10$ (B) $m = 3, n \neq 10$ |
| | (C) $m \neq 3, n = 10$ (D) $m \neq 3, n \neq 10$ |
| 2. | If α , β , γ are the roots of the equation $x^3 - 6x^2 + 11x - 6 = 0$, then the equation whose roots are $\alpha\beta$, $\beta\gamma$, $\gamma\alpha$ is : |
| | (A) $x^3 - 11x^2 + 36x + 36 = 0$ (B) $x^3 - 11x^2 + 36x - 36 = 0$ |
| | (C) $x^3 + 11x^2 - 36x + 36 = 0$ (D) $x^3 - 11x^2 - 36x + 36 = 0$ |
| 3. | If α , β , γ are the roots of the equation $x^3 + ax - b = 0$, then $\alpha^2 \beta^2 + \beta^2 \gamma^2 + \gamma^2 \alpha^2 =$ |
| | (A) a^2 (B) $a^2 + b$ (C) $a^2 - 2b$ (D) $a^2 - b$ |
| 4. | The numbers of positive and negative roots of the equation $x^3 + x^2 + x - 1 = 0$ are respectively : |
| | (A) 1,1 (B) 1,2 |
| | (C) 2, 1 (D) 2, 2 |
| 5. | How many roots does the equation $z^4 + z^2 + 1 = 0$ have in $ z < 1$? |
| | (A) 4 (B) 3 (C) 2 (D) 0 |
| 6. | If 'a' and 'b' are the supremum and infimum of the set $S = \left\{\frac{1}{n}, n \in N\right\}$, then : |
| | (A) $a \in S, b \in S$ (B) $a \in S, b \notin S$ |
| | (C) $a \notin S, b \in S$ (D) $a \notin S, b \notin S$ |
| 7. | If Q, Q ^c and R are the sets of rational, irrational and real numbers respectively, then the set Q together with the set of its limit points equals : (A) Q (D) Q (D) Q (D) Q (D) Q |
| | $(A) Q (B) Q^{*} (C) R (D) \phi$ |
| 8. | Which of the following is true for the sequences $\{a_n\}$ and $\{b_n\}$, where |
| | $a_n = 1 + \frac{1}{2!} + \frac{1}{3!} + \dots + \frac{1}{n!}$ and $b_n = \frac{(-1)^n}{n}$, $n = 1, 2, 3, \dots, ?$ |
| | (A) $\{a_n\}$ is convergent, $\{b_n\}$ is divergent |
| | (B) $\{b_n\}$ is convergent, $\{a_n\}$ is divergent |
| | (C) Both are convergent |
| | (D) Both are divergent |
| 1 | |
| | |

2.

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At which point x in [-1, 1] is the tangent to the curve $y = \sqrt{1 - x^2}$ parallel to the x-axis ?

| (A) | x = -1 | (B) | $\mathbf{x} = 1$ |
|-----|------------------|-----|-------------------|
| (C) | $\mathbf{x} = 0$ | (D) | None of the above |

- 10. If f(x) is continuous on [a, b], then which of the following is not true in general?
 - (A) $\int_{a}^{b} f(x) dx = \lambda(b-a)$ for some number λ lying between the bounds of f(x)(B) $\int_{a}^{b} f(x) dx = (b-a) f(c)$ for some number c lying between a and b

(C) $\left| \int_{a}^{b} f(x) dx \right| \le k |b-a|$ for some number k such that

 $|f(x)| \le k, \forall x \in [a, b]$

(D)
$$\int_{a}^{b} f(x) dx = 0 \text{ if } f(x) \ge 0, \forall x \in [a, b]$$

11. Which of the following is true for the function

f(x) = 1, x rational = 0, x irrational

- 0, x in [a, b] ?

(A)
$$\int_{a}^{b} f(x) dx = 0$$

(B)
$$\int_{a}^{b} f(x) dx = 1$$

(C) f(x) is not R-integrable over [a, b]

(D) None of the above

12. What is the value of
$$\int_{-1}^{1} |x| dx$$
?
(A) 1 (B) -1 (C) 2 (D) 0

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9.

13. If [x] denotes the greatest integer function not greater than x, then $\int [x] dx =$

0

14.
$$\lim_{(x,y)\to(0,0)} \frac{xy(x^2 - y^2)}{x^2 + y^2} =$$

(A) 0 (B) 1 (C) 2 (D) -1

15. If $f(x, y) = 2x^4 - 3x^2y + y^2$, then f(x, y) has :

- (A) a maximum at (0, 0)
- (B) a minimum at (0, 0)
- (C) neither a maximum nor a minimum at (0, 0)
- (D) none of the above properties

16. If
$$\Gamma(\alpha) = \int_{0}^{\infty} x^{\alpha-1} e^{-x} dx$$
, then $\Gamma\left(\frac{3}{2}\right) =$

(A)
$$\sqrt{\pi}$$
 (B) $\frac{\sqrt{\pi}}{2}$ (C) $\sqrt{2\pi}$ (D) $\sqrt{\frac{\pi}{2}}$

17. What is the value of $\iint_E e^{\frac{y}{x}} dx dy$, where E is the triangle formed by the straight lines y = x, y = 0 and x = 1?

(A)
$$e-1$$
 (B) $\frac{e}{2}$ (C) $\frac{1-e}{2}$ (D) $\frac{e-1}{2}$

18. If a function $f: [0, 1] \rightarrow R$ is defined by $f(x) = x^2$, then f is :

- (A) one-one (B) onto
- (C) one-one and onto (D) many-one
- 19. If $G = \{z \in C, z^n = 1\}$, then G is a multiplicative group which is :
 - (A) Abelian(B) non-abelian(C) of prime order(D) without any subgroups

20. If the number of left cosets of a subgroup H of a group G with identity e, then :

| (A) | $H = \{e\}$ | (B) $H = G$ |
|-----|------------------|-----------------|
| (C) | H is normal in G | (D) G is simple |

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21. If G is a group and f: G \rightarrow G is defined by $f(x) = x^{-1} ax$, $\forall x \in G$ for some fixed element $a \in G$, then f is : (B) an isomorphism on G (A) a homomorphism on G (C) an automorphism on G (D) all the above 22. Which of the following is true for any two subrings S_1 and S_2 of a ring R? (B) $S_1 \cap S_2 \neq \Phi$ (A) $S_1 \cap S_2 = \Phi$ (D) $S_1 \subset S_2$ (C) $S_1 \cup S_2 = R$ 23. Which of the following is both a prime and a maximal ideal in the ring of intergers ? (D) (15) (A) (4) (B) (6) (C) (2) 24. If X is a finite dimensional vector space and X' its dual space, then : (B) $\dim(X') > \dim(X)$ (A) $\dim(X') < \dim(X)$ (D) $\dim(X) < \dim(X')$ (C) $\dim(X') = \dim(X)$ 25. If T is a linear transformation from the vector space X_F to the vector space Y_{F} , then T is one-one if and only if :

| (A) | $T(x) = 0 \implies x = 0$ | (B) | $x = 0 \Rightarrow T(x) = 0$ |
|-----|---------------------------|------------|------------------------------|
| (C) | Neither (A) nor (B) holds | (D) | None of the above holds |

26. Which of the following is a point of discontinuity of the function :

f (0) =
$$x \sin \frac{1}{x}$$
, $x \neq 0$
= 0, $x = 0$?
(A) $x = 0$
(B) $x = 1$
(D) None of the above

27. What is the value of the 'c' of the Lagrange's Mean Value Theorem for the function $f(x) = 2x^2 - 7x + 10$ in [2, 5]?

| (A) | $c = \frac{7}{4}$ | (B) | $c = \frac{7}{2}$ | (C) | $c = \frac{2}{7}$ | (D) | $c = \frac{10}{7}$ |
|-----|-------------------|-----|-------------------|-----|-------------------|-----|--------------------|
| | · · · · | | | | | | |

28. If f''(x) exists and is continuous, then
$$\frac{f(x+h) + f(x-h) - 2f(x)}{h} =$$

| (A) t' | (X) | (B) | I(X) |
|--------|------|-----|-------------------|
| (C) f | "(x) | (D) | None of the above |

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29. If $u = \lim_{x \to 0} \frac{e^{\frac{1}{x}}}{e^{\frac{1}{x}} + 1}$, then : (A) u = 0 (B) u = 1(C) u = e (D) u does not exist

30. What is the value of
$$\lim_{x\to 0} \frac{e^x \sin x - x - x^2}{x^3}$$
?
(A) 0 (B) $\frac{2}{3}$ (C) $\frac{1}{3}$ (D)

31. The angle of intersection of the curves $r = a\theta$ and $r = \frac{a}{\theta}$ is equal to :

(A)
$$\frac{\pi}{3}$$
 (B) $\frac{\pi}{2}$ (C) $\frac{\pi}{4}$ (D) $\frac{\pi}{6}$

32. If
$$u = \tan^{-1}\left(\frac{x^2 + y^2}{x + y}\right)$$
, then $x\frac{\partial u}{\partial x} + y\frac{\partial u}{\partial y} =$
(A) $\sin 2u$ (B) $\sin u$ (C) $\frac{1}{2}\sin 2u$ (D) $\frac{1}{2}\sin u$

- 33. The points of numerically maximum curvature on the curve y = log sin x are given by :
 - (A) $x = \pm n\pi$ (B) $x = \pm (2n+1)\frac{\pi}{2}$ (C) $x = \pm \frac{n\pi}{2}$ (D) $x = \pm (2n+1)\pi$,

where n = 0, 1, 2, 3

34. Which of the following pairs gives the modulus and amplitude of the complex number : $1 - \cos \phi + i \sin \phi$?

| (A) | $2\sin\frac{\phi}{2},\frac{\pi}{2}$ | (B) | $2\sin\frac{\phi}{2}, \frac{\pi}{2}-\frac{\phi}{2}$ |
|-----|-------------------------------------|-----|---|
| (C) | $\sin\frac{\phi}{2},\frac{\pi}{2}$ | (D) | $\sin\frac{\phi}{2},\frac{\pi}{2}-\frac{\phi}{2}$ |

35. If $\cos 2\theta + i \sin 2\theta = p$, $\cos 2\phi + i \sin 2\phi = q$, then $\sqrt{\frac{p}{q}} + \sqrt{\frac{q}{p}} =$ (A) $\cos(\theta - \phi)$ (B) $2\cos(\theta - \phi)$ (C) $2i\sin(\theta - \phi)$ (D) $i\sin(\theta - \phi)$

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36. The real and imaginary parts of Log(-i) are respectively :

(A)
$$1, -\frac{\pi}{2}$$

(B) $0, (4n-1)\pi$
(C) $1, (4n-1)\frac{\pi}{2}$
(D) $0, (4n-1)\frac{\pi}{2}$

37. What is the sum to n terms of the series

$$\tan^{-1}\frac{1}{3} + \tan^{-1}\frac{1}{7} + \tan^{-1}\frac{1}{13} + \dots ?$$
(A)
$$\tan^{-1}\frac{n}{n+1}$$
(B)
$$\tan^{-1}\frac{n+1}{n}$$
(C)
$$\tan^{-1}\frac{n}{n+2}$$
(D)
$$\tan^{-1}\frac{n+2}{n}$$

38. The coordinates of the foci and eccentricity of the ellipse $\frac{x^2}{9} + \frac{y^2}{16} = 1$ are respectively :

| (A) | $(0,\pm\sqrt{7}),\frac{\sqrt{7}}{4}$ | (B) | $(\pm\sqrt{7},0),\frac{\sqrt{7}}{4}$ |
|-----|--------------------------------------|-----|--------------------------------------|
| (C) | $(\pm\sqrt{7}, 0), \sqrt{7}$ | (D) | $(0,\pm\sqrt{7}),\sqrt{7}$ |

39. Which of the following is the equation of the normal to the rectangular hyperbola

 $x^2 - y^2 = a^2$ at the point (a sec θ , b tan θ)?

- (A) $x \sec \theta y \tan \theta = a \tan \theta \sec \theta$
- (B) $x \tan \theta + y \sec \theta = a \tan \theta \sec \theta$
- (C) $x \tan \theta + y \sec \theta = 2a \tan \theta \sec \theta$
- (D) $x \sec \theta y \tan \theta = 2a \tan \theta \sec \theta$

40. What is the centre of the conic

$$36x^{2} + 24xy + 29y^{2} - 72x + 126y + 81 = 0?$$
(A) (2, 3) (B) (3, 2) (C) (3, -2) (D) (2, -3)

- 41. The image of the point (1, 3, 4) in the plane 2x y + z + 3 = 0 is : (A) (2, -1, 1) (B) (1, 3, 4) (C) (-1, 4, 3) (D) (-3, 5, 2)
- 42. The distance of the centre of the sphere

$$x^2 + y^2 + z^2 - 2y - 4z = 11$$

from the yz-plane is :

(A) 0 (B) 1 (C) 2 (D) 11

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43. The semi-vertical angle of a right circular cone having 3 mutually perpendicular generators is :

(A)
$$\tan^{-1}\frac{1}{\sqrt{2}}$$
 (B) $\tan^{-1}\sqrt{2}$ (C) $\tan^{-1}\sqrt{3}$ (D) $\tan^{-1}\frac{1}{\sqrt{3}}$

44. The locus of the tangents to a sphere which are parallel to a given line is : (A) a sphere (B) a cone (C) a cylinder (D) a circle

45. Which of the following is the condition for the plane lx + my + nz = p to touch the conicoid $ax^2 + by^2 + cz^2 = 1$?

(A)
$$al^{2} + bm^{2} + cn^{2} = p^{2}$$

(B) $a^{2}l^{2} + b^{2}m^{2} + c^{2}n^{2} = p^{2}$
(C) $a^{2}l + b^{2}m + c^{2}n = p^{2}$
(D) $\frac{\ell^{2}}{a} + \frac{m^{2}}{b} + \frac{n^{2}}{c} = p^{2}$

46. What is the value of
$$\int \frac{xe^x dx}{(x+1)^2}$$
?

(A)
$$\frac{e^x}{(x+1)^2} + c$$

(B) $\frac{e^x}{x^2+1} + c$
(C) $\frac{e^x}{x+1} + c$
(D) None of the above

47. Which of the following is the value of $\int_{0}^{x} \sin^{5} x dx$? (A) $\frac{4}{5}$ (B) $\frac{8}{15}$ (C) $\frac{3}{4}$ (B) $\frac{15}{8}$ (D) $\frac{15}{8}$ (A) $\sin x$ (C) $\frac{1}{3}$ (B) $\cos x$ (C) $\frac{1}{3}$ (D) None of the above

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- 49. If $\vec{a} = \hat{i} + \hat{j} + \hat{k}$, $\vec{b} = \hat{i} \hat{j} + \hat{k}$ and $\vec{c} = \hat{i} + \hat{j} \hat{k}$, then $\vec{a} \cdot \vec{b} \times \vec{c}$ and $\vec{a} \times (\vec{b} \times \vec{c})$ are respectively equal to :
 - (A) $4, -2\hat{j}+2\hat{k}$ (B) $4, 2\hat{i}-2\hat{k}$ (C) $4, 2\hat{i}-2\hat{j}$ (D) $4, 2\hat{j}-2\hat{k}$

50. The pair giving the degree and order of the differential equation

$$\left[1 + \left(\frac{dy}{dx}\right)^2\right]^3 = \left(\frac{d^2y}{dx^2}\right)^2 \text{ is :}$$
(A) (3,2) (B) (2,2) (C) (2,3) (D) (3,3)

51. Which of the following is the general solution of the differential equation

$$(1 + x^{2})\frac{dy}{dx} + y = e^{\tan^{-1}x} ?$$
(A) $y = \frac{1}{2}e^{-\tan^{-1}x} + ce^{\tan^{-1}x}$
(B) $y = \frac{1}{2}e^{\tan^{-1}x} + c^{-\tan^{-1}x}$
(C) $y = \frac{1}{2}e^{2\tan^{-1}x} + ce^{-2\tan^{-1}x}$
(D) $y = \frac{1}{2}e^{-2\tan^{-1}x} + ce^{2\tan^{-1}x}$

52. The general solution of the differential equation $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = x^2 e^{3x}$ is :

(A)
$$y = (c_1 + c_2 x) e^x + \frac{e^{3x}}{8} (2x^2 - 4x + 3)$$

(B)
$$y = (c_1 + c_2 x) e^x$$

(C)
$$y = (c_1 + c_2 x + c_3 x^2) e^x$$

(D)
$$y = (c_1 + c_2 x) e^x + \frac{c}{8} (x^2 - x + 2)$$

53. The general solution of the differential equation $x \frac{dy}{dx} + \left(\frac{dy}{dx}\right)^2 - y = 0$ is :

- (A) $y = cx + c^2$ (B) $y = cx - \frac{1}{c^2}$ (C) xy = c(D) None of the above
- 54. If A is a skew-symmetric matrix of order n, then :

| A) | $ \mathbf{A} = \mathbf{n}$ | Sec. 1 | (B) | A = 1 |
|----|-----------------------------|--------|------------|-------------------|
| C) | A = 0 | | (D) | None of the above |

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55. If A' is the transpose of a square matrix A and $P = \frac{A + A'}{2}, Q = \frac{A - A'}{2}$, then :

- (A) P is symmetric, Q is skew-symmetric
- (B) P and Q are both symmetric
- (C) Q is symmetric, P is skew-symmetric
- (D) Neither P nor Q is symmetric

56. If $A = \begin{bmatrix} 5 & 6 & 7 \\ 4 & 3 & 2 \\ 1 & 8 & -9 \end{bmatrix}$, $B = \begin{bmatrix} \lambda & 6 & 7 \\ 4 & \mu & 2 \\ 1 & 8 & \nu \end{bmatrix}$ and $A + 2B = \begin{bmatrix} 1 & 18 & 21 \\ 12 & 5 & 6 \\ 3 & 24 & 5 \end{bmatrix}$, then (λ, μ, ν) = (A) (-2, 1, 7) (C) (2, -1, 7) (C) (2, -1, 7) (D) (7, 1, 2) 57. If A is a square matrix of order 3 such that |A| = k, then |2A| =(A) 2k (C) 6k (D) 8k

58. If A = $\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$, for what value of m and n is the characteristic

 $-x^{3} + mx^{2} + nx + 4 = 0$ the characteristic equation of A?

(A) m = -6, n = 9(B) m = 6, n = -9(C) m = 9, n = 6(B) m = 6, n = -9(D) m = -9, n = 6

| | | 2 | 3 | -1 | -1 | | | |
|-----|--------------------------------------|---|------|----|----|---|-----|---|
| 50 | What is the rank of the matrix A | 1 | -1 - | -2 | -4 | 0 | | |
| 59. | what is the rank of the matrix $A =$ | 3 | 1 | 3 | -2 | | | |
| | | 6 | 3 | 0 | -7 | | , | |
| | (A) 4 (B) 3 | | (C) | 2 | | | (D) | 1 |

60. The vectors $[2 \ 3 \ -1 \ -1]$, $[1 \ -1 \ -2 \ -4]$, $[3 \ 1 \ 3 \ -2]$ and $[6 \ 3 \ 0 \ -7]$:

- (A) are linearly independent
- (B) are linearly dependent

(C) form a basis for the vector space of all row matrices of order 4

(D) satisfy none of the above properties

CLM-53699-B

Mathematics/B

- 1. Which of the following are respectively the infimum and supremum of the set
 - $\begin{cases} \frac{(-1)^{n}}{n}, n \in N \\ \end{cases} ?$ (A) 0, 1
 (B) -1, 1
 (C) -1, \frac{1}{2}
 (D) \frac{1}{2}, 1

2. Which of the following is the value of $\lim a_n$ where $a_n = 1 + (-1)^n$, $n \in \mathbb{N}$?

| (A) | 0 | (B) | 1 |
|-----|----|-----|---|
| (C) | -1 | (D) | 2 |

- 3. For what value of S_n is the sequence $\{S_n\}$ convergent?
 - (A) $S_n = 1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$
 - (B) $S_n = 1 + \frac{1}{3} + \frac{1}{5} + \dots + \frac{1}{2n-1}$
 - (C) $S_n = 1 + \frac{1}{4} + \frac{1}{7} + \dots + \frac{1}{3n-2}$
 - (D) $S_n = 1 + \frac{1}{4} + \frac{1}{9} + \dots + \frac{1}{n^2}$
- 4. The image of a closed interval under a continuous function is :
 - (A) a closed interval (B) an open interval
 - (C) a semi-open interval (D) a semi-closed interval

5. The upper and lower Riemann integrals of the function f(x) = 0, x rational = 1, x irrational

on any interval [a, b] are respectively equal to :

- (A) 0, b-a (B) a, b
- (C) b-a, b+a (D) b-a, 0

CZB-29327(B)

6. What is the value of the R-intergral $\int_{-1}^{1} |x| dx$?

- (A) 0 (B) -1
- (C) 1 (D) 2
- 7. Which of the following is not true for the function

f(x) = 1, x rational = -1, x irrational

defined on [a, b]?

(A)
$$\int_{\underline{a}}^{b} f(x) dx = a - b$$

(B)
$$\int_a^b f(x) dx = b - a$$

- (C) f(x) is R-integrable over [a, b]
- (D) f(x) is not R-integrable over [a, b]
- 8. If a function f(x) has an infinite number of discontinuities in [a, b] then :
 - (A) f(x) is not R-integrable over [a, b]
 - (B) f(x) is R-integrable over [a, b]
 - (C) f(x) may or may not be R-integrable over [a, b]
 - (D) None of the above holds

9. If
$$f(x,y) = \left(\frac{y-x}{y+x}\right) \left(\frac{1+x}{1+y}\right)$$
, then $\lim_{(x,y)\to(0,0)} f(x,y)$:
(A) = 0 (B) = 1
(C) = -1 (D) Does not exist

10. For the function :

$$f(x,y) = \frac{xy(x^2 - y^2)}{x^2 + y^2}, (x, y) \neq (0, 0)$$

= 0, (x, y) = (0, 0)
(A) fxy=fyx

(B) fx

(C) fxy and fyx do not exist

) fxy≠fyx

(D) None of the above holds

CZB-29327(B)

| 11. | The value of $\iint (x + y) dx dy$ where $A = \{(x, y), 0 < x < 1, 0 < y < 1\}$ is: | | | |
|-----|---|---|-----------|--------------------------------|
| | (A) | 0 | (B) | 1 |
| | (C) | $\frac{1}{2}$ | (D) | 2 |
| 12. | If x = r si | $n \theta \cos \phi, y = r \sin \theta \sin \phi, z = r \cos \theta, r$ | then | |
| | $\frac{\partial (\mathbf{x}, \mathbf{x})}{\partial (\mathbf{r}, \mathbf{x})}$ | $\frac{(y,z)}{(\theta,\phi)} =$ | | |
| | (A) | r sin θ | (B) | $r\cos\theta$ |
| | (C) | $r^2 \sin \theta$ | (D) | $r^2 \cos \theta$ |
| 13. | If in a gr | oup G, $a^{-1} = a$, $\forall a \in G$, then G is : | | |
| | (A) | finite | (B) | infinite |
| | (C) | abelian | (D) | non-abelian |
| 14. | The inter | rsection of two subgroups of finite index | is: | |
| | (A) | empty | (B) | of finite index |
| | (C) | normal | (D) | none of the above |
| 15. | lf G is a | group with center $Z(G)$ and if $\frac{G}{Z(G)}$ is | cyclic, t | hen G is : |
| | (A) | finite | (B) | infinite |
| | (C) | abelian | (D) | non-abelian |
| 16 | . The cor | verse of Lagrange's theorem is true for | : | |
| | (A) | finite groups | (B) | abelian groups |
| | (C) | non-abelian groups | (D) | cyclic groups |
| 17 | . In the ri | ng $\{a + bi; a, b \text{ integers}\}$ with respect to us of units is: | isual add | lition and multiplication, the |
| | (A) | 1 | (B) | 2 |
| | (C) | 3 | (D) | 4 |
| | (\mathbf{c}) | - | | |

CZB-29327(B)

4

- 18. If R is a commutative ring with unity having no nontrivial ideals, then R is :
 - (A) a division ring **(B)** an integral domain
 - (C) a field (D)
- - none of the above
- 19. Which of the following is a subspace of the vector space of complex numbers over the field of real numbers?
 - (A) the set of integers
 - (B) the set of natural numbers
 - (C) the set of real numbers
 - (D) the set of irrational numbers
- 20. The dimension of the vector space of complex numbers over the real field is :
 - (A) 1 **(B)** 2 (C) 3 (D) 4
- 21. The function f(x) is defined by

$$f(x) = \frac{|x - 4|}{|x - 4|}, x \neq 4$$

= 0, x = 4

what is the value of $\lim_{x \to 4} f(x)$?

- (A) 0
- (C) –1

(B) 1

(D) It does not exist

22. If
$$f(x) = \frac{\sin 2x}{x}, x \neq 0$$

= 1, x = 0,

then f(x) has:

- (A) a removable discontinuity at x = 0
- a discontinuity of the first kind x = 0(B)
- (C) a discontinuity of the second kind at x = 0
- none of the above properties (D)

23. Which of the following is the value of the 'C' of the Lagrange's Mean Value Theorem

for the function $f(x) = \log x$ on $\left[\frac{1}{2}, 2\right]$?

(A)
$$3 \log 2$$
 (B) $\frac{2}{3 \log 2}$
(C) $\frac{3}{\log 2}$ (D) $\frac{3}{4 \log 2}$

24. If $f(x) = 0, x \le 0$

= x, x > 0,

Then f(x) is:

- (A) continuous and differentiable at x = 0
- (B) differentiable but not continuous at x = 0
- (C) continuous but not differentiable at x = 0
- (D) neither continuous nor differentiable at x = 0

25. Which of the following is the value of
$$\lim_{x \to 0} \left(\frac{1}{x^2} - \frac{1}{\sin^2 x} \right)?$$
(A) $\frac{1}{3}$
(B) $\frac{1}{2}$
(C) $-\frac{1}{3}$
(D) $-\frac{1}{2}$

26. The polar subtangent for the parabola $\frac{2a}{\gamma} = 1 - \cos\theta$ is equal to :

(A)
$$a \csc \frac{\theta}{2}$$
 (B) $2a \csc \frac{\theta}{2}$
(C) $2a \csc \theta$

(C)
$$a \csc \theta$$
 (D) $2a \csc \theta$

27. The radius of curvature at any point of the curve

$$x = a (\theta - \sin \theta), y = a(1 - \cos \theta)$$

is equal to :

(A)
$$a \sin \frac{\theta}{2}$$
 (B) $4 a \sin \theta$

(C)
$$4 a \sin \frac{\theta}{2}$$
 (D) $4 a \cos \theta$

CZB-29327(B)

- 28. What type of a double point is the origin on the curve $a^2y^2 = a^2x^2 4x^3$?
 - (A) a node (B) a cusp
 - (C) a conjugate point (D) none of the above

29. For any two complex numbers z_1 and z_2 , $|z_1 + z_2|^2 + |z_1 - z_2|^2 - 2(|z_1|^2 + |z_2|^2) =$ (A) 0
(B) 1
(C) $|z_1|^2 + |z_2|^2$ (D) $|z_1|^2 - |z_2|^2$

30. What is the value of $\frac{(\sqrt{3} + i)^4}{(-1 + i\sqrt{3})^6}$?

(A)
$$\frac{1}{8} - i\frac{\sqrt{3}}{8}$$

(B) $-\frac{1}{8} + i\frac{\sqrt{3}}{8}$
(C) $\frac{1}{8} + i\frac{\sqrt{3}}{8}$
(D) $-\frac{1}{8} - i\frac{\sqrt{3}}{8}$

31. What is the real part of $\sin^{-1}(\cos \theta + i \sin \theta)$?

(A)
$$\sin^{-1}(\sqrt{\sin \theta})$$
 (B) $\cos^{-1}(\sqrt{\cos \theta})$
(C) $\sin^{-1}(\sqrt{\cos \theta})$ (D) $\cos^{-1}(\sqrt{\sin \theta})$

32.
$$\log\left(\frac{a+bi}{a-bi}\right) = :$$

(A) $\frac{\pi}{2}i$ (B) $i \tan^{-1}\left(\frac{b}{a}\right)$
(C) $2i \tan^{-1}\left(\frac{b}{a}\right)$ (D) $i \tan h^{-1}\left(\frac{b}{a}\right)$

33. The line y = mx + c is a normal to the parabola $y^2 = 4ax$ for all values of m if:

(A)
$$c = a m + \frac{a}{m}$$
 (B) $c^2 = a^2 + m^2$
(C) $c = \frac{a}{m}$ (D) $c = -2am - am^3$

CZB-29327(B)

34. The eccentricity and the distance between the foci of the ellipse $3x^2 + 4y^2 = 12$ are respectively equal to :

(A)
$$2 \text{ and } \frac{1}{2}$$
 (B) $\frac{1}{2} \text{ and } 2$
(C) $\frac{1}{3} \text{ and } 3$ (D) $\frac{1}{4} \text{ and } 4$

- 35. The equation of the diameter which is conjugate to the diameter x = 2y of the hyperbola $16x^2 9y^2 = 144$ is :
 - (A) y = 2x(B) 16x = 9y(C) 32x = 9y(D) 9x = 16y
- 36. The equation of a straight line through the point (3, 1, -6) and parallel to each of the planes x + y + 2z 4 = 0 and 2x 3y + z + 5 = 0 is :

(A)
$$\frac{x-3}{1} = \frac{y-1}{1} = \frac{z+6}{2}$$

(B) $\frac{x-3}{2} = \frac{y-1}{-3} = \frac{z+6}{1}$

(C)
$$\frac{x-3}{3} = \frac{y-1}{7} = \frac{z+6}{-5}$$

(D)
$$\frac{x-3}{7} = \frac{y-1}{3} = \frac{z+6}{-5}$$

- 37. The spheres $a(x^2 + y^2 + z^2) + 2lx + 2my + 2nz + p = 0$ and $b(x^2 + y^2 + z^2) = k^2$ will cut orthogonally if:
 - (A) $l^2 + m^2 + n^2 = p^2$ (B) $al^2 + bm^2 + pn^2 = 0$
 - (C) $ak^2 = bp$ (D) $a^2 + b^2 = p^2$
- 38. The general equation of a cone which passes through the axes is :

| (A) | $ax^2 + by^2 + cz^2 = 0$ | (B) | $ax^2 + by^2 + cz^2 = 1$ |
|-----|--------------------------|-----|--------------------------|
| (C) | fyz + gzx + hxy = 0 | (D) | fyz + gzx + hxy = 1 |

CZB-29327(B)

39. The locus of the points of intersection of three mutually perpendicular tangent planes to the central conicoid $ax^2 + by^2 + cz^2 = 1$ is a :

| (A) | circle | (B) | sphere |
|-----|--------|------------|----------|
| (C) | cone | (D) | cylinder |

40. The number of normals that can be drawn to the conicoid $ax^2 + by^2 + cz^2 = 1$ from a given point in general is :

(D)

two

- (A) six (B) five
- (C) three

41. What is the value of
$$\int_{a}^{b} \frac{\log x}{x} dx$$
?
(A) $2 \log \left(\frac{b}{a}\right) \log (ab)$ (B) $2 \log \left(\frac{a}{b}\right) \log (a b)$
(C) $\frac{1}{2} \log \left(\frac{b}{a}\right) \log (a b)$ (D) $\frac{1}{2} \log \left(\frac{a}{b}\right) \log (a b)$

42. Which of the following is the value of the integral $\int \cos^{-1}\left(\frac{1-x^2}{1+x^2}\right) dx$?

- (A) $2x \tan^{-1} x \log(1 + x^2) + c$
- (B) $2x \tan^{-1} x + \log(1 + x^2) + c$
- (C) $x \tan^{-1} x \frac{1}{2} \log(1 + x^2) + c$
- (D) $x \tan^{-1} x + \frac{1}{2} \log(1 + x^2) + c$
- 43. For any three vectors $\vec{a}, \vec{b}, \vec{c}$, what is the value of $\vec{a} \times (\vec{b} \times \vec{c}) + \vec{b} \times (\vec{c} \times \vec{a}) + \vec{c} \times (\vec{a} \times \vec{b})$? (A) 3 (B) $\vec{a} \cdot \vec{b} \times \vec{c}$ (C) $\vec{a} + \vec{b} + \vec{c}$ (D) 0

CZB-29327(B)

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44. $\nabla^2 \gamma =$

(A)
$$\frac{1}{\gamma}$$
 (B) $\frac{2}{\gamma}$
(C) 2γ (D) γ^2

45. Which of the following is the solution of the differential equation

$$\frac{dy}{dx} + 3y = e^{2x} ?$$
(A) $y = (2x + c) e^{-x^2}$
(B) $y = \frac{1}{5}e^{2x} + ce^{-3x}$
(C) $y = cx + 2e^{-x^2}$
(D) $y = \frac{1}{5}e^{-3x} + ce^{2x}$

46. For what value of 'a' and 'b' is the function a e^{bx} particular integral of the differential equation

$$\frac{d^2y}{dx^2} + 13\frac{dy}{dx} + 42y = 112e^x ?$$
(A) $a = 2, b = 1$
(B) $a = 6, b = -1$
(C) $a = -4, b = 2$
(D) $a = 1, b = 2$

47. Which of the following is the value of $\frac{1}{D^2 + 4}(\sin 2x)$?

(A)
$$\frac{1}{4}x \sin 2x$$
 (B) $-\frac{1}{4}x \sin 2x$
(C) $-\frac{1}{4}x \cos 2x$ (D) $\frac{1}{4}x \cos 2x$

48. Which of the following is the complete primitive of the differential equation

$$p^{2} + p - 6 = 0, \text{ where } p = \frac{dy}{dx} ?$$
(A) $(y - 2x - c) (y + 3x - c) = 0$
(B) $(y - 2x - c_{1}) (y + 3x - c_{2})$
(C) $(y - 3x - c_{1}) (y + 2x - c_{2}) = 0$
(D) $(y - 3x - c) (y + 2x - c) = 0$

CZB-29327(B)

49. If $D = \text{diag}(\alpha_1, \alpha_2, \dots, \alpha_n)$ is a diagonal matrix of order n, then $D^p =$

- (A) diag $(\alpha_1, \alpha_2, \dots, \alpha_n)$
- (B) diag $(p\alpha_1, p\alpha_2, \dots, p\alpha_n)$
- (C) diag $(\alpha_1 + p, \alpha_2 + p, ..., \alpha_n + p)$
- (D) diag $(\alpha_1^{p}, \alpha_2^{p}, \dots, \alpha_n^{p})$

50. If A is a Skew-Hermitian matrix then the diagonal elements of A are all :

- (A) zeros (B) purely imaginary
- (C) zeros or real (D) zeros or purely imaginary
- 51. If X and Y are inversible matrices of the same order, then X Y is inversible if and only if:

| (A) | $\mathbf{X} = \mathbf{Y}$ | (B) | $\mathbf{X}^2 = \mathbf{Y}^2$ |
|-----|---------------------------|-----|-----------------------------------|
| (C) | XY = YX | (D) | $\mathbf{X}^2 + \mathbf{Y}^2 = 0$ |

52. How many square matrices A and B are there such that AB - BA = I?

| (A) | finite | (B) | infinite |
|-----|--------------------|-----|----------|
| (C) | finite or infinite | (D) | none |

53. For what values of α nd β is the equation $\lambda^3 - 6\lambda^2 + \alpha\lambda - \beta = 0$, the characteristics

equation of the matrix
$$\begin{bmatrix} 1 & 2 & 5 \\ 0 & 2 & 4 \\ 0 & 0 & 3 \end{bmatrix}$$
?
(A) $\alpha = 6, \beta = 11$
(B) $\alpha = 11, \beta = 6$
(C) $\alpha = 3, \beta = 5$
(D) $\alpha = 2, \beta = 3$

54. What is the rank of the matrix
$$\begin{bmatrix} 1 & 0 & 0 & 4 \\ 0 & 1 & 5 & 6 \\ 1 & 3 & 2 & 1 \end{bmatrix}$$
?
(A) 4 (B) 3
(C) 2 (D) 1

CZB-29327(B)

55. If A is a 4×5 matrix with rank 3, then the number of linearly independent solutions of the equation AX = 0 is :

| (A) | 4 | (B) | 3 |
|-----|---|-----|---|
| (C) | 2 | (D) | 1 |

56. If C_1, C_2, \dots, C_n are the linearly dependent columns of a m × n matrix A of rank r, then:

| (A) | r < n | (B) | r > n |
|-----|---------------------------|-----|-------------------------|
| (C) | $\mathbf{r} = \mathbf{n}$ | (D) | None of the above holds |

57. If a_1, a_2, \dots, a_n are the roots of the equation $x^n + nax - b = 0$, then

| $(a_1 - a_2) (a_1 - a_3) \dots (a_1 - a_n) =$ | | |
|---|------------|--------------------------------|
| (A) na ₁ | (B) | na _l ⁿ⁻¹ |
| (C) $(n-1)a$ | (D) | $n(a_1^{n-1} + a)$ |

58. If the roots of the equation $x^3 - px^2 + qx - r = 0$ are in H.P., then the mean root is equal to :

| (A) | $\frac{3p}{q}$ | (B) | <u>3q</u> p |
|-----|----------------|-----|----------------|
| (C) | <u>3r</u> q | (D) | <u>3q</u> r |

59. Which of the following is the equation whose roots are the cubes of the roots of the equation $x^3 + 3x^2 + 2 = 0$?

| (A) | $y^3 + 33y^2 + 12y + 8 = 0$ | (B) | $y^3 + 12y^2 + 33y + 8 = 0$ |
|-----|-----------------------------|-----|-----------------------------|
| (C) | $y^3 + 8y^2 + 12y + 33 = 0$ | (D) | $y^3 + 33y^2 + 8y + 12 = 0$ |

60. What is the minimum number of imaginary roots which the equation $2x^7 - x^4 + 4x^3 - 5 = 0$ can possess?

(A) 2 (B) 3

(C) 4 (D) 5

CZB-29327(B)

Mathematics - 2010

M. Sc. Mathematics

1. Which of the following is true ?

- I. As $x \rightarrow 0$, the infinitesimal log (1+x) is of higher order than the infinitesimal x
- II. As $x \to 0$, the infinitesimal $\sqrt{x(1-x)}$ is of lower order than the infinitesimal x
 - (a) Ionly (b) IIonly
 - (c) Both I and II (d) None of the above
- 2. In the Lagrange's Mean Value theorem, what is the value of C if $f(x) = x^3 3x^2 + 2x$, a = 0 and $b = \frac{1}{2}$?

| (a) | $1-\frac{\sqrt{3}}{3}$ | (b) $1 + \frac{\sqrt{21}}{6}$ | |
|-----|---------------------------|-------------------------------|-----|
| (c) | $1 - \frac{\sqrt{21}}{6}$ | (d) None of the abo | ove |

3. What is the coefficient of x³ in the power series expansion of the function Sin³x :

| (a) | $\frac{1}{6}$ | (b) | $\frac{1}{3}$ |
|-----|---------------|-----|-------------------|
| (c) | $\frac{1}{2}$ | (d) | None of the above |

4. Which of the following is the value of the limit :

 $\lim_{x \to 0} \frac{(3\tan x - 3x - x^3 + x^4 \sin x)}{x^5}$ (a) Non - existent
(b) $\frac{7}{5}$ (c) $\frac{2}{5}$ (d) None of the above

5. If P is the radius of curvature at any point P on the parabola $y^2 = 8x$ and S is its focus,

then what is the value of $\frac{P^2}{(SP)^3}$?

| (a) | $\frac{1}{4}$ | (b) | $\frac{1}{2}$ |
|-----|---------------|-----|---------------|
| (c) | 4 | (d) | 2 |

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2
- 6. Consider the curve $y^2 = (x a) (x b) (x c), 0 \le a \le b \le c$. Then which of the following is true?
 - I. The curve has no double points
 - II. A part of the curve lies to the left of the line x = a
 - (a) None (b) Both I and II
 - (c) Ionly (d) II only
- 7. If Z_1 and Z_2 are two complex numbers such that $|Z_1|^2 + |Z_2|^2 = 5$, then what is the
 - value of $\sqrt[4]{|Z_1 + 2Z_2|^2 + |2Z_1 Z_2|^2}$?
 - (a) It cannot be determined by the given information
 - (b) $\sqrt{10}$
 - (c) 4
 - (d) 5
- 8. If $\sin \alpha + \sin \beta + \sin \gamma = 0 = \cos \alpha + \cos \beta + \cos \gamma$, then which of the following is the value of M + N where M = $\sin (\alpha + \beta) + \sin (\beta + \gamma) + \sin (\gamma + \alpha)$ and

 $N = \frac{\cos 3\alpha + \cos 3\beta + \cos 3\gamma}{\cos(\alpha + \beta + \gamma)}$? (a) 3 (b) 1 (c) 0 (d) None of the above

- 9. Which of the following statements is true :
 - I. The sum of the rth powers of the nth roots of unity vanishes if r is a multiple of n
 - II. The product of the n^{th} roots of unity is $(-1)n^{-1}$
 - (a) Ionly (b) IIonly (d) Nereoftheol
 - (c) Both I and II (d) None of the above
- 10. For what value of $\psi(\theta)$, $-\frac{\pi}{2} < \theta < \frac{\pi}{2}$, $\log(1 + e^{i2\theta}) i\theta = \psi(\theta)$? (a) $\log(2\cos\theta)$ (b) $i\theta$
 - (c) $\log(2\sin\theta) + i\theta$ (d) None of the above

11. What is the value of $\tan^{-1} 1 + 2 \tan^{-1} \frac{1}{3} + \tan^{-1} \frac{1}{7}$? (a) π (b) $\frac{2\pi}{3}$

(c) $\frac{\pi}{2}$ (d) None of the above

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[Turn Over

12. An equilateral triangle is inscribed in the parabola $y^2 = 2x$, one of whose vertex is the vertex of the parabola. If a is the length of its sides, what is the value of a?

| (a) $4\sqrt{3}$ | (b) | 2√3 |
|-----------------|-----|-----|
|-----------------|-----|-----|

- (c) $\sqrt{3}$ (d) None of the above
- 13. If e is the eccentricity and l is the length of the latus rectum of the ellipse $9x^2 + 25y^2 = 225$, what is the value of the pair (e, l)?

| (a) | $\left(\frac{4}{3},\frac{50}{9}\right)$ | (b) | $\left(\frac{4}{3},\frac{18}{5}\right)$ |
|-----|---|-----|---|
| (c) | $\left(\frac{4}{5},\frac{50}{3}\right)$ | (d) | $\left(\frac{4}{5},\frac{18}{5}\right)$ |

- 14. Which of the following is the equation of the hyperbola whose directrix is 2x + y = 1,
 - focus (1, 1) and eccentricity $\sqrt{3}$?
 - (a) $x^2 + y^2 2x 2y 4 = 0$
 - (b) $5x^2 + 5y^2 + 4x 2y 1 = 0$
 - (c) $7x^2 + 2y^2 12xy 10x + 8y + 5 = 0$
 - (d) $7x^2 2y^2 + 12xy 2x + 4y 7 = 0$
- 15. For which of the following values of the pair (α, β) , $\alpha x + \beta y 3z = 5$ represents the equation of the plane passing through the points (1, 2, 1) and (-2, 2, -1)?

| (a) | (3, 2) | (b) | (2, 3) |
|-----|---------|-----|-------------------|
| (c) | (-3, 1) | (d) | None of the above |

16. If the axes are rectangular and O is the origin, what is the equation of the plane through the point P (2, 3, -1) at right angles to OP ?

| (a) | 3x + 2y - z = 11 | (b) | 3x - 2y + 4z + 4 = 0 |
|-----|------------------|-----|----------------------|
| (c) | 2x + 3y - z = 14 | (d) | None of the above |

17. For which of the following values of the pair (α, β) , $\frac{x-3}{\alpha} = \frac{y+1}{\beta} = \frac{z-11}{4}$ is the equation of the perpendicular from (3, -1, 11) to the line $\frac{x}{2} = \frac{y-2}{3} = \frac{z-3}{4}$?

| (a) | (1, -6) | (b) | (6, -1) |
|-----|---------|-----|-------------------|
| (c) | (4, 5) | (d) | None of the above |

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18. What is the radius of the circular section of the sphere $x^2 + y^2 + z^2 = 41$ by the plane $2x + 3y + z = 5\sqrt{14}$?

| (a) | $\sqrt{41}$ | (b) | 5 |
|-----|-------------|-----|---|
| (c) | $\sqrt{14}$ | (d) | 4 |

- 19. If $a^{-1} + b^{-1} + c^{-1} = 0$, what is the angle between the lines of intersection given by x + y + z = 0 and the cone ayz + bzx + cxy = 0?
 - (a) $\frac{\pi}{2}$ (b) $\frac{\pi}{3}$ (c) $\frac{\pi}{6}$ (d) None of the above
- 20. What are the equations of the tangent planes of the conicoid $2x^2 6y^2 + 3z^2 = 5$, which pass through the line x + 9y 3z = 0, 3x 3y + 6z 5 = 0?
 - (a) 4x 6y + z = 5 and 4x 9y + 2z = 5
 - (b) 4x + 6y 3z = 5 and 5x + 15y z = 5
 - (c) 4x + 6y + 3z = 5 and 2x 12y + 9z = 5
 - (d) None of the above
- 21. What is the value of the integral $\int_{0}^{1} \left(\frac{1-x^{2}}{1+x^{2}}\right) dx$?
 - (a) $\frac{\pi}{4}$ (b) $\frac{\pi}{2} + 1$ (c) $\frac{\pi}{2} - 1$ (d) None of the above
- 22. Which of the following is the value of the integral $\int \sin^3 x \, dx$?
 - (a) $\frac{2}{3}$ (b) $\frac{8}{3}$ (c) $\frac{10}{3}$ (d) None of the above

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23. What is the value of the integral $\int_{0}^{1} \frac{\sqrt{x}}{\sqrt{x} + \sqrt{1-x}} dx$? (b) $\frac{1}{2}$ (a) 0 (d) None of the above (c) 2 24. What is the entire length of the asteroid $x^{\frac{3}{2}} + y^{\frac{3}{2}} = 4b^{\frac{3}{2}}$? (b) 12b (a) 6b (d) 48b (c) 24b 25. Three vectors $\vec{a} = 12\vec{i} + 4\vec{j} + 3\vec{k}$, $\vec{b} = 8\vec{i} - 12\vec{j} - 9\vec{k}$ and $\vec{c} = 33\vec{i} - 4\vec{j} - 24\vec{k}$ define a parallelopiped. What is its volume? (b) 5915 (a) 3696 (d) None of the above (c) 9061 26. If $\vec{a}, \vec{b}, \vec{c}$ and $\vec{a^{i}}, \vec{b^{i}}, \vec{c^{i}}$ form a reciprocal system of vectors, then which of the following is true? II. $\vec{a} \times \vec{a^{1}} + \vec{b} \times \vec{b^{1}} + \vec{c} \times \vec{c^{1}} = 0$ I. $\vec{a} \cdot \vec{a}^{1} + \vec{b} \cdot \vec{b}^{1} + \vec{c} \cdot \vec{c}^{1} = 1$ (b) Ionly (a) Both I and II (d) None of the above (c) II only 27. The differential equation $(1 + x^2)\left(\frac{dy}{dx}\right) - 4x^2\cos^2 y + x\sin 2y = 0$ can be reduced to the linear form by the transformation z = (b) cos²y (a) $1 + x^2$ (d) tan y (c) sin²y 28. What is the value of $\left[\frac{1}{(D+3)^2}\right](x^2+1)$ where $D = \frac{d}{dx}$? (b) $\frac{1}{27}(3x^2-4x+5)$ (a) $4(x^2+3)^2$ (c) $\frac{1}{27}(3x^2 - x + 2)$ (d) None of the above

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29. Which of the following is the solution of the differential equation

$$\frac{d^2y}{dx^2} + \frac{dy}{dx} + \left(\frac{dy}{dx}\right)^3 = 0 ?$$
(a) $y = x^2 + C_1 x + C_2$
(b) $Sin (C_1 - y) = C_2 e^{-x}$
(c) $sin (y + C_1) = C_2 x$
(d) None of the above

30. For what value of the pair (α, β) Lagendre polynomial $P_4(x) = \frac{1}{8} (\alpha x^4 - 30x^2 + \beta)$? (a) (5, 1) (b) (25, 3) (c) (35, 3) (d) None of the above

31. Let Q be a skew - symmetric matrix of order 3. For which of the following values of n, the matrix Qⁿ is a symmetric matrix of order 3 :

| (a) | 6 | (b) | 7 |
|-----|---|-----|-------------------|
| (c) | 9 | (d) | None of the above |

32. Let $P = \begin{bmatrix} 2 & -1 & 3 \\ 0 & 2 & 0 \\ 2 & 1 & 1 \end{bmatrix}$ and $Q = \begin{bmatrix} 2 & 4 & -6 \\ 0 & \alpha & \beta \\ -4 & -4 & 4 \end{bmatrix}$. For which of the following values of the pair $(\alpha, \beta), Q = (adj P)$? (a) (4, 4) (b) (-4, 4)(c) (0, -4) (d) (-4, 0)

- 33. What is the rank of the matrix P³, where $P = \begin{bmatrix} 1 & 1 & 3 \\ 5 & 2 & 6 \\ -2 & -1 & -3 \end{bmatrix}$? (a) 3 (b) 2 (c) 1 (d) 0
- 34. Let $P = [p_{ij}]$ be a square matrix of order $n \ge 2$. Then which of the following is true ? I. adj (kP) = k (adj P), where k is a scalar
 - II. $|adj P| = |P|^{n-1}$, if $|P| \neq 0$
 - (a) Ionly (b) II only
 - (c) Both I and II (d) None of the above

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| [4] dependent? (a) -1 (b) 1 (c) 3 (d) No 36. How many linearly independent solutions does the ex- have? (a) Three (b) Tw (c) One (d) No 37. For what value of p, the polynomial $2x^4 - 7x^3 + p^2x^4$ (a) ± 2 (b) $\pm (x^4 - 7x^3 + p^2x^4)$ (a) ± 2 (b) $\pm (x^4 - 7x^3 + p^2x^4)$ (c) 3 (d) No 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (d) No 39. The equation $x^n - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - [Z] \le 1$? (a) None (b) O (c) Two (d) Fo 41. Which of the following are true? 1. Every finite set of numbers is bounded II. The set N of natural numbers is bounded II. The set N of natural numbers is not bounded (a) All I, II and III (b) Ia (c) II and III only (d) II | $= \lambda$, $X_{y} = 11$ are linearly | | | |
|--|---|--|--|--|
| dependent? (a) -1 (b) 1 (c) 3 (d) No 36. How many linearly independent solutions does the ex- have? (a) Three (b) Tw (c) One (c) One (c) One (d) No 37. For what value of p, the polynomial $2x^4 - 7x^3 + p^2x + (a) \pm 2$ (c) 3 (d) No 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (c) 32 (c) 3 (c) 2 (d) No 39. The equation $x^a - nx + n - 1 = 0, n \ge 2, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation Z^4 - 2Z^3 + 3Z^2 - [Z] \le 1?(a) None(b) On(c) Two(c) Tau(c) I and III only(c) I and III only(c) I and III only(c) II and III only$ | | | | |
| (a) -1 (b) 1 (c) 3 (d) No 36. How many linearly independent solutions does the ex- have? (a) Three (b) Tw (c) One (d) No 37. For what value of p, the polynomial $2x^4 - 7x^3 + p^2x + (a) \pm 2$ (b) $\pm (c) = 3$ (d) No 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (d) No 39. The equation $x^a - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - [Z] \le 1$? (a) None (b) Oi (c) Two (d) Fo 41. Which of the following are true? I. Every finite set of numbers is bounded II. The set N of natural numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | | | | |
| (c) 3(d) No36. How many linearly independent solutions does the exhave?(a) Three(b) Tw(c) One(d) No37. For what value of p, the polynomial $2x^4 - 7x^3 + p^2x + (a) \pm 2$ (b) $\pm -(c) 3$ (a) ± 2 (b) $\pm -(c) 3$ (d) No38. For which of the following values of k, the equation multiple root?(a) -8 (b) -1 (c) 32 (d) No39. The equation $x^a - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root?(a) more than 3(b) 3(c) 2(d) 140. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - Z \le 1$?(a) None(b) On(c) Two(d) Fo41. Which of the following are true?I. Every finite set of numbers is boundedII. The set N of natural numbers is not bounded(a) All I, II and III(b) I additional product of the following of the set of numbers is not boundedII. The set N of natural numbers is not bounded | | | | |
| 36. How many linearly independent solutions does the exhave? (a) Three (b) Tw (c) One (d) No 37. For what value of p, the polynomial 2x⁴ - 7x³ + p²x + (a) ± 2 (b) ± + (c) 3 (d) No 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (d) No 39. The equation x^a - nx + n - 1 = 0, n ≥ 2, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation Z⁴ - 2Z³ + 3Z² - Z ≤ 1? (a) None (b) On (c) Two (d) Fo 41. Which of the following are true? I. Every finite set of numbers is bounded above III. The set N of natural numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | one of the above | | | |
| (a) Three (b) Tw (c) One (d) No 37. For what value of p, the polynomial $2x^4 - 7x^3 + p^2x + (a) \pm 2$ (b) $\pm -(c) = 3$ (d) No 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (d) No 39. The equation $x^a - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - Z \le 1$? (a) None (b) On (c) Two (d) Fo 41. Which of the following are true? I. Every finite set of numbers is bounded II. The set N of natural numbers is not bounded (a) All I, II and III (b) I a (c) II and III only (d) III | quation 6x - 5y + 4z - 3t = 21 | | | |
| (c) One(d) No37. For what value of p, the polynomial $2x^4 - 7x^3 + p^2x + (a) \pm 2$ (b) $\pm -(c) = 3$ (a) ± 2 (b) $\pm -(c) = 3$ (c) $3 + (c) = 3$ (c) 3 (d) No38. For which of the following values of k, the equation multiple root?(a) -8 (b) -1 (c) 32 (d) No39. The equation $x^a - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root?(a) more than 3(b) 3 (c) 2 (d) 1 40. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - Z \le 1$?(a) None(b) On(c) Two(d) Fo41. Which of the following are true?I. Every finite set of numbers is boundedII. The set N of natural numbers is not bounded(a) All I, II and III(b) Ia(a) All I, II and III(b) Ia(c) II and III only(d) II | vo | | | |
| 37. For what value of p, the polynomial 2x⁴-7x³ + p²x + (a) ± 2 (b) ± + (c) 3 (d) No 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (d) No 39. The equation x^a - nx + n - 1 = 0, n ≥ 2, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation Z⁴ - 2Z³ + 3Z² - Z ≤ 1? (a) None (b) On (c) Two (d) Fo 41. Which of the following are true? Every finite set of numbers is bounded above III. The set N of natural numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (c) II and III only | one of the above | | | |
| (a) ± 2 (b) ± -1 (c) 3 (d) No 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (d) No 39. The equation $x^n - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - Z \le 1$? (a) None (b) On (c) Two (d) Fo 41. Which of the following are true? I. Every finite set of numbers is bounded II. The set N of natural numbers is not bounded (a) All I, II and III (b) I a (c) II and III only (d) III | + 15 is divisible by x - 3? | | | |
| (c) 3(d) No38. For which of the following values of k, the equation multiple root?(a) -8 (b) -1 (c) 32(d) No39. The equation $x^n - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root?(a) more than 3(b) 3(c) 2(d) 140. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - Z \le 1$?(a) None(b) Or(a) None(b) Or(c) Two(d) For41. Which of the following are true?I. Every finite set of numbers is boundedII. The set N of natural numbers is not bounded(a) All I, II and III(b) Ia(c) II and III only(d) II | $\sqrt{14}$ | | | |
| 38. For which of the following values of k, the equation multiple root? (a) -8 (b) -1 (c) 32 (d) No 39. The equation x^a - nx + n - 1 = 0, n ≥ 2, is satisfied by of this root? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation Z⁴ - 2Z³ + 3Z² - Z ≤ 1? (a) None (b) Or (c) Two (d) Fo 41. Which of the following are true? I. Every finite set of numbers is bounded II. The set N of natural numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (c) II and III only | one of the above | | | |
| (a) -8 (b) -1 (c) 32 (d) No 39. The equation $x^n - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root ? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - Z \le 1$? (a) None (b) On (c) Two (d) Fo 41. Which of the following are true ? I. Every finite set of numbers is bounded II. The set N of natural numbers is not bounded (a) All I, II and III (b) I a (c) II and III only (d) III | $n x^3 - 9x^2 + 24x + k = 0$, has a | | | |
| (c) 32(d) No39. The equation $x^a - nx + n - 1 = 0, n \ge 2$, is satisfied by of this root?(a) more than 3(b) 3(c) 2(d) 140. How many roots does the equation $Z^4 - 2Z^3 + 3Z^2 - Z \le 1$?(a) None(b) One(c) Two(d) For41. Which of the following are true?I. Every finite set of numbers is boundedII. The set N of natural numbers is bounded(a) All I, II and III(b) Ia(c) II and III only(d) II | 6 | | | |
| 39. The equation xⁿ - nx + n - 1 = 0, n ≥ 2, is satisfied by of this root ? (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation Z⁴ - 2Z³ + 3Z² - Z ≤ 1 ? (a) None (b) On (c) Two (d) For 41. Which of the following are true ? I. Every finite set of numbers is bounded II. The set N of natural numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | one of the above | | | |
| (a) more than 3 (b) 3 (c) 2 (d) 1 40. How many roots does the equation Z ⁴ - 2Z ³ + 3Z ² - Z ≤ 1 ? (a) None (b) Or (c) Two (d) For 41. Which of the following are true ? I. Every finite set of numbers is bounded II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) Ia (c) II and III only (d) II | x = 1. What is the multiplicity | | | |
| (c) 2 (d) 1 40. How many roots does the equation Z⁴ - 2Z³ + 3Z² - Z ≤ 1 ? (a) None (b) Or (c) Two (d) For 41. Which of the following are true ? I. Every finite set of numbers is bounded II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) Ia (c) II and III only (d) II | | | | |
| 40. How many roots does the equation Z⁴ - 2Z³ + 3Z² - Z ≤ 1 ? (a) None (b) Or (c) Two (d) For 41. Which of the following are true ? I. Every finite set of numbers is bounded II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) Ia (c) II and III only (d) II | | | | |
| (a) None (b) Out (c) Two (d) For 41. Which of the following are true? I. Every finite set of numbers is bounded II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) III | -4Z + 5 = 0 have in the circle | | | |
| (c) Two (d) For the following are true? 41. Which of the following are true? I. Every finite set of numbers is bounded II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | ne | | | |
| 41. Which of the following are true? I. Every finite set of numbers is bounded II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | our | | | |
| I. Every finite set of numbers is bounded II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | | | | |
| II. The set N of natural numbers is bounded above III. The set Q of rational numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | I. Every finite set of numbers is bounded | | | |
| III. The set Q of rational numbers is not bounded (a) All I, II and III (b) I at (c) II and III only (d) II | but not bounded below | | | |
| (a) All I, II and III(b) I at(c) II and III only(d) II | | | | |
| (c) II and III only (d) II | and II only | | | |
| | I and I only | | | |
| | | | | |

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42. Which of the following statements is true?

- I. The set $\left\{\frac{1}{n}; n = 1, 2, 3, \dots\right\}$ has no limit point.
- II. Every point of the set Z of all integers is a limit point of Z.(a) Both I and II(b) I only
 - (c) II only (d) None of the above
- 43. The sequence $\{b_n\}$ where $b_n = \frac{1}{n} \{1 + 2^{\frac{1}{2}} + 3^{\frac{1}{3}} + \dots + n^{\frac{1}{n}}\}$ converges to : (a) 0 (b) 1 (c) e (d) None of the above

44. Which of the following is true?

I. The series
$$\sum_{n=1}^{\infty} \frac{1}{n^2 + n}$$
 is convergent.

II. The series $\sum_{n=3}^{\infty} \frac{1}{n \log n (\log \log n)^2}$ is divergent. (a) None (b) Both I and II

| (1) | INONE | (0) | Dom I an |
|-----|-------|-----|----------|
| (c) | Ionly | (d) | II only |

45. If a function f is derivable on a closed interval [a, b] with f' (a) ≠ f'(b) and if k is a number lying between f'(a) and f'(b) then there exist at least on point C between a and b such that :

| (a) | f(C) = k | (b) | f'(k) = C |
|-----|-----------|-----|-------------------|
| (c) | f'(C) = k | (d) | None of the above |

46. What is the value of the integral $\int_0^2 x[x] dx$, where [x] is the largest integer less or

equal to x?

| (a) | $\frac{3}{2}$ | (b) | $\frac{7}{3}$ |
|-----|---------------|-----|-------------------|
| (c) | 83 | (d) | None of the above |

| 47. | What is t | he value of the simultaneous limit | $\lim_{(x,y)\to(2}$ | $\frac{\sin^{-1}(xy-2)}{\tan^{-1}(3xy-6)}$? |
|-----|-----------|------------------------------------|---------------------|--|
| | (a) | 0 | (b) | 1 |
| | (c) | $\frac{1}{2}$ | (d) | $\frac{1}{3}$ |

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48. If V is a function of two variables x and y then for what value of the pair (α, β) ,

 $\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} - \frac{\partial^2 V}{\partial r^2} = \alpha \frac{\partial^2 V}{\partial \theta^2} + \beta \frac{\partial V}{\partial r} \text{ where } x = r\cos\theta \text{ and } y = r\sin\theta:$ (a) $\left(\frac{1}{r}, \frac{1}{r^2}\right)$ (b) $\left(\frac{1}{r^2}, \frac{1}{r}\right)$ (c) $\left(1, \frac{1}{r}\right)$ (d) None of the above

49. If xyz = 4(x + y + z), what is the minimum value of yz + zx + xy?

| (a) | 0 | (b) | 18 |
|-----|----|-----|-------------------|
| (c) | 36 | (d) | None of the above |

50. Which of the following is the value of the double integral $\iint \sqrt{x^2 + y^2} dx dy$ where

E is the region in the xy - plane bounded by $x^2 + y^2 = 4$ and $x^2 + y^2 = 9$?

| (a) | $\frac{38\pi}{3}$ | (b) | 5π |
|-----|-------------------|-----|-------------------|
| (c) | $\frac{14\pi}{3}$ | (d) | None of the above |

51. What is the value of the triple integral $\iiint_E xyz \, dx \, dy \, dz$ where E is a domain bounded by x = 0, y = 0, z = 0 and x + y + z = 1?

| (a) | $\frac{1}{6}$ | (b) | $\frac{1}{24}$ |
|-----|---------------|-----|-----------------|
| (c) | 1 120 | (d) | $\frac{1}{720}$ |

52. Which of the following is true on Z, the set of all integers?

(a) Both I and II

 The binary operation * on Z defined by a * b = a² + b² is commutative as well associative.

II. The binary operation * on Z given by a * b = 2a + b is neither commutative nor associative.

(b) Ionly

(c) II only (d) None of the above

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| 53. | Which of the following sets together with the respective binary operations defined on |
|-----|---|
| | them are groups ? |

- I. The set $G = \{2^n; n \in Z\}$ with the operation of ordinary multiplication.
- II. The set Q of all rationals with the operation * defined by a * b = a + b + ab, a, b in Q.
 - (a) Both I and II (b) I only
 - (c) II only (d) None of the above
- 54. If a is a generator of a cyclic group G of order 8, and if $\alpha =$ order of a^3 and $\beta =$ order of a^6 , then the pair (α , β) =

| (a) | (4, 2) | (b) | (4, 8) |
|-----|--------|-----|--------|
| (c) | (8,8) | (d) | (8,4) |

55. Which of the following statements is true?

- I. If p is the smallest prime factor of the order of a finite group G then any subgroup of index p is not always a normal subgroup.
- II. A finite group G of even order has no element of order 2.
 - (a) None (b) Ionly
 - (c) II only (d) Both I and II
- 56. Consider the ring X = {0, 1, 2, 3, 4, 5, 6, 7} under the addition and multiplication modulo 8. Which of the following is a unit of the ring X ?

| (a) 2 | (b) | 3 |
|-------|-----|-------------------|
| (c) 4 | (d) | None of the above |

57. Which of the following statements is true?

- I. A matrix ring F, over a field F is not always a simple ring.
- II. A division ring is a simple ring.
 - (a) Both I and II (b) I only
 - (c) II only (d) None of the above
- 58. Let V be a vector space of all functions from R to R. If V₁ is the subset of even functions and V₂ the subset of odd functions then :
 - (a) V_1 and V_2 are not sub spaces of V
 - (b) V_1 and V_2 are sub spaces of V
 - (c) V_1 is a sub space of V but V_2 is not a subspace of V
 - (d) V, is a sub space of V but V, is not a subspace of V

ELW-6746

11

[Turn Over

59. Let V = {(a, b); a, b ∈ R}. Let the operations of addition and scalar multiplication be given by :

I. (a, b) + (c, d) = (0, b + d) and k (a, b) = (0, kb)

II. (a, b) + (c, d) = (a + c, b + d) and k (a, b) = (|k|a, |k|b).

Then V is a vector space under the operations defined by :

(a) Ionly
(b) II only
(c) Both I and II
(d) None of the above

- 60. The set W of all triads defined by $W = \{(x + y, 3y, 2x y); x, y \in R\}$ is a subspace of $V_1(R)$. What is the dimension of W?
 - (a) 2 (b) 3
 - (c) 1 (d) None of the above

ELW-6746

12

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- 1. For what value of the constant k, the infinitesimals $x^5 1$ and k(x 1), as $x \rightarrow 1$, are equivalent?
 - (a) Zero
 - (b) 1
 - (c) 3
 - (d) 5

2. Let
$$f(x) = e^{-\frac{1}{x}}$$
 when $x \neq 0$

= 0 when x = 0

and let

$$g(x) = x \sin \frac{1}{x} \text{ when } x \neq 0$$

$$= 0$$
 when $x = 0$,

then which of the following is true ?

- (a) f(x) and g(x) are both continuous at x = 0
- (b) f(x) is not continuous at x = 0, but g(x) is continuous at x = 0
- (c) f(x) and g(x) are both discontinuous at x = 0

(d) None of the above

3. What is the coefficient of x^3 in the power series expansion of the function :

$$\log\left(\frac{1+x}{1-x}\right)^{\frac{1}{3}}$$
 for $-1 \le x \le 1$?

(a) $\frac{2}{9}$ (b) $\frac{1}{9}$

(c) 2

(d) None of the above

Math.

1

Which of the following is the value of the limit 4.

 $\lim_{x\to 0}\frac{\tan x - x + \frac{1}{3}x^3}{x^3}?$

- (a) 0
- $\frac{2}{15}$ (b)
- $\frac{1}{3}$ (c)
- 23 (d)

For which of the following functions : 5.

(I)
$$f(x) = 1 - (x - 1)^{\frac{2}{3}}$$
 on [0, 2] and

 $f(x) = (x + 1)^2 (x - 2)$ on [-1, 2], (II)

Rolle's theorem is valid ?

- For both (I) and (II) (a)
- (b) For (I) only
- (c) For (II) only
- (d) None of the above

What is the curvature of the parabola $y^2 = 2px$ at the point $\left(\frac{p}{2}, p\right)$? 6.

- $\frac{1}{2\sqrt{2}p}$ (a)
- (b) $\sqrt{2}p^3$
- $2p^{\frac{3}{2}}$ (c)
- (d) None of the above

Math.

2

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7. For which of the following values of the pair (k, m), the straight line kx + m is an oblique asymptote to the curve :

$$y=\frac{x^2+2x-1}{x}?$$

- (a) (1, 0)
- (b) (1, 2)
- (c) (2, 2)
- (d) None of the above

8. If
$$\frac{(1+i)^9}{(1-i)^7} = \mathbf{P} + i\mathbf{Q}$$
,

then what is the value of P?

- (a) 0
- (b) 4
- (c) 2
- (d) None of the above

9. If $\omega = \cos \frac{2\pi}{3} + i \sin \frac{2\pi}{3}$, then which of the following is the value of $(1 + \omega)^3$?

- (a) -1
- (b) 1
- (c) i
- (d) None of the above

10. For what value of the pair (α, β) ,

 $\cos 40 - 8 \cos^4\theta = \alpha \cos^2\theta + \beta$?

- (a) (1, 1)
- (b) (6, 0)
- (c) (8, 0)
- (d) (-8, 1)

Math.

3

11. If $\log(z)$ denotes the principal value of $\log(z)$ and n is an integer, then :

$$\log(-7) - \log 7 =$$

- (a) 2*n*π
- (b) *nπi*
- (c) $(2n + 1) i\pi$
- (d) None of the above

12. If C + iS = $e^{i\theta}(2\sin\theta)^{-\frac{1}{2}}(\sin\theta - i\cos\theta)^{-\frac{1}{2}}$, then which of the following is the value of S?

(a)
$$\frac{\sin\left(\theta + \frac{\pi}{2}\right)}{\sqrt{2\sin\theta}}$$

(b)
$$\frac{\sin\left(\frac{\theta}{2} + \frac{\pi}{4}\right)}{\sqrt{2\sin\theta}}$$

- (c) $\frac{1}{\sqrt{2}}\cos\left(\frac{\theta}{2}+\frac{\pi}{4}\right)$
- (d) None of the above
- 13. Which of the following is the equation of the chord of the parabola $y^2 = 8x$ which is bisected at the point (2, -3)?
 - (a) 3x + 4y + 6 = 0
 - (b) 4x 3y 17 = 0
 - (c) 4x 3y + 31 = 0

(d)
$$4x + 3y + 1 = 0$$

Math.

14. What is the pole of the line 2x + y - 1 = 0 with respect to the ellipse

$$\frac{x^2}{3} + \frac{y^2}{2} = 1?$$

- (a) (6, 2)
- (b) (18, 4)
- (c) $(2\sqrt{3}, \sqrt{2})$

(d) None of the above

15. Let P(x, y) be a point on the hyperbola

$$\frac{x^2}{4} - \frac{y^2}{3} = 1.$$

If PS and PS' are focal distances of P(x, y), then |PS' - PS| =

(a) 8

•

- (b) 6
- (c) 4
- (d) None of the above

a.

16. What is the length of the semi-major axis of the ellipse

$$36x^2 + 24xy + 29y^2 - 72x + 126y + 81 = 0$$

given that the centre is the point (2, -3) and the semi-axes of the ellipse are connected by the equation

$$\left(\frac{1}{5}-\frac{1}{r^2}\right)\left(\frac{29}{180}-\frac{1}{r^2}\right)=\frac{1}{225}$$
?

(a) 9

- (b) 3
- (c) 2
- (d) None of the above

Math.

5

- 17. Which of the following is the equation of the plane which meets the coordinate axes in P, Q, R such that the centroid of the ΔPQR is the point (l, m, n)?
 - (a) $\frac{x}{l} + \frac{y}{m} + \frac{z}{n} = 3$
 - (b) lx + my + nz = 3
 - (c) lx + my + nz = 1
 - (d) None of the above
- 18. Which of the following is the condition that the two spheres :

$$x^{2} + y^{2} + z^{2} + 2u_{1}x + 2v_{1}y + 2w_{1}z + d_{1} = 0$$

and

$$x^{2} + y^{2} + z^{2} + 2u_{2}x + 2v_{2}y + 2w_{2}z + d_{2} = 0$$

be orthogonal ?

(a) $u_1u_2 + v_1v_2 + w_1w_2 = d_1d_2$

(b)
$$u_1u_2 + v_1v_2 + w_1w_2 = \frac{d_1d_2}{2}$$

(c)
$$u_1u_2 + v_1v_2 + w_1w_2 = \frac{d_1 + d_2}{2}$$

- (d) None of the above
- 19. What is the general equation of the cone of second degree which passes through the axes ?

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- (a) $fx^2 + gy^2 + hz^2 = 0$
- (b) fyz + gzx + hxy = 0
- (c) $ax^2 + by^2 + cz^2 = fyz + gzx + hxy$
- (d) None of the above

Math.

- 20. Which of the following is the equation of the plane which cuts the conicoid $x^2 + 4y^2 5z^2 = 1$ in a conic whose centre is at the point (2, 3, 4)?
 - (a) x + 4y 5z + 4 = 0
 - (b) 3x + 5y 4z 5 = 0
 - (c) x + 4y + 2z 22 = 0
 - (d) x + 6y 10z + 20 = 0
- 21. What is the value of the integral

$$\int_0^1 \frac{x\,dx}{\sqrt{1-x^4}}\,?$$

(a) $\frac{\pi}{2}$ (b) $\frac{\pi}{4}$ (c) $\frac{3}{2}$

(d) None of the above

22. For which of the following values of $\phi(x)$,

$$\int x^{m} \cos nx \, dx + \frac{m(m-1)}{n^{2}} \int x^{m-2} \cos nx \, dx$$
$$= \frac{x^{m-1}\phi(x)}{n^{2}} \text{ where } m > 2, \ n \ge 1 ?$$

(a) $(m \sin nx + n \cos nx)$

.

- (b) $n \cos nx m \sin nx$
- (c) $mx \cos nx + n(n-1) \sin nx$
- (d) $m \cos nx + nx \sin nx$

Math.

7

23. Given that

$$\int_0^1 \frac{\log(1+x)}{x} \, dx = \frac{\pi^2}{12}.$$

What is the value of the integral

$$\int_0^1 \frac{\log x}{1+x} \, dx \, ?$$

(a)
$$-\frac{\pi^2}{12}$$

(b) $\frac{\pi^2}{6}$
(c) $\frac{\pi}{12}$

(d) None of the above

24. For what value of $\phi(x)$,

$$\int_a^b \phi(x) \, dx$$

gives the length of the arc for the curve y = f(x) between two points whose abscissa are a and b where f'(x) is continuous and single valued in the range (a, b)?

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(a) $\left\{1+(f'(x))^2\right\}^{\frac{3}{2}}$

(b)
$${f(x) + f'(x)}^{\frac{1}{2}}$$

(c)
$$\left\{1+(f'(x))^2\right\}^{1/2}$$

(d) None of the above

4

Math.

25. The necessary and sufficient condition for a vector function $\overrightarrow{f}(t)$ to have constant direction is :

....

(a)
$$\vec{f} + \frac{\vec{d}f}{dt} \times \frac{\vec{d^2}f}{dt^2} = 0$$

12

(b)
$$\vec{f} \times \frac{\vec{df}}{dt} = 0$$

(c)
$$\vec{f} \cdot \frac{\vec{d}f}{dt} = 0$$

(d) None of the above

26. If
$$f$$
 and g are continuously differentiable vector point functions, then :

2

$$\operatorname{curl} (\vec{f} \times \vec{g}) + (\vec{f} \cdot \nabla) \vec{g} - (\vec{g} \cdot \nabla) \vec{f} =$$

(a) $\vec{f} \operatorname{div} \vec{g} - \vec{g} \operatorname{div} \vec{f}$

(b)
$$\vec{f} \times \operatorname{curl} \vec{g} + \operatorname{curl} \vec{f} \times g$$

(c)
$$\vec{f} \cdot \operatorname{curl} \vec{g} - \vec{g} \cdot \operatorname{curl} \vec{f}$$

- (d) None of the above
- 27. Which of the following is the integrating factor of the differential equation :

$$(1+x)\frac{dy}{dx}-xy=1-x?$$

9

(a) $e^{-\frac{x}{2}}$ (b) e^{-x} (c) $-x + e^{1+x}$ (d) $e^{-x}(1+x)$

Math.

28. What is the value of

$$\left(\frac{1}{D^2-5D+6}\right)xe^x?$$

(a) $e^{x}(6x-5)$

(b)
$$\frac{e^x}{2}(5x^2+6x+1)$$

(c)
$$\frac{e^x}{4}(2x+3)$$

(d) None of the above

Which of the following transformations reduce the differential equation :

$$xp^2 - 2yp + x + 2y = 0$$
, where $p = \frac{dy}{dx}$,

- to Clairaut's form ?
- (a) $x^2 = u, y^2 = v$
- (b) $x^2 = u, y x = v$

(c)
$$x + y = u$$
, $xy = v$

- (d) None of the above
- 30. If $P_n(x)$ denote Legendre's polynomials for different values of positive integer n, then for what value of $\psi(n)$:

$$P_{n+1}(x) - P_{n-1}(x) = \psi(n) P_n(x)$$
?

- (a) 2n
- (b) n + 1
- (c) 2n + 1
- (d) None of the above

Math.

31. Let

$$\mathbf{G} = \begin{bmatrix} \mathbf{1} & \mathbf{1} & \mathbf{3} \\ \mathbf{0} & \mathbf{1} & -\mathbf{1} \\ \mathbf{2} & \mathbf{0} & -\mathbf{4} \end{bmatrix}$$

If H = adjoint of G, what is :

 $[H]_{22} + [H]_{32}$ equal to ?

(a) -8

- (b) 12
- (c) -12
- (d) None of the above

32.

Let Q be a skew-symmetric matrix of order three, then which of the following is always *true* ?

(a) Q^2 and Q^3 are both skew-symmetric matrices

(b) Q^2 and Q^3 are both symmetric matrices

(c) Q^2 is a skew-symmetric matrix but Q^3 is a symmetric matrix

(d) Q^2 is a symmetric matrix but Q^3 is a skew-symmetric matrix

33. Let

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| | 2 | 3 | 4] | | [1 | 3 | 0 | |
|-----|----|---|----|----------------|------------|---|---|--|
| G = | 1 | 2 | 3 | and H = | -1 | 2 | 1 | |
| | _1 | 1 | 2 | | 0 | 0 | 2 | |

then what is the trace GH ?

5.2

- (a) 30
- (b) 11
- (c) 13
- (d) None of the above

Math.

34. For what value of β ,

3

$$\lambda^3 - 12\lambda^2 + \beta\lambda - 32 = 0$$

is the characteristic equation of the matrix

$$\begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}?$$

(a) 36

(b) 46

(c) 38

(d) None of the above

35. How many linearly independent solutions does the equation

$$7x + 6y - 11z + 14 = 0$$

have ?

- (a) None
- (b) One
- (c) Two

(d) Three

36. For what value of λ , the column vectors

$$\mathbf{X}_{1} = \begin{bmatrix} 7\\5\\3 \end{bmatrix}, \ \mathbf{X}_{2} = \begin{bmatrix} 1\\-2\\2 \end{bmatrix}, \ \mathbf{X}_{3} = \begin{bmatrix} 11\\\lambda\\0 \end{bmatrix}$$

are linearly dependent ?

(a) 4

(b) 16

(c) **-3**

(d) None of the above

Math.

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- 37. Every polynomial equation of degree 2n + 1, $n \ge 1$, with real coefficients always has :
 - (a) no real roots
 - (b) 2n real roots
 - (c) n real roots
 - (d) at least one real root

38. Given that $x = -\frac{3}{2}$ is a root of the equation

$$4x^3 + 12x^2 + 11x + 3 = 0$$

what are its other two roots ?

- (a) -1, 2
- (b) $1, \frac{1}{2}$ (c) $-1 - \frac{1}{2}$

(c)
$$-1, -\frac{1}{2}$$

(d) None of the above

39. If $P(z) = z^3 + 3Hz + G$ and $G^2 + 4H^3$ is negative, then the cubic equation P(z) = 0 always has :

- (a) all the three roots equal
- (b) two equal roots
- (c) one real and two complex roots
- (d) all the three roots real
- 40. If α , β , γ are the roots of the equation

$x^3 - 9x^2 + 14x + 24 = 0,$

what is the value of $1 + \Sigma \frac{1}{\alpha}$?

(a) $\frac{5}{12}$ (b) $\frac{19}{12}$ (c) $\frac{10}{9}$ (d) None of the above

Math.



41. Consider the set

$$\mathbf{S} = \left\{ \frac{2n+1}{n}; \ n \in \mathbf{N} \right\}.$$

If l is the supremum and g is the infimum of the set S, then which of the following is *true*?

- (a) *l* belongs to S whereas g does not
- (b) g belongs to S whereas l does not
- (c) l and g both belong to S
- (d) None of the above
- 42. The sequence $\{S_n\}$ where

$$\mathbf{S}_n = \frac{(-1)^{n-1}}{n!}, n \in \mathbf{N},$$

is :

- (a) not bounded but has one limit point
- (b) bounded but has no limit point
- (c) bounded and has only one limit point
- (d) bounded and has two limit points

43. Let $\sum_{1}^{\infty} u_n$ be a positive term series such that :

$$\frac{u_n}{u_{n+1}} = \alpha + \frac{\beta}{n} + \frac{\gamma_n}{n^p},$$

where $\alpha > 0$, p > 1 and $\{\gamma_n\}$ is a bounded sequence, then for $\alpha \neq 1$, which of the following is *true*?

- (a) $\sum_{1}^{\infty} u_n$ converges if $\alpha < 1$ and diverges if $\alpha > 1$ whatever β may be
- (b) $\sum_{n=1}^{\infty} u_n$ converges if $\alpha > 1$ and diverges if $\alpha < 1$ for all real β
- (c) $\sum_{1}^{\infty} u_n$ converges if $\beta < 1$ and diverges if $\beta > 1$ for all real $\alpha \neq 1$
- (d) None of the above

Math.

- Let the function f(x) be defined by 44.
 - f(x) = 1 when x is irrational
 - = -1 when x is rational,

then f(x) is :

- (a) continuous at every point
- (b) discontinuous at every point
- continuous at rationals and discontinuous at irrationals (c)
- (d) none of the above
- If [x] denotes the greatest integer not greater than x, then what is the value 45. of the integral

$$\int_0^8 [x] dx ?$$

- (a) Does not exist
- (b) Zero 9 2 (c)
- (d) 3

Let $f(x) = \sin x$, $x \in [0, t]$ where $t \le \frac{\pi}{2}$. Consider a partition 46.

$$p = \left\{0, \frac{t}{n}, \frac{2t}{n}, \frac{3t}{n}, \dots, n\frac{t}{n}\right\}$$

of the interval [0, t]. Then which of the following is equal to $\frac{n}{t} \{L(p, f)\}$?

(a)
$$\left(\sin\frac{t}{n}\right) - \frac{n}{t}\cos t$$

(b)
$$\cos\frac{t}{n} + \cos\frac{2t}{n} + \dots + \cos\frac{nt}{n}$$

(c)
$$\sin \frac{t}{n} + \sin \frac{2t}{n} + \dots + \sin (n-1) \frac{t}{n}$$

(d)
$$\sin \frac{t}{n} + \sin \frac{2t}{n} + \dots + \sin \frac{nt}{n}$$

Math.

47. Let
$$f(x, y) = x \sin\left(\frac{1}{y}\right) + y \sin\left(\frac{1}{x}\right), xy \neq 0$$

= 0, $xy = 0$

then what is the value of the limit $\lim_{(x, y)\to(0, 0)} f(xy)$?

- Does not exist (a)
- (b) 00
- 2 (c)
- (d) Zero

48. Let
$$f(x, y) = \frac{x^2 y^2}{x^2 + y^2}, (x, y) \neq (0, 0)$$

 $= 0, \qquad x = y = 0$

If $l = f_x(0, 0)$ and $m = f_x(2, 1)$, what is the value of the pair (l, m)?

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 $\left(0,\frac{4}{25}\right)$ (a) (0, 1) **(b)** 1 41

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(c)
$$\left(0,\frac{4}{5}\right)$$

32.90

(d) None of the above

If $x = r \cos \theta$ and $y = r \sin \theta$, which of the following is equal to the pair 49.

$$\begin{pmatrix} \frac{\partial r}{\partial \mathbf{x}}, \frac{\partial \theta}{\partial \mathbf{y}} \end{pmatrix} ?$$
(a) $\left(\sec \theta, \frac{\sec \theta}{r} \right)$
(b) $\left(\sec \theta, \frac{\cos \theta}{r^2} \right)$
(c) $\left(\cos \theta, \frac{\cos \theta}{r} \right)$

None of the above (d)

Math.

50. If

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$$F(x, y) = x^2 + y^2 + \lambda (x^2 + 8xy + 7y^2 - 225),$$

then what is the value of $d^2 F$ at $\lambda = -\frac{1}{9}$ where $\frac{\partial F}{\partial x} = 0$ and $\frac{\partial F}{\partial y} = 0$?

(a) $-\frac{4}{9}(4(dx)^2+(dy)^2)$

(b)
$$\frac{4}{9}(2dx - dy)^2$$

(c)
$$\frac{16}{9}(dx)^2$$

- (d) None of the above
- 51. What is the value of the double integral

$$\iint\limits_{\mathbf{R}} (x^2 + y^2) dx dy$$

where **R** = $\{(x, y); x^2 + y^2 \le \sqrt{2}\}$?

- (a) π
- (b) 2π
- (c) $2\sqrt{2}\pi$

(d) None of the above

Math.

17

52. Which of the following is the value of the triple integral

where

$$\mathbf{R} = \{(x, y, z); 0 < z < y, 0 < y < x, 0 < x < 1\} ?$$

- $\frac{1}{8}$ (a) (b) $\frac{1}{48}$
- (c)
- (d) None of the above
- Let Z_1 be the set of all non-negative integers and Q_1 be the set of all non-53. zero rational numbers, then which of the following is true ?
 - Z_1 is not a group under addition composition but Q_1 is a group under (a) multiplication composition
 - $\mathbf{Q}_{\mathbf{J}}$ is not a group under multiplication composition but \mathbf{Z}_1 is a group (b) under addition composition
 - \mathbf{Z}_1 and \mathbf{Q}_1 are groups under the composition of addition and multipli-(c) cation respectively
 - (d) None of the above
- Let Z be the additive group of integers and let H, denote the set of all multiples 54. of a positive integer t then which of the following is true ?
 - (a) H_{15} is not a subgroup of Z but H_{19} is a subgroup of Z
 - (b) H₁₅ is a subgroup of Z but H₁₉ is not a subgroup of Z
 - Both H₁₅ and H₁₉ are not subgroups of Z (c)
 - Both ${\rm H}_{15}$ and ${\rm H}_{19}$ are subgroups of Z (d)

Math.

55. Let Z be the set of all integers and $G = \{1, -1\}$. Here G is a group under multiplication. Define a mapping

$$f: \mathbb{Z} \to \mathbb{G}$$

by putting f(n) = 1 if n is even and f(n) = -1 if n is odd. Then which of the following is *true*?

- (a) $f(m + n) \neq f(m)$ f(n) for all m, n in Z
- (b) f(m + n) = f(m) f(n) for all m, n in Z but f is not onto
- (c) f(m + n) = f(m) f(n) for all m, n in Z and f is also onto
- (d) None of the above
- 56. What is the number of distinct cycles of length 4 in S_{g} , the symmetric group of degree 9 ?
 - (a) 3024
 - (b) 126
 - (c) 36
 - (d) 756

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57. A ring with unity is called a division ring if :

- (a) it has proper zero divisors
 - (b) its all non-zero elements form a group under multiplication
 - (c) its all non-zero elements form a group under addition
 - (d) None of the above

Math.

19

58. Let

$$\mathbf{R}_1 = \left\{ \begin{bmatrix} a & 0 \\ 0 & 0 \end{bmatrix} \middle| a \in \mathbf{R} \right\},\$$

.

where R is a ring. Define a mapping $f : \mathbf{R}_1 \to \mathbf{R}$ by

$$f\left(\begin{bmatrix}a & 0\\ 0 & 0\end{bmatrix}\right) = a \text{ for all } \begin{bmatrix}a & 0\\ 0 & 0\end{bmatrix} \in \mathbf{R}_1,$$

then which of the following is true ?

- (a) $f(X + Y) \neq f(X) + f(Y)$ for all X, Y in R₁
- (b) $f(XY) \neq f(X)f(Y)$ for all X, Y in \mathbb{R}_1
- (c) $f(XY) \neq f(X)f(Y)$ but f(X + Y) = f(X) + f(Y) for all X; Y in R_1

(d)
$$f(XY) = f(X)f(Y)$$
 and $f(X + Y) = f(X) + f(Y)$ for all X, Y in \mathbb{R}_1

59. Let P = R[x] and let f(x), g(x) h(x), $h(x) \in P$ be such that

$$f(t) = 1, g(t) = t, h(t) = t^2, k(t) = 1 + t + t^2$$

for all $t \in \mathbb{R}$, then which of the following is true ?

- (a) f(x), g(x), h(x), k(x) are linearly independent
- (b) f(x), g(x), h(x) are linearly independent
- (c) f(x), g(x), h(x) are linearly dependent
- (d) None of the above
- 60. Let C be the field of complex numbers. We can regard C as a vector space over itself. Define $T : C \rightarrow C$ such that :

T(Z) = x for any Z = x + iy, $x, y \in R$,

then which of the following is true ?

- (a) $T((2 + i) (2 i)) \neq (2 + i) T (2 i)$
- (b) T((2 + i) (2 i)) = (2 + i) T(2 i)
- (c) $T(Z_1 + Z_2) \neq T(Z_1) + T(Z_2)$, where $Z_1 = x_1 + iy_1$, $Z_2 = x_2 + iy_2$, x_1, x_2, y_1 , $y_2 \in \mathbb{R}$

(d) None of the above

Math.

HOME SCIENCE

- 1. Polyandry refers to :
 - (A) one man marrying one woman
 - (B) one man marrying more than one woman
 - (C) one woman marrying more than one man
 - (D) none of the above
- 2. A value of variable which divides the series in such a manner that number of items below it is equal to the number of items above it, is called :
 - (A) Mean
 - (B) Mode
 - (C) Median
 - (D) Average
- 3. Which of the following is not a measure of dispersion ?
 - (A) Range
 - (B) Mean Deviation
 - (C) Standard Deviation

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(D) Class Interval

4. The UN resolution on discrimination against women was adopted in :

- (A) 1967
- (B) 1963
- (C) 1975
- (D) 1981
- 5. Who was the Chairman of Indian Education Commission ?
 - (A) D.S. Kothari
 - (B) J.P. Naik
 - (C) Hamid Ansari
 - (D) None of the above

Home Sc.

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- 6. Integration of pupils with learning difficulties into regular class rooms for all or a part of school day is called :
 - (A) Guidance
 - (B) Mainstreaming
 - (C) Counselling
 - (D) Directing
- 7. Down's syndrome refers to :
 - (A) Nutritional Deficiency
 - (B) Infection
 - (C) Temp. Shock
 - (D) Chromosomal Abnormality
- 8. Which of the following are known as protective foods ?
 - (A) Fruits
 - (B) Fats and oils
 - (C) Cereals
 - (D) All of the above
- 9. Which of the following should necessarily be supplied through diet ?
 - (A) Short chain fatty acids
 - (B) Long chain fatty acids
 - (C) Essential fatty acids
 - (D) Non-essential fatty acids
- 10. Which of the following is a water soluble vitamin ?
 - (A) Vit. E
 - (B) Vit. D
 - (C) Vit. A
 - (D) Vit. C

Home Sc.

- 11. Major part of wheat flour is obtained from which part of the seed ?
 - (A) Endosperm
 - (B) Germ
 - (C) Aleuron layer
 - (D) Scutellum
- 12. Which of the following are filamentous ?
 - (A) Bacteria
 - (B) Yeast
 - (C) Fungi
 - (D) None of the above
- 13. Who is the basic functionary in a community development programme ?
 - (A) Gram Sewak
 - (B) BDO
 - (C) District Collector
 - (D) None of the above
- 14. In Panchayati Raj, the Sarpanch is elected by :
 - (A) People
 - (B) Panchayat Members
 - (C) MLAs
 - (D) Nominated by DC
- 15. In a communication model, which of the following is the first element of communication ?
 - (A) Treatment
 - (B) Message
 - (C) Sender
 - (D) Channel

Home Sc.

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- 16. Symposia are the examples of :
 - (A) Mass approach
 - (B) Group approach
 - (C) Individual approach
 - (D) None of the above
- 17. Which of the following statements about a poster is false ?

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- (A) Always write captions vertically
- (B) Bring out the message clearly
- (C) Use bright attractive colours
- (D) It should recommend action
- 18. Film projectors are included in :
 - (A) Reflected projectors
 - (B) Indirect projectors
 - (C) Direct projectors
 - (D) None of the above
- 19. Which of the following have a background of coloured cloth ?
 - (A) White board
 - (B) Black board
 - (C) Bulletin board
 - (D) All of the above
- 20. Which of the following is not a poverty alleviation programme ?
 - (A) NREP
 - (B) TRYSEM
 - (C) IRDP
 - (D) ICDS

Home Sc.

- 21. Which of the following is not a component of staffing ?
 - (A) Placement
 - (B) Transfers
 - (C) Directing
 - (D) Training
- 22. Write the odd one :
 - (A) Knowledge
 - (B) Money
 - (C) Skills
 - (D) Interest
- 23. The measurement of the amount of light emitted by a bulb is called its :

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- (A) Lumen
- (B) Watt
- (C) Wattage
- (D) Reflection
- 24. Which of the following soil types can bear maximum pressure of building on it ?
 - (A) Hard clay
 - (B) Sandy clay
 - (C) Sandy loams
 - (D) Moist soils
- 25. Which of the following statements pertain to organismic theory/theories of child development ?
 - (A) Psychological structures exist inside
 - (B) Change is stimulated by environment
 - (C) Both the above
 - (D) None of the above

Home Sc.

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- 26. Directly observable features of a person are known as :
 - (A) Prototype
 - (B) Phenotype
 - (C) Genotype
 - (D) Karyotype
- 27. Each cell in our body contains :
 - (A) 23 pairs of genes
 - (B) 46 pairs of genes
 - (C) 23 pairs of chromosomes
 - (D) 46 pairs of chromosomes
- 28. Which of the following is an X linked disease ?
 - (A) Hemophilia
 - (B) Cystic fibrosis
 - (C) PKU
 - (D) Sickle Cell Anemia
- 29. Palmer grasp disappears at the age of :
 - (A) 2 years
 - (B) 18 months
 - (C) 1 year
 - (D) 3-4 months
- 30. An organized pattern of physical growth and motor control that proceeds head to tail is called :
 - (A) Cephalocaudal trend
 - (B) Cephalothoracic trend
 - (C) Proximodistal trend
 - (D) Dynamic systems theory

Home Sc.
- 31. A standard of fairness in which individuals express the same concern for the welfare of others as they do for themselves is known as :
 - (A) Reciprocity
 - (B) Autonomous morality
 - (C) Realism
 - (D) Heteronymous morality
- 32. Vishwa Bharati at Shantiniketan was established by :
 - (A) Gandhiji
 - (B) Rabindranath Tagore
 - (C) G.K. Gokhale
 - (D) Jawahar Lal Nehru
- 33. The feeling of satisfaction which a person derives out of the use of a good or service is called :
 - (A) Psychic income
 - (B) Real income
 - (C) Money income
 - (D) None of the above
- 34. Which of the following acts protects consumers from hazards of food adulteration ?
 - (A) Dangerous Drug Act
 - (B) Weights and Measurement Act
 - (C) FPO
 - (D) PFA
- 35. In which of the following the return is in the form of profit ?
 - (A) Bonds
 - (B) Shares
 - (C) Both the above
 - (D) None of the above

Home Sc.

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- 36. Windows placed on the walls raised above the roof to allow light and air is called :
 - (A) Clerestory
 - (B) Ventilator
 - (C) Exhaust
 - (D) Aerator
- 37. Which of the following is an alkaline salt of fatty acid ?
 - (A) Washing soda
 - (B) Detergents
 - (C) Disinfectants
 - (D) Soaps
- 38. Which of the following is used as an egg beater ?
 - (A) Whisks
 - (B) Mixers
 - (C) Grinders.
 - (D) All of the above
- 39. Which of the following is not a component of a refrigerator ?
 - (A) Beater
 - (B) Compressor
 - (C) Expansion valve
 - (D) Gasket
- 40. The ironing surface of an electric iron is known as :
 - (A) Sole plate
 - (B) Hot plate
 - (C) Heating mantle
 - (D) Thermoregulator

Home Sc.

- 41. Which of the following is the more appropriate appliance to heat a Samosa or a patti ?
 - (A) Hot air oven
 - (B) Microwave oven
 - (C) BOD incubator
 - (D) Toaster
- 42. Which of the following is not a primary colour ?
 - (A) Red
 - (B) Yellow
 - (C) Blue
 - (D) Green
- 43. Staple is associated with :
 - (A) Dimensions of fibre
 - (B) Elasticity of fibre
 - (C) Colour of fibre
 - (D) All of the above
 - 44. Cotton is an example of fibre.

- (A) Protein
- (B) Mineral
- (C) Cellulosic
- (D) Thermoplastic
- 45. The process of pressing the fabric to smooth out wrinkles and add sheen to it is known as :

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- (A) Beetling
- (B) Embossing
- (C) Sanforising
- (D) Calendering

Home Sc.

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P.T.O.

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- 46. Which of the following is not used for solubility test of fibres ?
 - (A) Ethanol
 - (B) Acetone
 - (C) Phenol
 - (D) Conc. Sulphuric acid
- 47. Which of the following absorbs moisture readily ?
 - (A) Linen
 - (B) Cotton
 - (C) Nylon
 - (D) Non-difference
- 48. Which of the following laundry blues are insoluble in water ?
 - (A) Ultramarine
 - (B) Prussian blue
 - (C) Methylene blue
 - (D) Coal tar dyes
- 49. Energy required by the body when lying at rest in a comfortable environment, mentally relaxed and without food is known as :
 - (A) RDI
 - (B) SDA
 - (C) RDA
 - (D) BMR
- 50. Which of the following yields highest energy in the body ?
 - (A) Vitamins
 - (B) Carbohydrates
 - (C) Protein
 - (D) Fat

Home Sc.

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- 51. Calcium requirements increase in :
 - (A) Third trimester of pregnancy
 - (B) Second trimester of pregnancy
 - (C) First trimester of pregnancy
 - (D) Do not change
- 52. Protein requirement during infancy (first 6 months) is :
 - (A) 10 g/kg body weight
 - (B) 15 g/kg body weight
 - (C) 5 g/kg body weight
 - (D) 2 g/kg body weight
- 53. Which of the following is a monosaccharide ?
 - (A) Glucose
 - (B) Lactose
 - (C) Sucrose
 - (D) Maltose
- 54. Which of the following is starch?
 - (A) Lactose
 - (B) Cellulose
 - (C) Pectin
 - (D) Amylopectin
- 55. Which of the following is a saturated fatty acid ?
 - (A) Palmitic acid
 - (B) Oleic acid
 - (C) Linoleic acid
 - (D) Linolenic acid

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Home Sc.

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56. Which of the following is a sulphur containing amino acid ?

- (A) Cystein
- (B) Cystine
- (C) Methionine
- (D) All of the above
- 57. Enzymes are in nature.
 - (A) Proteins
 - (B) Carbohydrates
 - (C) Fats

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- (D) None of the above
- 58. Which of the following need metabolic energy ?
 - (A) Diffusion
 - (B) Passive transport
 - (C) Active transport
 - (D) All of the above
- 59. Which of the following catalyse blood clotting ?
 - (A) Calcium
 - (B) Fluoride
 - (C) Copper
 - (D) All of the above
- 60. National Institute of Nutrition (NIN) is located at :
 - (A) Hyderabad
 - (B) Bangalore
 - (C) Mysore
 - (D) Delhi

Home Sc.

HOME SCIENCE

- 1. Which of the following statements is not true about ovum :
 - (A) Contains 23 chromosomes
 - (B) Develops in ovaries
 - (C) Elongated with a fine hair like tail
 - (D) Contains yolk
 - 2. In human development, the germinal stage lasts for after fertilization.
 - (A) 10 days-10 weeks
 - (B) 10 days-2 weeks
 - (C) 4 weeks-6 weeks
 - (D) 12 weeks-20 weeks
 - 3. An average baby can walk with help at the age of :
 - (A) 6-8 months
 - (B) 4-6 months
 - (C) 16-18 months
 - (D) 9-11 months
- 4. A child starts making use of holophrases at the age of :
 - (A) 1 year
 - (B) 2 years
 - (C) 6 months
 - (D) 4 months

Hom. Sc.

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- 5. The psychosocial theory of personality development was given by :
 - (A) Erik Erikson
 - (B) Sigmund Freud
 - (C) Yarrow
 - (D) Pederson
- 6. A child is in anal stage from :
 - (A) 1½-3 years
 - (B) Birth-11/2 years
 - (C) 3-4 years
 - (D) 4-5 years
- 7. Slanting eyes is a feature of :
 - (A) Cretinism
 - (B) Microcephaly
 - (C) Mongolism
 - (D) Albinism
- 8. A child plays independently among other children and does not influence or modify the activity of other children. The play is :
 - (A) Solitary independent play
 - (B) Associative play
 - (C) Parallel play
 - (D) Organized supplementary play

- 9. When parents try to control their children's behaviour and make them conform to a set and usually absolute standard of conduct, they are :
 - (A) Authoritarian parents
 - (B) Authoritative parents
 - (C) Permissive parents
 - (D) None of the above
- 10. Enuresis refers to :
 - (A) Sleeplessness
 - (B) Bed wetting;
 - (C) Down's syndrome
 - (D) Night blindness
- 11. Resilience refers to of fiber.
 - (A) Flexibility
 - (B) Strength
 - (C) Water absorption
 - (D) Springiness
- 12. Which of the following methods is used for determining hair weight of textiles ?
 - (A) Clegg's method
 - (B) Winson's method
 - (C) A.S.T.M. method
 - (D) All of the above

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- 13. Fells are the fabrics made by :
 - (A) Passing one set of yarns above and below another
 - (B) Twisting many fibers about each other
 - (C) Looping one yarn about itself
 - (D) Uniting loose fibers
- 14. The number of units of weight in a unit of length is given by :
 - (A) Denier
 - (B) Plies
 - (C) Crimp
 - (D) None of the above
- 15. Which of the following is a cellulosic material ?
 - (A) Cotton
 - (B) Silk
 - (C) Wool
 - (D) None of the above

16. Which of the following needs weight and height for its calculation ?

- (A) BMR
- (B) BMI
- (C) PER
- (D) BV

- 17. Which of the following is not used for anthropometric methods of nutritional assessment ?
 - (A) Height
 - (B) Mid arm circumference
 - (C) Head circumference
 - (D) Haemoglobin
- 18. The major objective of mid day meal programme is :
 - (A) To provide minerals to infants
 - (B) To provide vit. D to pregnant ladies
 - (C) To provide protein to poor children
 - (D) To reduce school dropouts
- 19. Potable water refers to :
 - (A) Water that can be transported
 - (B) Water which contains minerals
 - (C) Water which is safe for drinking
 - (D) Water which contains pathogens

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- 20. Which of the following pertains to food adulteration ?
 - (A) PFA
 - (B) FPO
 - (C) MFPO
 - (D) All of the above
- 21. Which of the following is a water soluble vitamin ?
 - (A) Vit. A
 - (B) Vit. C
 - (C) Vit. D
 - (D) All of the above
- 22. Which of the following components of wheat grain contributes to flour ?
 - (A) Endosperm
 - (B) Germ
 - (C) Epicotyle
 - (D) Hypocotyle
- 23. Which of the following is a pome fruit ?
 - (A) Apple
 - (B) Grapes
 - (C) Banana
 - (D) Strawberry

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- 24. Which of the following is comprised of glucose and galactose ?
 - (A) Sucrose
 - (B) Lactose
 - (C) Maltose
 - (D) None of the above
- 25. Which of the following undergoes saponification ?
 - (A) Fatty acids
 - (B) Glycogen
 - (C) Cellulose
 - (D) Pectin

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- 26. Which of the following is the activity of management ?
 - (A) Planning
 - (B) Organizing
 - (C) Leading
 - (D) All of the above
- 27. The lumen is the measurement of :
 - (A) Light emitted
 - (B) Power consumed
 - (C) Heat emitted
 - (D) All of the above

Hom. Sc.

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28. A continuous magnet is embedded in the gasket of the refrigerator :

- (A) To attract metallic pieces from food
- (B) To prevent chilling injury
- (C) To hold the door of refrigerator tightly
- (D) To reduce the temperature
- 29. The sole plate of electric iron is coated with :
 - (A) Chromium
 - (B) Silver
 - (C) Iron
 - (D) Foam
- 30. An education which is institutional activity, subject oriented, full time and leads to certificates and degrees is called :
 - (A) Technical education
 - (B) Extension education
 - (C) Non-formal education
 - (D) Formal education
- 31. Rural reconstruction institute was started by Rabindra Nath Tagore at :
 - (A) Lucknow
 - (B) Gurgaon
 - (C) Shantiniketan
 - (D) Delhi

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Hom. Sc.

- 32. Which of the following is not a characteristic of extension ?
 - (A) Cooperative
 - (B) Informal
 - (C) Nonflexible
 - (D) Voluntary
- 33. Any change of behaviour which takes place as a result of experience may be called :
 - (A) Learning
 - (B) Formal education
 - (C) Adult education
 - (D) None of the above
- 34. Polyandry refers to :
 - (A) A man marrying more than one wife
 - (B) A woman marrying more than one husband
 - (C) Having many children
 - (D) All of the above

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- 35. Which of the following defined communication as "Process by which two or more people exchange ideas, facts, feelings or impressions in" a way that each gains common understanding of message" ?
 - (A) Leagans
 - (B) Coleman
 - (C) Schramm
 - (D) Loomis
- 36. Tick the odd one out :
 - (A) Frequency curves
 - (B) Frequency polygons
 - (C) Continuous curves
 - (D) Pictograms
- 37. Free radicle theory pertains to :
 - (A) Aging
 - (B) Child development
 - (C) Infancy
 - (D) Adolescence

- 38. Insomnia refers to :
 - (A) Lack of appetite
 - (B) Lack of thirst
 - (C) Inability to sleep
 - (D) Inability to breathe
- 39. The greek word 'geron' means :
 - (A) Old man
 - (B) Young man
 - (C) Young woman
 - (D) Infant
- 40. Zygote refers to :
 - (A) Male sex cell
 - (B) Female sex cell
 - (C) Cell formed as a result of fertilization
 - (D) None of the above
- 41. Neonate is the baby in :
 - (A) First month of life
 - (B) First year of life
 - (C) First two years of life
 - (D) First three years of life

- 42. The first conference on women was held in :
 - (A) 1975
 - **(B)** 1965
 - (C) 1955
 - (D) 1985
- 43. In India, the community development programme was launched in :
 - (A) 1975
 - (B) 1965
 - (C) 1947
 - (D) 1952
- 44. Krishi Vigyan Kendras are established by :
 - (A) ICAR
 - (B) ICMR
 - (C) ICCR
 - (D) NIN
- 45. Which of the following is an audio-visual aid ?
 - (A) Poster
 - (B) Radio
 - (C) Television
 - (D) Black-board

- 46. Which of the following is not a poverty alleviation programme ?
 - (A) IRDP
 - (B) JRY
 - (C) NREP
 - (D) ICDS
- 47. Which of the following is an unsaturated fatty acid ?
 - (A) Caproic acid
 - (B) Caprylic acid
 - (C) Capric acid
 - (D) Oleic acid
- 48. Which of the following contains a pyrole ring ?
 - (A) Carotene
 - (B) Vit. C
 - (C) Sucrose
 - (D) Hemoglobin
- 49. The sequence of amino acids linked by peptide bonds refers to which of the following structures of protein ?
 - (A) Primary
 - (B) Secondary
 - (C) Tertiary
 - (D) Quaternary

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- 50. The non-protein organic component of enzymes is called :
 - (A) Zymogen

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- (B) Prosthetic group
- (C) Apoenzyme
- (D) Isozyme
- 51. Fat is stored in :
 - (A) Adipose tissue
 - (B) Neural tissue
 - (C) Muscle tissue
 - (D) Epithelial tissue
- 52. Hemoglobin contains :
 - (A) Iron
 - (B) Magnesium
 - (C) Calcium
 - (D) All of the above

Hom. Sc.

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- 53. Glomerulus is present in :
 - (A) Axon
 - (B) Neuron
 - (C) Dendron
 - (D) Nephron
- 54. Fundus is a part of :
 - (A) Kidney
 - (B) Stomach
 - (C) Lung
 - (D) Brain

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- 55. Which of the following is associated with dental caries :
 - (A) Iodide
 - (B) Chloride
 - (C) Fluoride
 - (D) Bromide
- 56. National Institute of Nutrition is affiliated to :
 - (A) ICMR
 - (B) UGC
 - (C) ICAR
 - (D) None of the above

Hom. Sc.

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- 57. Demonstrating the jam making rural women is an example of :
 - (A) Method demonstration
 - (B) Result demonstration
 - (C) Technical demonstration
 - (D) All of the above
- 58. Which of the following is Vit. C?
 - (A) Calciferol
 - (B) Tocopherol
 - (C) Ascorbic acid
 - (D) β -carotene
- 59. Which of the following is most suitable for delivering a lecture ?
 - (A) MS word
 - (B) MS Axel
 - (C) MS Power Point
 - (D) MS Access
- 60. Which of the following is used in jam making ?
 - (A) Gelatin
 - (B) Starch
 - (C) Pectin
 - (D) All of the above